#### Dependence of breakup probability estimation on ScFi background

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#### Abstract

ScFi detector plays essential role in measurement of transversal components of relative momentum Q. For correct simulation of "Coulomb" correlation function it is needed to know errors of measurement which are induced by resolution of the detector and admixture of background hits in the experimental data. Influence of background hits on measured value of breakup probability is investigated.

## Introduction

Background hits in ScFi detector could change a shape of "atomic" and "Coulomb" pair distributions. If there are two hits from particles of "atomic pair" in one ScFi plane then presence of 3-rd background hit leads to the event rejection by analysis procedure. But for the case of one correct hit per two particles (both particle hit the same column or one is not detected due to inefficiency) background hit could be taken as second one if it is sufficiently close in space (up to 2 cm) and in time ( $\pm 4$  ns). Therefore transverse component or relative momentum could be measured with big (few MeV/c) error.

The main source of additional hits is background particles. Their distribution and intensity was investigated and simulated recently [1].

The second source is a crosstalk between columns of fiber detector and optical crosstalk between PSPM channels.

In this report a probability of the second source is investigated. And influence of both background sources on the breakup probability is estimated.

## 1 Crosstalk

Numeration of ScFi channels in PSPM photocathodes is shown in Fig. 1.

Using channels from different PSPM it is possible to investigate crosstalk in ScFi detector itself with probability of two hits as function of column difference between them. For big distances this probability is constant. If crosstalk exists then for small distances probability is to increase.

32	31	30	29
25	26	27	28
24	23	22	21
17	18	19	20

16	15	14	13
9	10	11	12
8	7	6	5
1	2	3	4

Figure 1: Scheme of ScFi channel arrangement on the PSPM photocathodes.

After it is possible to repeat this procedure for channels connected to one PSPM. Subtracting effect of crosstalk in the detector it is possible to select pure optical crosstalk.

Analysis have been done using Ni2001 data. ARIANE based program selects events which fit a few criteria.

Firstly events have to have only one track per each arm.

On the second stage for each track the hits in X- (Y-) plane of fiber detector are found in  $\pm 1$  cm regions around X- (Y-) coordinate which provides upstream track pointed to the beam position at the target. Time difference between ScFi and VH measurement is in the limits  $\pm 4$  ns (time-of-flight is taken into account). Only event which have not crossed regions for different tracks and two hit at least in one space-time regions are selected.

Only two hit regions are used for final analysis.

To reject  $e^+e^-$  pairs the events with big amplitudes in Cherenkov counter are excluded. Admixture of  $e^+e^-$  pairs with low amplitudes have been estimated using PrSh detector. Influence of this events is compensated by subtracting of distribution filled by corresponding number of electron-positron pairs.

Table 1 presents probability of crosstalk from column number n to column number n+i as function of i. Evidently probability of crosstalk to column number n-i is the same. Statistical accuracy is at the level 0.02%.

Investigation of optical crosstalk in PSPM shows that crosstalk to the adjacent channel is at the level  $0.25 \div 0.30\%$  (see Table 2) and it is practically zero in "diagonal" (for example from channel 1 to channel 7 in Fig. 1) direction. Summary crosstalk probability to at least one of

1	i	Crosstalk	Crosstalk
		in X-plane	in Y-plane
		%	%
	1	4.68	5.18
4	2	0.80	0.82
	3	0.31	0.31
4	4	0.22	0.15
(	5	0.09	0.03
(	6	0.08	0.03
	7	0.07	0.01

Table 1: Probability of crosstalk from n-th column to n + i-th in the ScFi detector.

adjacent channel is at the level 1%. This is in agreement with ScFi detector description [2].

Plane	Downward	Upward	Downward	Upward
	directly	$\operatorname{directly}$	diagonally	diagonally
	%	%	%	%
X	0.25	0.24	0.01	-0.01
Y	0.28	0.29	0.01	0.01

Table 2: Probability of optical crosstalk to adjacent channel of PSPM.

# 2 Simulated pair distributions for different background conditions

In order to investigate dependence of  $A_{2\pi}$  breakup probability estimation on background conditions the "Coulomb" and "atomic" pair distributions have been simulated in 3 versions:

- 1. Monte-Carlo data generated by GEANT-DIRAC have been analyzed by ARIANE without generation of background hits.
- 2. ARIANE produces hits from background particle for intensity  $3.5 \cdot 10^{11} \text{s}^{-1}$ . In one plane of ScFi this intensity provides average multiplicity which is 4.
- 3. ARIANE produces hits from background particle for intensity  $3.32 \cdot 10^{11} s^{-1}$  and from crosstalk is ScFi detector and PSPM for distances from 2 to 8 columns (Tables 1,2). The crosstalk to adjacent column is treated by PSC response simulation. The average ScFi Plane multiplicity is also 4.

In Fig. 2a,b normalized distributions of "atomic pairs" over Q are presented. Solid line in Fig. 2a is the distribution of "atomic pairs" without background, dashed line in Fig. 2a and solid line in Fig. 2b are the distribution with background from particles only and dashed line Fig. 2b is a distribution with background both from particles and crosstalk. In Figs. 2c,d normalized distributions of "atomic pairs" over  $Q_L$  are presented in the same order like Q-distributions in Figs. 2a,b.

Results of simulation of "Coulomb pairs" are presented in Fig. 3 as correlation functions of Q without background (solid line Fig. 3a), with background from particles only (dashed line in Fig. 3a and solid line in Fig. 3b) and with background both from particles and crosstalk. Correlation function of  $Q_L$  are presented in Figs. 3c,d similarly to correlation functions of Q in Figs. 3a,b.

From Figs. 2,3 it is seen that distributions over Q are essentially modified by background in ScFi detector. For  $Q_L$  such modification is significantly less.

## 3 Breakup probability for different background description

Experimental data obtained in 2001 with nickel targets have been analyzed using three sets of simulated data. Experimental correlation function is approximated by a mixture of "Coulomb" and "non-Coulomb" correlation function i the regions where "atomic pair" are absent. Fraction of "non-Coulomb pairs" and normalization coefficient are free parameters of fit. After fit number of "free pairs" with small Q (or its projection) is calculated. An excess of experimental data over this number is a signal from "atomic pairs"  $N_a$ . Ratio of "atomic pair" number to "Coulomb pair" number  $N_a/N_C$  together with coefficient k which have been calculated for each version of background allows us to calculate breakup probability  $P_{\rm br}$ . Also total number of "atomic pairs"  $N_a^{\rm total}$  is calculated for each cut using simulated distribution of "atomic pairs" over Q and projections of Q.

For different cuts on  $Q_L$  table 3 presents a number of "atomic pairs"  $N_a$ , ratio of "atomic" and "Coulomb" pair numbers  $N_a/N_c$ , breakup probability  $P_{\rm br}$  and total number of "atomic pairs"  $N_a^{\rm total}$ . Cut on  $Q_T$  is 4 MeV/c. In tables 4,5,6,7,8 these values are given for different variables and cuts.

The data in tables 3,4,5,6,7,8 shows that results obtained with  $Q_L$  are less sensitive to presence of background in ScFi detector. Also it is seen that difference of "atomic pair" numbers and breakup probabilities between  $Q_L$  analysis and Q(F) analysis (which is an estimation of systematic error) is less if background is taken into account during simulation.

Another way to obtain  $N_a$  is to fit whole interval over Q using shape of simulated distribution of "atomic pairs". Table 9 contains numbers  $N_a$  obtained in this approach for different background description for simulation procedure.

It is seen that this version of analysis demonstrates the same dependence on background description as for previous one.

$Q_L$	$N_a$	$N_a/N_C$	$P_{ m br}$	$N_a^{ m total}$
		No backgro	ound.	
0.5	$3892. \pm 283.$	$0.1842 \pm 0.0157$	$0.4473 \pm 0.0382$	$6311. \pm 459.$
1.0	$5494. \pm 444.$	$0.1330 \pm 0.0124$	$0.4388 \pm 0.0409$	$6242. \pm 504.$
1.5	$6196. \pm 571.$	$0.1041 \pm 0.0109$	$0.4636 \pm 0.0486$	$6569. \pm 606.$
2.0	$6312. \pm 678.$	$0.0827 \pm 0.0099$	$0.4656 \pm 0.0558$	$6585. \pm 708.$
		Backgrou	ind.	
0.5	$3883. \pm 283.$	$0.1834 \pm 0.0157$	$0.4441 \pm 0.0381$	$6349. \pm 463.$
1.0	$5509. \pm 444.$	$0.1332 \pm 0.0124$	$0.4392 \pm 0.0409$	$6303. \pm 507.$
1.5	$6243. \pm 571.$	$0.1049 \pm 0.0109$	$0.4662 \pm 0.0485$	$6659. \pm 609.$
2.0	$6378. \pm 677.$	$0.0835 \pm 0.0099$	$0.4693 \pm 0.0557$	$6694. \pm 711.$
		Background and	l crosstalk.	
0.5	$3846. \pm 284.$	$0.1815 \pm 0.0156$	$0.4220 \pm 0.0363$	$6251. \pm 461.$
1.0	$5434. \pm 444.$	$0.1312 \pm 0.0123$	$0.4162 \pm 0.0390$	$6203. \pm 507.$
1.5	$6118. \pm 572.$	$0.1026 \pm 0.0109$	$0.4389 \pm 0.0466$	$6513. \pm 609.$
2.0	$6255. \pm 679.$	$0.0818 \pm 0.0099$	$0.4424 \pm 0.0536$	$6553. \pm 711.$

Table 3: Atomic pair numbers and ionization probability analyzed with  $Q_L(Q_T < 4)$ .

## Conclusions

These results allow to make three conclusions:

- Background hits in ScFi provide essential change of measured breakup probability and should to be taken into account during analysis.
- Despite of small fraction of background hits which occur due to crosstalk there influence is significant. Because they arise in vicinity to true hits in time and space. This fact allows then to fit selection criteria.
- Background hits distort mainly  $Q_T$ . Change of  $Q_L$  is essentially less. Therefore the best variable for analysis is  $Q_L$  because of  $Q_T$  value does not affect distribution of events between bins.
- [1] O. Gortchakov. Report on DIRAC analysis meeting.
- [2] B. Adeva *et all.*, Nucl. Instr. Meth. A515 (2003) 467.

$Q_L$	$N_a$	$N_a/N_C$	$P_{ m br}$	$N_a^{ m total}$
		No backgro	ound.	
0.5	$3852. \pm 248.$	$0.2779\pm0.0225$	$0.4645 \pm 0.0376$	$6533. \pm 421.$
1.0	$5348. \pm 390.$	$0.1979 \pm 0.0176$	$0.4451 \pm 0.0396$	$6356. \pm 464.$
1.5	$5766. \pm 501.$	$0.1493 \pm 0.0153$	$0.4473 \pm 0.0459$	$6398. \pm 556.$
2.0	$5760. \pm 590.$	$0.1174 \pm 0.0139$	$0.4399\pm0.0521$	$6290. \pm 645.$
		Backgrou	ind.	
0.5	$3897. \pm 248.$	$0.2815 \pm 0.0225$	$0.4733 \pm 0.0379$	$6689. \pm 425.$
1.0	$5406. \pm 389.$	$0.2001 \pm 0.0176$	$0.4524 \pm 0.0398$	$6497. \pm 468.$
1.5	$5888. \pm 499.$	$0.1526\pm0.0154$	$0.4597 \pm 0.0464$	$6599. \pm 559.$
2.0	$5912. \pm 588.$	$0.1206 \pm 0.0139$	$0.4548 \pm 0.0524$	$6522. \pm 649.$
		Background and	l crosstalk.	
0.5	$3877. \pm 248.$	$0.2797 \pm 0.0225$	$0.4550\pm0.0367$	$6604. \pm 422.$
1.0	$5392. \pm 390.$	$0.1995\pm0.0176$	$0.4381 \pm 0.0387$	$6452. \pm 466.$
1.5	$5823. \pm 500.$	$0.1507 \pm 0.0153$	$0.4402 \pm 0.0447$	$6500. \pm 558.$
2.0	$5847. \pm 589.$	$0.1191 \pm 0.0139$	$0.4350 \pm 0.0508$	$6425. \pm 647.$

Table 4: Atomic pair numbers and ionization probability analyzed with  $Q_L(Q_T < 3)$ .



Figure 2: Normalized distributions of "atomic pairs" over Q: (a) solid line — without background and dashed line with background from particles only, (b) solid line — background from particles only and dashed line — background both from particles and crosstalk. Normalized distributions of "atomic pairs" over  $Q_L$ : (c) solid line — without background and dashed line with background from particles only, (d) solid line — background from particles only and dashed line — background both from particles and crosstalk.



Figure 3: Simulated "Coulomb" correlation functions of Q: (a) solid line — without background and dashed line with background from particles only, (b) solid line — background from particles only and dashed line — background both from particles and crosstalk. Simulated "Coulomb" correlation functions of  $Q_L$ : (c) solid line — without background and dashed line with background from particles only, (d) solid line — background from particles only and dashed line background both from particles and crosstalk.

$Q_L$	$N_a$	$N_a/N_C$	$P_{ m br}$	$N_a^{ m total}$
		No backgro	ound.	
0.5	$3050. \pm 202.$	$0.4087 \pm 0.0373$	$0.4373 \pm 0.0400$	$6261. \pm 415.$
1.0	$4094. \pm 318.$	$0.2838\pm0.0289$	$0.4027 \pm 0.0410$	$5901. \pm 459.$
1.5	$4378. \pm 405.$	$0.2158 \pm 0.0250$	$0.4015 \pm 0.0465$	$5896. \pm 545.$
2.0	$4350. \pm 473.$	$0.1709 \pm 0.0226$	$0.3914 \pm 0.0518$	5766. $\pm$ 627.
		Backgrou	ınd.	
0.5	$3084. \pm 201.$	$0.4143 \pm 0.0373$	$0.4474 \pm 0.0403$	$6449. \pm 421.$
1.0	$4182. \pm 316.$	$0.2909 \pm 0.0290$	$0.4184 \pm 0.0417$	$6123. \pm 463.$
1.5	$4505. \pm 402.$	$0.2228\pm0.0251$	$0.4192 \pm 0.0472$	$6158. \pm 550.$
2.0	$4498. \pm 470.$	$0.1772 \pm 0.0226$	$0.4113 \pm 0.0525$	$6056. \pm 632.$
		Background and	l crosstalk.	
0.5	$3132. \pm 200.$	$0.4231 \pm 0.0376$	$0.4493 \pm 0.0400$	$6449. \pm 412.$
1.0	$4230. \pm 315.$	$0.2950\pm0.0290$	$0.4165 \pm 0.0410$	$6124. \pm 456.$
1.5	$4566. \pm 401.$	$0.2264\pm0.0252$	$0.4192\pm0.0467$	$6177. \pm 542.$
2.0	$4570. \pm 468.$	$0.1804 \pm 0.0227$	$0.4118 \pm 0.0518$	$6086. \pm 623.$

Table 5: Atomic pair numbers and ionization probability analyzed with  $Q_L(Q_T < 2)$ .

Q	$N_a$	$N_a/N_C$	$P_{ m br}$	$N_a^{ m total}$
		No backgro	ound.	
0.5	$274. \pm 53.$	$0.5632 \pm 0.1501$	$0.3084 \pm 0.0823$	$4985. \pm 969.$
1.0	$1361. \pm 122.$	$0.4466\pm0.0522$	$0.3367 \pm 0.0394$	$5278. \pm 475.$
1.5	$2511. \pm 214.$	$0.2706\pm0.0281$	$0.3057 \pm 0.0318$	$4814. \pm 410.$
2.0	$3417. \pm 324.$	$0.1784 \pm 0.0198$	$0.3081 \pm 0.0342$	$4713. \pm 447.$
2.5	$3837. \pm 456.$	$0.1159 \pm 0.0156$	$0.2991 \pm 0.0403$	$4523. \pm 538.$
3.0	$4376. \pm 602.$	$0.0860\pm0.0131$	$0.3219 \pm 0.0490$	$4777. \pm 658.$
3.5	$4573. \pm 762.$	$0.0627 \pm 0.0114$	$0.3290\pm0.0598$	$4810. \pm 801.$
4.0	$4546. \pm 933.$	$0.0455\pm0.0100$	$0.3232 \pm 0.0710$	$4691. \pm 963.$
		Backgrou	ınd.	
0.5	$282. \pm 53.$	$0.5896\pm0.1526$	$0.3194 \pm 0.0829$	$5252. \pm 982.$
1.0	$1445. \pm 120.$	$0.4869 \pm 0.0537$	$0.3761 \pm 0.0416$	$5763. \pm 480.$
1.5	$2670. \pm 211.$	$0.2926 \pm 0.0285$	$0.3348 \pm 0.0327$	$5220. \pm 413.$
2.0	$3643. \pm 321.$	$0.1924 \pm 0.0200$	$0.3359 \pm 0.0349$	$5108. \pm 450.$
2.5	$4100. \pm 452.$	$0.1247 \pm 0.0157$	$0.3245 \pm 0.0409$	$4896. \pm 540.$
3.0	$4660. \pm 598.$	$0.0920 \pm 0.0132$	$0.3466 \pm 0.0497$	$5141. \pm 660.$
3.5	$4891. \pm 757.$	$0.0673 \pm 0.0114$	$0.3545\pm0.0601$	5187. $\pm$ 802.
4.0	$4860. \pm 928.$	$0.0487 \pm 0.0100$	$0.3464 \pm 0.0711$	$5049. \pm 964.$
		Background and	l crosstalk.	
0.5	$313. \pm 51.$	$0.6973 \pm 0.1628$	$0.3945 \pm 0.0924$	$5695. \pm 923.$
1.0	$1474. \pm 119.$	$0.5016\pm0.0541$	$0.3834 \pm 0.0415$	$5749. \pm 466.$
1.5	$2704. \pm 210.$	$0.2972 \pm 0.0286$	$0.3384 \pm 0.0326$	$5214. \pm 406.$
2.0	$3724. \pm 319.$	$0.1973\pm0.0201$	$0.3406\pm0.0347$	5163. $\pm$ 443.
2.5	$4212. \pm 450.$	$0.1284 \pm 0.0157$	$0.3287 \pm 0.0402$	$4991. \pm 533.$
3.0	$4791. \pm 596.$	$0.0947 \pm 0.0132$	$0.3478\pm0.0485$	5263. $\pm$ 655.
3.5	$5014. \pm 755.$	$0.0690\pm0.0114$	$0.3524 \pm 0.0582$	$5303. \pm 798.$
4.0	$5005. \pm 926.$	$0.0502 \pm 0.0100$	$0.3446\pm0.0687$	$5188. \pm 960.$

Table 6: Atomic pair numbers and ionization probability analyzed with  $Q(Q_T < 4)$ .

Q	$N_a$	$N_a/N_C$	$P_{ m br}$	$N_a^{ m total}$
		No backgr	ound.	
0.5	$275. \pm 53.$	$0.5660 \pm 0.1497$	$0.3100 \pm 0.0821$	$5002. \pm 965.$
1.0	$1367. \pm 120.$	$0.4493 \pm 0.0507$	$0.3388 \pm 0.0383$	$5298. \pm 465.$
1.5	$2527. \pm 202.$	$0.2729 \pm 0.0260$	$0.3083 \pm 0.0294$	$4845. \pm 386.$
2.0	$3450. \pm 292.$	$0.1805 \pm 0.0176$	$0.3117 \pm 0.0304$	$4759. \pm 404.$
2.5	$3892. \pm 396.$	$0.1178 \pm 0.0134$	$0.3041 \pm 0.0346$	$4588. \pm 467.$
3.0	$4458. \pm 509.$	$0.0878 \pm 0.0110$	$0.3287 \pm 0.0412$	$4867. \pm 556.$
3.5	$4688. \pm 631.$	$0.0644 \pm 0.0094$	$0.3379 \pm 0.0493$	$4930. \pm 664.$
		Backgrou	ınd.	
0.5	$283. \pm 52.$	$0.5930 \pm 0.1522$	$0.3213 \pm 0.0826$	$5270. \pm 978.$
1.0	$1451. \pm 118.$	$0.4902 \pm 0.0522$	$0.3786 \pm 0.0404$	5788. $\pm$ 470.
1.5	$2689. \pm 199.$	$0.2954 \pm 0.0264$	$0.3380 \pm 0.0303$	$5257. \pm 389.$
2.0	$3681. \pm 290.$	$0.1949 \pm 0.0178$	$0.3402 \pm 0.0311$	$5161. \pm 406.$
2.5	$4163. \pm 393.$	$0.1269 \pm 0.0134$	$0.3302 \pm 0.0349$	$4971. \pm 470.$
3.0	$4753. \pm 506.$	$0.0941 \pm 0.0110$	$0.3545 \pm 0.0415$	$5244. \pm 558.$
3.5	$5020. \pm 627.$	$0.0692 \pm 0.0094$	$0.3645 \pm 0.0495$	$5324. \pm 665.$
		Background and	l crosstalk.	
0.5	$314. \pm 50.$	$0.7007 \pm 0.1624$	$0.3965 \pm 0.0922$	$5710. \pm 919.$
1.0	$1480. \pm 117.$	$0.5049 \pm 0.0525$	$0.3859 \pm 0.0402$	$5771. \pm 456.$
1.5	$2722. \pm 198.$	$0.2999 \pm 0.0265$	$0.3415 \pm 0.0302$	$5249. \pm 383.$
2.0	$3760. \pm 288.$	$0.1997 \pm 0.0178$	$0.3447 \pm 0.0308$	$5213. \pm 400.$
2.5	$4273. \pm 392.$	$0.1306\pm0.0135$	$0.3343 \pm 0.0346$	$5063. \pm 464.$
3.0	$4881. \pm 504.$	$0.0967 \pm 0.0111$	$0.3552 \pm 0.0408$	$5362. \pm 554.$
3.5	$5139. \pm 626.$	$0.0709 \pm 0.0094$	$0.3621 \pm 0.0480$	$5435. \pm 662.$

Table 7: Atomic pair numbers and ionization probability analyzed with  $Q(Q_X < 4, Q_Y < 4)$ .

F	$N_a$	$N_a/N_C$	$P_{ m br}$	$N_a^{\mathrm{total}}$
		No backgr	round.	
0.5	$165. \pm 44.$	$0.5172 \pm 0.1835$	$0.2725 \pm 0.0968$	$4413. \pm 1167.$
1.0	$1117. \pm 99.$	$0.5502 \pm 0.0656$	$0.3591 \pm 0.0429$	$5570. \pm 493.$
1.5	$2409. \pm 166.$	$0.3842 \pm 0.0333$	$0.3475 \pm 0.0302$	$5354. \pm 368.$
2.0	$3374. \pm 241.$	$0.2522 \pm 0.0215$	$0.3298 \pm 0.0281$	$5031. \pm 359.$
2.5	$4289. \pm 323.$	$0.1853 \pm 0.0162$	$0.3523 \pm 0.0308$	$5263. \pm 396.$
3.0	$4709. \pm 414.$	$0.1308 \pm 0.0130$	$0.3542 \pm 0.0352$	$5256. \pm 462.$
3.5	$4842. \pm 512.$	$0.0934 \pm 0.0109$	$0.3514 \pm 0.0410$	$5161. \pm 545.$
4.0	4980. $\pm$ 614.	$0.0705 \pm 0.0095$	$0.3578 \pm 0.0482$	$5189. \pm 640.$
		Backgro	und.	
0.5	$172. \pm 43.$	$0.5536 \pm 0.1878$	$0.2885 \pm 0.0981$	$4658. \pm 1162.$
1.0	$1176. \pm 97.$	$0.5967 \pm 0.0676$	$0.4008 \pm 0.0456$	$6053. \pm 500.$
1.5	$2514. \pm 164.$	$0.4075 \pm 0.0338$	$0.3736 \pm 0.0311$	$5701. \pm 372.$
2.0	$3529. \pm 239.$	$0.2666 \pm 0.0217$	$0.3523 \pm 0.0287$	$5356. \pm 362.$
2.5	$4490. \pm 320.$	$0.1956 \pm 0.0163$	$0.3748 \pm 0.0313$	$5582. \pm 398.$
3.0	$4964. \pm 411.$	$0.1387 \pm 0.0131$	$0.3776 \pm 0.0357$	$5599. \pm 464.$
3.5	$5081. \pm 509.$	$0.0984 \pm 0.0109$	$0.3713 \pm 0.0411$	$5461. \pm 547.$
4.0	$5216. \pm 611.$	$0.0740 \pm 0.0095$	$0.3756 \pm 0.0482$	$5468. \pm 641.$
		Background an	d crosstalk.	
0.5	$192. \pm 41.$	$0.6564 \pm 0.2002$	$0.3616 \pm 0.1106$	$5047. \pm 1088.$
1.0	$1199. \pm 96.$	$0.6153 \pm 0.0682$	$0.4060 \pm 0.0452$	$6032. \pm 485.$
1.5	$2574. \pm 163.$	$0.4216 \pm 0.0341$	$0.3833 \pm 0.0311$	$5738. \pm 363.$
2.0	$3619. \pm 237.$	$0.2755 \pm 0.0218$	$0.3599 \pm 0.0285$	$5424. \pm 356.$
2.5	$4612. \pm 319.$	$0.2020 \pm 0.0164$	$0.3801 \pm 0.0309$	$5688. \pm 393.$
3.0	$5098. \pm 410.$	$0.1431 \pm 0.0131$	$0.3807 \pm 0.0349$	$5725. \pm 460.$
3.5	$5238. \pm 507.$	$0.1018 \pm 0.0110$	$0.3733 \pm 0.0403$	$5615. \pm 544.$
4.0	$5406. \pm 609.$	$0.0769 \pm 0.0095$	$0.3775 \pm 0.0466$	$5657. \pm 638.$

Table 8: Atomic pair numbers and ionization probability analyzed with  $F(Q_X < 4, Q_Y < 4)$ .

 

 Table 9: Atomic pair numbers are found using the signal shape for different background descriptions.

Variable	Cut	Atomic pair number		
	MeV/c	No Background	Background	Background and
				$\operatorname{crosstalk}$
$F \\ Q \\ Q_L$	$Q_{X,Y} < 4$ $Q_T < 4$ $Q_T < 4$	$5023.0 \pm 377.9 4557.3 \pm 405.7 6079.0 \pm 452.1$	$5339.1 \pm 383.4 4929.2 \pm 412.2 6059.9 \pm 452.2$	$5481.2 \pm 383.2 \\ 5030.7 \pm 412.5 \\ 5988.9 \pm 451.5$