# Dependence of breakup probability estimation on $K^{+} K^{-}$and $\mathbf{p} \overline{\mathrm{p}}$ background 

O.E.Gorchakov (JINR, Dubna) and V.V.Yazkov (SINP, Moscow)

January 21, 2005


#### Abstract

Admixture of unidentified $K^{+} K^{-}$and $\mathrm{p} \overline{\mathrm{p}}$ pairs provides essential distortion of "Coulomb" background and leads to an error in a number of "atomic pairs" and in a measured value of breakup probability. The value of admixture and resulting distortion are investigated.


## Introduction

At present DIRAC setup is not able to identify $K^{+} K^{-}$-pairs for any momentum and $\mathrm{p} \overline{\mathrm{p}}$ pairs with lab momentum of particles more than $1.8 \mathrm{GeV} / c$. Protons (antiprotons) with $P_{l} a b<1.8 \mathrm{GeV} / c$ are rejected by cut on the difference of times measured by VH and upstream detectors.

As result data are analyzed in assumption that all hadrons are pions. From Lorentz transformation it is known that in this case transverse components of relative momentum in CMS $Q_{X}, Q_{Y}$ are measured correctly but longitudinal component $Q_{L}$ is underestimated by factor $\approx m_{\pi} / m_{K}\left(m_{\pi} / m_{\mathrm{p}}\right)$.

If pair has $Q_{T}=0$ and $Q_{L} \neq 0$ than Coulomb factor is calculated with small error because of error in $Q\left(Q=Q_{L}\right)$ is compensated by error in a particle mass in Eq. 1:

$$
\begin{equation*}
A_{C}(Q)=\frac{\eta}{1-e^{-\eta}}, \eta=\frac{2 \pi \alpha m}{Q} \tag{1}
\end{equation*}
$$

Here $A_{C}(Q)$ is a Coulomb factor, $\alpha$ is a fine structure constant, m is a particle mass.
But if $Q_{T} \neq 0$ and $Q_{L}=0$ than Coulomb factor is calculated with big error because parameter $\eta$ in Eq. 1 is underestimated by factor $\approx 3.5$ for $K^{+} K^{-}$pairs and $\approx 6.7$ for $\mathrm{p} \overline{\mathrm{p}}$ pairs. Therefore Coulomb factor is underestimated too. This effect is partly compensated by fit procedure which increases a fraction of Coulomb pairs in order to fit more sharp peak of experimental distribution. But in our analysis a distribution of "free" pairs is fitted in the region $2<Q_{L}<15(22) \mathrm{MeV} / c, Q_{T}<4 \mathrm{MeV} / c$. "Atomic pairs" are found in the region $Q_{L}<2 \mathrm{MeV} / c, Q_{T}<4 \mathrm{MeV} / c$ where $Q_{T}$ gives more essential contribution by comparison with a region is used for fit and as result an approximation function has lower value for small $Q$. It leads to overestimation of "atomic" pair number. Number of Coulomb pairs is also overestimated because $K^{+} K^{-}$and $p \bar{p}$ pairs are included to a number of $\pi^{+} \pi^{-}$pairs. The resulting change of breakup probability estimation is investigated in this report.

## 1 Sensitivity of "atomic" pair number and breakup probability to the admixture of $K^{+} K^{-}$and $\mathrm{p} \overline{\mathrm{p}}$ pairs

At the first stage of investigation an approximation function was built in assumption that $1 \%$ or $2 \%$ pairs are $K^{+} K^{-}$or $\mathrm{p} \overline{\mathrm{p}}$. Lab momentum spectra of admixtures was taken to be equal to spectrum of $\pi^{+} \pi^{-}$pairs. Table 1 presents a values of estimated "atomic" pair numbers $N_{a}$ and breakup probabilities for different admixture of non-pion pairs to approximation function. Analysis was done with distribution over $F$. Column $\delta_{P_{b r}}$ contains relative statistical error of a breakup probabilities $P_{b r}$ and column $\Delta P_{b r}$ shows relative change of $P_{b r}$ in comparison with analysis fulfilled in assumption that all hadrons are pions.

Table 1: Atomic pair numbers and breakup probabilities with $F\left(Q_{X}<4, Q_{Y}<4 \mathrm{MeV} / c\right)$ for different assumed admixtures

| $F$ | $K^{+} K^{-}$ <br> $\%$ | $\mathrm{p} \overline{\mathrm{p}}$ <br> $\%$ | $N_{a}$ |  | $P_{b r}$ | $\delta_{P_{b r}}$ <br> $\%$ |
| :---: | ---: | ---: | :--- | :--- | ---: | ---: |
| 1.0 | 0.00 | 0.00 | $1188 . \pm 97$. | $\Delta P_{b r}$ <br> $\%$ |  |  |
| 1.0 | 1.00 | 0.00 | $1179 . \pm 97$. | $0.3975 \pm 0.3938 \pm 0.0446$ | 11.23 | 0.00 |
| 1.0 | 2.00 | 0.00 | $1168 . \pm 97$. | $0.3892 \pm 0.0444$ | 11.32 | -0.94 |
| 1.0 | 0.00 | 1.00 | $1170 . \pm 97$. | $0.3899 \pm 0.0444$ | 11.40 | -1.09 |
|  |  |  |  |  |  |  |
| 2.0 | 0.00 | 0.00 | $3571 . \pm 240$. | $0.3526 \pm 0.0286$ | 8.10 | 0.00 |
| 2.0 | 1.00 | 0.00 | $3507 . \pm 241$. | $0.3457 \pm 0.0285$ | 8.25 | -1.96 |
| 2.0 | 2.00 | 0.00 | $3445 . \pm 241$. | $0.3391 \pm 0.0285$ | 8.40 | -3.81 |
| 2.0 | 0.00 | 1.00 | $3447 . \pm 241$. | $0.3389 \pm 0.0284$ | 8.39 | -3.88 |
|  |  |  |  |  |  |  |
| 2.5 | 0.00 | 0.00 | $4556 . \pm 322$. | $0.3758 \pm 0.0311$ | 8.28 | 0.00 |
| 2.5 | 1.00 | 0.00 | $4450 . \pm 323$. | $0.3667 \pm 0.0311$ | 8.48 | -2.42 |
| 2.5 | 2.00 | 0.00 | $4348 . \pm 324$. | $0.3580 \pm 0.0311$ | 8.68 | -4.75 |
| 2.5 | 0.00 | 1.00 | $4351 . \pm 324$. | $0.3577 \pm 0.0310$ | 8.67 | -4.82 |
|  |  |  |  |  |  |  |
| 3.0 | 0.00 | 0.00 | $5082 . \pm 413$. | $0.3822 \pm 0.0354$ | 9.27 | 0.00 |
| 3.0 | 1.00 | 0.00 | $4920 . \pm 414$. | $0.3699 \pm 0.0354$ | 9.57 | -3.21 |
| 3.0 | 2.00 | 0.00 | $4756 . \pm 416$. | $0.3574 \pm 0.0354$ | 9.90 | -6.50 |
| 3.0 | 0.00 | 1.00 | $4771 . \pm 416$. | $0.3580 \pm 0.0353$ | 9.87 | -6.34 |
|  |  |  |  |  |  |  |
| 4.0 | 0.00 | 0.00 | $5312 . \pm 614$. | $0.3757 \pm 0.0475$ | 12.65 | 0.00 |
| 4.0 | 1.00 | 0.00 | $5014 . \pm 617$. | $0.3549 \pm 0.0475$ | 13.40 | -5.54 |
| 4.0 | 2.00 | 0.00 | $4702 . \pm 621$. | $0.3329 \pm 0.0476$ | 14.29 | -11.40 |
| 4.0 | 0.00 | 1.00 | $4740 . \pm 620$. | $0.3350 \pm 0.0475$ | 14.17 | -10.83 |
|  |  |  |  |  |  |  |

Data were also analyzed with $Q$ and $Q_{L}$. Results are presented in Tables 2, 3, 4 .

It is seen that even small admixtures of $K^{+} K^{-}$and $p \bar{p}$ pairs induce essential change in breakup probability.

## 2 Estimation of $K^{+} K^{-}$and p $\bar{p}$ pair admixture

Fraction of $K^{+} K^{-}$pairs was estimated with simulation. Samples $K^{+} K^{-}$and $\pi^{+} \pi^{-}$pairs were generated by FRITIOF 6.0 and propagated through DIRAC setup with GEANT-DIRAC code. Finally MC data was processed by ARIANE. Criteria $Q_{X}<4 \mathrm{MeV} / c, Q_{Y}<4 \mathrm{MeV} / c$ and $Q_{L}<22 \mathrm{MeV} / c$ (pion mass was assumed) were applied to events. Ratio (in \%) of $K^{+} K^{-}$pair distribution to $\pi^{+} \pi^{-}$pair distribution over total pair momentum $P_{\pi^{+} \pi^{-}}$is shown in Fig. 1a. This ratio growths with momentum. One of the reasons is decay probability of kaons which decreases for high momenta. Figs. 1b,c show ratios of distributions over $Q$ and $Q_{L}$. Coulomb factor for creation of this picture was set to 1 in order to simplify shape of distributions over $Q$ and $Q_{L}$. Small deep near 0 in Fig. 1b occurred due to more hard spectrum of $K^{+} K^{-}$pairs. As result these pairs with small $Q_{T}$ had lower efficiency to be detected due to problems with detection of close pairs by ScFi detector.

Fraction of $\mathrm{p} \overline{\mathrm{p}}$ pairs was estimated from experimental data collected in 2001 with the nickel target. Runs from 3843 to 4301 were used (about $50 \%$ of data). Events were processed by ARIANE in assumption that all hadron were protons or antiprotons. Fig. 2a presents time-offlight of negative particles from upstream detector (2 planes of ScFi and not less than 2 planes of DeDx had signals) to the vertical horoscope. Time expected for antiprotons corresponds to 0 . Program applied criterion on absence of hit in vicinity to selected tracks and cuts on momenta of particles $1.4<P_{h^{-}}<1.5 \mathrm{GeV} / c, 2.2<P_{h^{+}}<3 \mathrm{GeV} / c$. It allows to reject partly background of $\pi^{+} \pi^{-}$pairs using difference of time-of-flight of positive and negative particles from the target to the left and right arms of VH. This difference is practically 0 for pions in contradiction to $p \bar{p}$. Fig. 2b contains the similar distribution for pairs which was rejected by this criterion. It is seen that the last picture has much lower peak in the expected region $\Delta t=0$. The difference of event numbers in regions $[-1,1]$ ns of Figs. 2a,b allows to obtain a number of proton-antiproton pairs. In Figs. 3, 4 similar distribution of events with different momenta of negative particle are shown. Comparing estimated number of $\mathrm{p} \overline{\mathrm{p}}$ with a number of $\pi^{+} \pi^{-}$pairs it is possible to find their ratio $R_{\mathrm{p} \overline{\mathrm{p}}}$ as function of antiproton momentum $P_{\overline{\mathrm{p}}}$ (see Table 5).

In Fig. 5a ratio $R_{\mathrm{p} \overline{\mathrm{p}}}$ is presented for total pair momentum range $3.0<P_{\pi^{+} \pi^{-}}<8.4$. For calculation of this function at the first stage antiproton lab momentum was replaced by total par momentum with Eq. 2.

$$
\begin{equation*}
P_{\pi^{+} \pi^{-}}=2 P_{\overline{\mathrm{p}}}, R_{\mathrm{p} \overline{\mathrm{p}}}\left(P_{\pi^{+} \pi^{-}}>4.2\right)=R_{\mathrm{p} \overline{\mathrm{p}}}(4.2) \tag{2}
\end{equation*}
$$

Hear momentum is in $\mathrm{GeV} / c$. At the second stage this ratio was convoluted with a rejection factor which described suppression of protons and antiprotons by ARIANE at the processing of $\pi^{+} \pi^{-}$pairs. Spectrum of hadron pairs in DIRAC experiment is shown in Fig. 5b.

## 3 Change of "atomic" pair number and breakup probability due to estimated admixture of $K^{+} K^{-}$and $\mathrm{p} \overline{\mathrm{p}}$ pairs

Data collected in 2001 with the nickel target were processed in two way. The first one is analysis with approximation function built with accidentals. Influence of finite size corrections [1] was taken into account. For the second one approximation function was corrected by admixture of $K^{+} K^{-}$and $\mathrm{p} \overline{\mathrm{p}}$ pairs estimated in the previous section. Number of "atomic" pairs $N_{a}$ and probability of breakup $\mathrm{P}_{\mathrm{br}}$ are presented in Tables 6, 7, 8, 9. Columns $\Delta P_{b r}$ contain relative change of $P_{b r}$ in comparison with analysis fulfilled in assumption that there is no admixture.

The same comparison was fulfilled for fit procedure which used a shape of "atomic" pair distribution (other conditions are as in the previous case). Tables 10, 11, 12, 13 contain results.

From these data it is seen that an admixture of $K^{+} K^{-}$and $p \bar{p}$ background changes a number of "atomic" pairs and probability of ionization. This effect is maximal for $Q_{L}$. Probably the reason is lower sensitivity to this specific distortion of distribution shape which most dangerous for small $Q_{L}$. Also effect increases for wider $Q_{T}$ cut because of growth of background which is misidentified as extra "atomic" pairs.

## Conclusions

From above it is possible to make several conclusions:

- Admixture of non-pion pairs should be to take into account during analysis if masses of oppositely charged particles are equal which produces Coulomb peak in the same place as for $\pi^{+} \pi^{-}$pairs.
- Uncertainty in admixture of non-pion pairs induces systematic error. In our case fraction of $K^{+} K^{-}$pairs was obtained with simulation only and was not carefully checked with an experimental data. In this situation it is reasonable to assume that the error equals to the value of effect. Admixture of protons is obtained experimentally but only for one half of $\pi^{+} \pi^{-}$pair statistic. Therefore systematical error is at least $50 \%$. Finally it is possible to suppose that systematic error is $\sim 80 \%$ of breakup probability change due to taking into account of $K^{+} K^{-}$and $\mathrm{p} \overline{\mathrm{p}}$ pair admixture.
- In order to decrease this systematic error it is needed to verify fraction of $K^{+} K^{-}$and $\mathrm{p} \overline{\mathrm{p}}$ pair admixture with an experimental data available in literature or with dedicated measurements in the of DIRAC experiment itself.
[1] R. Lednicky, E-Mail to DIRAC Collaboration on 1 Nov 2005.

Table 2: Atomic pair numbers and breakup probabilities with $Q\left(Q_{T}<4 \mathrm{MeV} / c\right)$ for different assumed admixtures

| $Q$ | $K^{+} K^{-}$ <br> $\%$ | $\mathrm{p} \mathrm{\bar{p}}$ <br> $\%$ | $N_{a}$ |  | $P_{b r}$ | $\delta_{P_{b r}}$ <br> $\%$ |
| ---: | ---: | ---: | :--- | :--- | ---: | ---: |
|  |  |  |  | $\Delta P_{b r}$ <br> $\%$ |  |  |
| 1.0 | 0.00 | 0.00 | $1428 . \pm 122$. | $0.3615 \pm 0.0407$ | 11.26 | 0.00 |
| 1.0 | 1.00 | 0.00 | $1407 . \pm 122$. | $0.3542 \pm 0.0405$ | 11.43 | -2.01 |
| 1.0 | 2.00 | 0.00 | $1382 . \pm 123$. | $0.3459 \pm 0.0402$ | 11.63 | -4.31 |
| 1.0 | 0.00 | 1.00 | $1388 . \pm 123$. | $0.3477 \pm 0.0403$ | 11.58 | -3.82 |
|  |  |  |  |  |  |  |
| 2.0 | 0.00 | 0.00 | $3689 . \pm 322$. | $0.3364 \pm 0.0348$ | 10.35 | 0.00 |
| 2.0 | 1.00 | 0.00 | $3570 . \pm 324$. | $0.3242 \pm 0.0347$ | 10.70 | -3.62 |
| 2.0 | 2.00 | 0.00 | $3449 . \pm 326$. | $0.3118 \pm 0.0345$ | 11.07 | -7.30 |
| 2.0 | 0.00 | 1.00 | $3469 . \pm 325$. | $0.3136 \pm 0.0345$ | 11.01 | -6.78 |
|  |  |  |  |  |  |  |
| 2.5 | 0.00 | 0.00 | $4140 . \pm 454$. | $0.3239 \pm 0.0405$ | 12.51 | 0.00 |
| 2.5 | 1.00 | 0.00 | $3948 . \pm 457$. | $0.3077 \pm 0.0404$ | 13.12 | -4.99 |
| 2.5 | 2.00 | 0.00 | $3753 . \pm 460$. | $0.2915 \pm 0.0402$ | 13.80 | -10.00 |
| 2.5 | 0.00 | 1.00 | $3783 . \pm 459$. | $0.2936 \pm 0.0402$ | 13.70 | -9.34 |
|  |  |  |  |  |  |  |
| 3.0 | 0.00 | 0.00 | $4668 . \pm 601$. | $0.3413 \pm 0.0491$ | 14.40 | 0.00 |
| 3.0 | 1.00 | 0.00 | $4381 . \pm 605$. | $0.3193 \pm 0.0490$ | 15.34 | -6.42 |
| 3.0 | 2.00 | 0.00 | $4089 . \pm 610$. | $0.2970 \pm 0.0488$ | 16.44 | -12.97 |
| 3.0 | 0.00 | 1.00 | $4138 . \pm 609$. | $0.3004 \pm 0.0488$ | 16.24 | -11.96 |
|  |  |  |  |  |  |  |
| 4.0 | 0.00 | 0.00 | $4733 . \pm 934$. | $0.3300 \pm 0.0701$ | 21.23 | 0.00 |
| 4.0 | 1.00 | 0.00 | $4228 . \pm 942$. | $0.2942 \pm 0.0699$ | 23.77 | -10.84 |
| 4.0 | 2.00 | 0.00 | $3703 . \pm 949$. | $0.2570 \pm 0.0698$ | 27.15 | -22.11 |
| 4.0 | 0.00 | 1.00 | $3800 . \pm 948$. | $0.2635 \pm 0.0697$ | 26.45 | -20.15 |
|  |  |  |  |  |  |  |

Table 3: Atomic pair numbers and breakup probabilities with $Q_{L}\left(Q_{T}<4 \mathrm{MeV} / c\right)$ for different assumed admixtures.

| $Q_{L}$ | $K^{+} K^{-}$ <br> $\%$ | $\mathrm{p} \overline{\mathrm{p}}$ <br> $\%$ | $N_{a}$ |  | $P_{b r}$ | $\delta_{P_{b r}}$ <br> $\%$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  |  | $\Delta P_{b r}$ <br> $\%$ |  |  |  |
| 0.5 | 0.00 | 0.00 | $3812 . \pm 286$. | $0.4247 \pm 0.0371$ | 8.74 | 0.00 |
| 0.5 | 1.00 | 0.00 | $3549 . \pm 289$. | $0.3913 \pm 0.0368$ | 9.39 | -7.84 |
| 0.5 | 2.00 | 0.00 | $3290 . \pm 292$. | $0.3593 \pm 0.0364$ | 10.13 | -15.38 |
| 0.5 | 0.00 | 1.00 | $3284 . \pm 292$. | $0.3579 \pm 0.0363$ | 10.15 | -15.73 |
|  |  |  |  |  |  |  |
| 1.0 | 0.00 | 0.00 | $5337 . \pm 448$. | $0.4136 \pm 0.0398$ | 9.63 | 0.00 |
| 1.0 | 1.00 | 0.00 | $4905 . \pm 453$. | $0.3771 \pm 0.0395$ | 10.48 | -8.81 |
| 1.0 | 2.00 | 0.00 | $4465 . \pm 459$. | $0.3405 \pm 0.0392$ | 11.51 | -17.67 |
| 1.0 | 0.00 | 1.00 | $4499 . \pm 458$. | $0.3428 \pm 0.0392$ | 11.42 | -17.12 |
|  |  |  |  |  |  |  |
| 1.5 | 0.00 | 0.00 | $5952 . \pm 577$. | $0.4321 \pm 0.0472$ | 10.94 | 0.00 |
| 1.5 | 1.00 | 0.00 | $5426 . \pm 584$. | $0.3914 \pm 0.0470$ | 12.00 | -9.41 |
| 1.5 | 2.00 | 0.00 | $4892 . \pm 590$. | $0.3506 \pm 0.0467$ | 13.31 | -18.85 |
| 1.5 | 0.00 | 1.00 | $4964 . \pm 589$. | $0.3556 \pm 0.0466$ | 13.11 | -17.70 |
|  |  |  |  |  |  |  |
| 2.0 | 0.00 | 0.00 | $6011 . \pm 685$. | $0.4298 \pm 0.0543$ | 12.64 | 0.00 |
| 2.0 | 1.00 | 0.00 | $5439 . \pm 692$. | $0.3870 \pm 0.0540$ | 13.97 | -9.96 |
| 2.0 | 2.00 | 0.00 | $4860 . \pm 699$. | $0.3441 \pm 0.0538$ | 15.63 | -19.95 |
| 2.0 | 0.00 | 1.00 | $4957 . \pm 698$. | $0.3508 \pm 0.0537$ | 15.32 | -18.39 |
|  |  |  |  |  |  |  |

Table 4: Atomic pair numbers and breakup probabilities with $Q_{L}\left(Q_{T}<3 \mathrm{MeV} / c\right)$ for different assumed admixtures

| $Q_{L}$ | $K^{+} K_{-}^{-}$ <br> $\%$ | $\mathrm{p} \overline{\mathrm{p}}$ <br> $\%$ | $N_{a}$ |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  |  |  |  |  | $\mathrm{P}_{\mathrm{br}}$ | $\delta_{\mathrm{P}_{\mathrm{br}}}$ <br> $\%$ |
| 0.5 | 0.00 | 0.00 | $3822 . \pm 250$. | $\Delta \mathrm{P}_{\mathrm{br}}$ <br> $\%$ |  |  |
| 0.5 | 1.00 | 0.00 | $3644 . \pm 253$. | $0.4507 \pm 0.0369$ | 8.19 | 0.00 |
| 0.5 | 2.00 | 0.00 | $3473 . \pm 256$. | $0.4007 \pm 0.0365$ | 8.59 | -5.71 |
| 0.5 | 0.00 | 1.00 | $3482 . \pm 255$. | $0.4015 \pm 0.0361$ | 9.02 | -11.10 |
|  |  |  |  |  |  |  |
| 1.0 | 0.00 | 0.00 | $5337 . \pm 393$. | $0.4361 \pm 0.0391$ | 8.97 | 0.00 |
| 1.0 | 1.00 | 0.00 | $5046 . \pm 397$. | $0.4086 \pm 0.0388$ | 9.49 | -6.31 |
| 1.0 | 2.00 | 0.00 | $4756 . \pm 402$. | $0.3816 \pm 0.0384$ | 10.07 | -12.50 |
| 1.0 | 0.00 | 1.00 | $4799 . \pm 401$. | $0.3852 \pm 0.0384$ | 9.98 | -11.67 |
|  |  |  |  |  |  |  |
| 1.5 | 0.00 | 0.00 | $5771 . \pm 504$. | $0.4402 \pm 0.0455$ | 10.33 | 0.00 |
| 1.5 | 1.00 | 0.00 | $5427 . \pm 509$. | $0.4110 \pm 0.0452$ | 10.99 | -6.63 |
| 1.5 | 2.00 | 0.00 | $5079 . \pm 515$. | $0.3819 \pm 0.0448$ | 11.74 | -13.24 |
| 1.5 | 0.00 | 1.00 | $5152 . \pm 514$. | $0.3876 \pm 0.0449$ | 11.57 | -11.95 |
|  |  |  |  |  |  |  |
| 2.0 | 0.00 | 0.00 | $5724 . \pm 594$. | $0.4292 \pm 0.0514$ | 11.97 | 0.00 |
| 2.0 | 1.00 | 0.00 | $5360 . \pm 600$. | $0.3997 \pm 0.0511$ | 12.79 | -6.88 |
| 2.0 | 2.00 | 0.00 | $4986 . \pm 606$. | $0.3696 \pm 0.0508$ | 13.75 | -13.89 |
| 2.0 | 0.00 | 1.00 | $5078 . \pm 605$. | $0.3767 \pm 0.0508$ | 13.50 | -12.25 |
|  |  |  |  |  |  |  |

Table 5: Ratio of $\mathrm{p} \overline{\mathrm{p}}$ pair distribution to $\pi^{+} \pi^{-}$pair as function of $P_{\overline{\mathrm{p}}}$

| $P_{\overline{\mathrm{p}}}$ | $R_{\mathrm{p} \overline{\mathrm{p}}}$ <br> $\%$ |
| :---: | :---: |
| $1.4 \div 1.5$ | $0.028 \pm 0.009$ |
| $1.5 \div 1.6$ | $0.069 \pm 0.010$ |
| $1.6 \div 1.7$ | $0.143 \pm 0.011$ |
| $1.7 \div 1.8$ | $0.130 \pm 0.013$ |
| $1.8 \div 1.9$ | $0.195 \pm 0.016$ |
| $1.9 \div 2.0$ | $0.216 \pm 0.020$ |
| $2.0 \div 2.1$ | $0.212 \pm 0.028$ |



Figure 1: Ratio (in \%) of $K^{+} K^{-}$pair distribution to $\pi^{+} \pi^{-}$pair distribution as function of $P_{\pi^{+} \pi^{-}}$(a), $Q$ (b) and $Q_{L}(\mathrm{c})$


Figure 2: Distribution over time-of-flight of negative particles from upstream detector to the vertical horoscope: (a) pairs expected to be p ; (b) accidentals. Time-of-flight of antiprotons corresponds to 0 . Lab momentum of particles is in range $1.4<P_{h^{-}}<1.5 \mathrm{GeV} / c$


Figure 3: Distribution over time-of-flight of negative particles from upstream detector to the vertical horoscope: (a) pairs expected to be $\mathrm{p} \overline{\mathrm{p}}$; (b) accidentals. Time-of-flight of antiprotons corresponds to 0 . Lab momentum of particles is in range $1.5<P_{h^{-}}<1.6 \mathrm{GeV} / c$


Figure 4: Distribution over time-of-flight of negative particles from upstream detector to the vertical horoscope: (a) pairs expected to be $\mathrm{p} \overline{\mathrm{p}}$; (b) accidentals. Time-of-flight of antiprotons corresponds to 0 . Lab momentum of particles is in range $1.5<P_{h^{-}}<1.6 \mathrm{GeV} / c$


Figure 5: (a) Ratio (in \%) of $\mathrm{p} \overline{\mathrm{p}}$ pair distribution to $\pi^{+} \pi^{-}$pair distribution as function of $P_{\pi^{+} \pi^{-}}$. (b) Distribution of $\pi^{+} \pi^{-}$pairs over $P_{\pi^{+} \pi^{-}}$

Table 6: Atomic pair numbers and breakup probabilities with $F$ ( $Q_{X}<4, Q_{Y}<4 \mathrm{MeV} / c$ ) with and without assuming of admixtures of $K^{+} K^{-}$and $p \bar{p}$

| $F$ | $K^{+} K^{-}$ <br> and $\bar{p} \overline{\mathrm{p}}$ | $N_{a}$ |  | $\mathrm{P}_{\mathrm{br}}$ |
| ---: | ---: | ---: | ---: | ---: |
| 1.0 | No | $1178 . \pm 97$. | $\Delta_{\mathrm{P}_{\mathrm{br}}}$ <br> $\%$ |  |
| 1.0 | Yes | $1172 . \pm 97$. | $0.3906 \pm 0.3959 \pm 0.0450$ | 0.0 |
| 2.0 | No | $3516 . \pm 241$. | $0.3434 \pm 0.0283$ | 0.0 |
| 2.0 | Yes | $3487 . \pm 241$. | $0.3468 \pm 0.0288$ | 1.0 |
|  |  |  |  |  |
| 2.5 | No | $4471 . \pm 323$. | $0.3651 \pm 0.0308$ | 0.0 |
| 2.5 | Yes | $4418 . \pm 323$. | $0.3674 \pm 0.0314$ | 0.6 |
| 3.0 | No | $4965 . \pm 414$. | $0.3704 \pm 0.0351$ | 0.0 |
| 3.0 | Yes | $4875 . \pm 415$. | $0.3704 \pm 0.0358$ | 0.0 |
| 4.0 | No | $5142 . \pm 616$. | $0.3609 \pm 0.0472$ | 0.0 |
| 4.0 | Yes | $4929 . \pm 618$. | $0.3524 \pm 0.0480$ | -2.4 |

Table 7: Atomic pair numbers and breakup probabilities with $Q\left(Q_{T}<4 \mathrm{MeV} / c\right)$ with and without assuming of admixtures of $K^{+} K^{-}$and $p \bar{p}$

| $Q$ | $K^{+} K^{-}$ <br> and $\overline{\mathrm{p}}$ | $N_{a}$ | $\mathrm{P}_{\mathrm{br}}$ | $\Delta_{\mathrm{P}_{\mathrm{br}}}$ <br> $\%$ |
| ---: | ---: | ---: | ---: | ---: |
| 1.0 | No | $1411 . \pm 122$. | $0.3527 \pm 0.0402$ | 0.0 |
| 1.0 | Yes | $1395 . \pm 122$. | $0.3533 \pm 0.0407$ | 0.2 |
| 2.0 | No | $3603 . \pm 323$. | $0.3249 \pm 0.0344$ | 0.0 |
| 2.0 | Yes | $3526 . \pm 324$. | $0.3221 \pm 0.0349$ | -0.9 |
| 2.5 | No | $4010 . \pm 456$. | $0.3105 \pm 0.0401$ | 0.0 |
| 2.5 | Yes | $3878 . \pm 458$. | $0.3043 \pm 0.0407$ | -2.0 |
| 3.0 | No | $4494 . \pm 604$. | $0.3257 \pm 0.0487$ | 0.0 |
| 3.0 | Yes | $4290 . \pm 607$. | $0.3151 \pm 0.0494$ | -3.3 |
| 4.0 | No | $4488 . \pm 938$. | $0.3104 \pm 0.0695$ | 0.0 |
| 4.0 | Yes | $4073 . \pm 944$. | $0.2855 \pm 0.0704$ | -8.0 |
|  |  |  |  |  |

Table 8: Atomic pair numbers and breakup probabilities with $Q_{L}\left(Q_{T}<4 \mathrm{MeV} / c\right)$ with and without assuming of admixtures of $K^{+} K^{-}$and $\mathrm{p} \overline{\mathrm{p}}$

| $Q_{L}$ | $K^{+} K^{-}$ <br> and p $\bar{p}$ | $N_{a}$ | $\mathrm{P}_{\mathrm{br}}$ | $\Delta_{\mathrm{P}_{\mathrm{br}}}$ <br> $\%$ |
| ---: | ---: | ---: | ---: | ---: |
| 0.5 | No | $3756 . \pm 286$. | $0.4155 \pm 0.0369$ | 0.0 |
| 0.5 | Yes | $3492 . \pm 290$. | $0.3908 \pm 0.0373$ | -5.9 |
| 1.0 | No | $5233 . \pm 449$. | $0.4025 \pm 0.0395$ | 0.0 |
| 1.0 | Yes | $4799 . \pm 454$. | $0.3734 \pm 0.0400$ | -7.2 |
| 1.5 | No | $5813 . \pm 579$. | $0.4189 \pm 0.0469$ | 0.0 |
| 1.5 | Yes | $5301 . \pm 585$. | $0.3865 \pm 0.0475$ | -7.7 |
| 2.0 | No | $5848 . \pm 687$. | $0.4151 \pm 0.0539$ | 0.0 |
| 2.0 | Yes | $5306 . \pm 694$. | $0.3809 \pm 0.0545$ | -8.2 |

Table 9: Atomic pair numbers and breakup probabilities with $Q_{L}\left(Q_{T}<3 \mathrm{MeV} / c\right)$ with and without assuming of admixtures of $K^{+} K^{-}$and $p \bar{p}$

| $Q_{L}$ | $K^{+} K^{-}$ <br> and p $\bar{p}$ | $N_{a}$ | $\mathrm{P}_{\mathrm{br}}$ | $\Delta_{\mathrm{P}_{\mathrm{br}}}$ <br> $\%$ |
| ---: | ---: | ---: | ---: | ---: |
| 0.5 | No | $3781 . \pm 251$. | $0.4424 \pm 0.0367$ | 0.0 |
| 0.5 | Yes | $3613 . \pm 253$. | $0.4271 \pm 0.0370$ | -3.5 |
| 1.0 | No | $5261 . \pm 394$. | $0.4266 \pm 0.0388$ | 0.0 |
| 1.0 | Yes | $4993 . \pm 398$. | $0.4090 \pm 0.0392$ | -4.1 |
| 1.5 | No | $5669 . \pm 505$. | $0.4295 \pm 0.0452$ | 0.0 |
| 1.5 | Yes | $5362 . \pm 510$. | $0.4104 \pm 0.0456$ | -4.5 |
| 2.0 | No | $5607 . \pm 596$. | $0.4175 \pm 0.0510$ | 0.0 |
| 2.0 | Yes | $5286 . \pm 601$. | $0.3976 \pm 0.0516$ | -4.8 |

Table 10: Atomic pair numbers and breakup probabilities with $F\left(Q_{X}<4, Q_{Y}<4 \mathrm{MeV} / c\right)$ with and without assuming of admixtures of $K^{+} K^{-}$and $\mathrm{p} \overline{\mathrm{p}}$. Shape of "atomic" pair was used in fit

| $F$ | $K^{+} K^{-}$ <br> and $\overline{\mathrm{p}}$ | $N_{a}$ | $\mathrm{P}_{\mathrm{br}}$ | $\Delta_{\mathrm{P}_{\mathrm{br}}}$ <br> $\%$ |
| :---: | ---: | ---: | ---: | ---: |
| 1.0 | No | $1084 . \pm 87$. | $0.3605 \pm 0.0276$ | 0.00 |
| 1.0 | Yes | $1079 . \pm 87$. | $0.3598 \pm 0.0277$ | -0.19 |
| 2.0 | No | $3682 . \pm 269$. | $0.3605 \pm 0.0277$ | 0.00 |
| 2.0 | Yes | $3664 . \pm 269$. | $0.3602 \pm 0.0278$ | -0.06 |
| 2.5 |  | No | $4449 . \pm 323$. | $0.3643 \pm 0.0280$ |
| 2.5 | Yes | $4428 . \pm 323$. | $0.3641 \pm 0.0281$ | -0.00 |
|  |  |  |  |  |
| 3.0 | No | $4882 . \pm 354$. | $0.3652 \pm 0.0281$ | 0.00 |
| 3.0 | Yes | $4860 . \pm 354$. | $0.3652 \pm 0.0282$ | -0.01 |
| 4.0 |  | No | $5223 . \pm 378$. | $0.3676 \pm 0.0283$ |
| 4.0 | Yes | $5199 . \pm 378$. | $0.3677 \pm 0.0284$ | 0.00 |
|  |  |  |  |  |

Table 11: Atomic pair numbers and breakup probabilities with $Q\left(Q_{T}<4 \mathrm{MeV} / c\right)$ with and without assuming of admixtures of $K^{+} K^{-}$and $\mathrm{p} \overline{\mathrm{p}}$. Shape of "atomic" pair was used in fit

| $Q$ | $\begin{aligned} & K^{+} K^{-} \\ & \text {and } \mathrm{p} \overline{\mathrm{p}} \\ & \hline \end{aligned}$ | $N_{a}$ | $\mathrm{P}_{\text {br }}$ | $\begin{array}{r} \Delta_{\mathrm{P}_{\mathrm{br}}} \\ \% \end{array}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1.0 | No | 1317. $\pm 116$. | $0.3315 \pm 0.0295$ | 0.00 |
| 1.0 | Yes | 1312. $\pm 116$. | $0.3308 \pm 0.0296$ | -0.20 |
| 2.0 | No | 3693. $\pm 311$. | $0.3353 \pm 0.0299$ | 0.00 |
| 2.0 | Yes | 3678. $\pm 311$. | $0.3352 \pm 0.0300$ | -0.02 |
| 2.5 | No | 4314. $\pm 362$. | $0.3363 \pm 0.0300$ | 0.00 |
| 2.5 | Yes | 4296. $\pm 362$. | $0.3363 \pm 0.0301$ | 0.02 |
| 3.0 | No | 4643. $\pm 389$. | $0.3388 \pm 0.0302$ | 0.00 |
| 3.0 | Yes | 4624. $\pm 389$. | $0.3389 \pm 0.0304$ | 0.04 |
| 4.0 | No | 4902. $\pm 410$. | $0.3412 \pm 0.0305$ | 0.00 |
| 4.0 | Yes | 4882. $\pm 410$. | $0.3415 \pm 0.0306$ | 0.08 |

Table 12: Atomic pair numbers and breakup probabilities with $Q_{L}\left(Q_{T}<4 \mathrm{MeV} / c\right)$ with and without assuming of admixtures of $K^{+} K^{-}$and $\mathrm{p} \overline{\mathrm{p}}$. Shape of "atomic" pair was used in fit

| $Q_{L}$ | $K^{+} K^{-}$ <br> and p$\overline{\mathrm{p}}$ | $N_{a}$ | $\mathrm{P}_{\mathrm{br}}$ | $\Delta_{\mathrm{P}_{\mathrm{br}}}$ <br> $\%$ |
| ---: | ---: | ---: | ---: | ---: |
| 0.5 | No | $3713 . \pm 288$. | $0.4106 \pm 0.0346$ | 0.00 |
| 0.5 | Yes | $3450 . \pm 289$. | $0.3785 \pm 0.0343$ | -7.81 |
| 1.0 | No | $5319 . \pm 412$. | $0.4090 \pm 0.0345$ | 0.00 |
| 1.0 | Yes | $4943 . \pm 414$. | $0.3778 \pm 0.0343$ | -7.63 |
| 1.5 | No | $5694 . \pm 441$. | $0.4103 \pm 0.0346$ | 0.00 |
| 1.5 | Yes | $5292 . \pm 443$. | $0.3798 \pm 0.0345$ | -7.45 |
| 2.0 | No | $5780 . \pm 447$. | $0.4102 \pm 0.0346$ | 0.00 |
| 2.0 | Yes | $5372 . \pm 450$. | $0.3802 \pm 0.0345$ | -7.30 |

Table 13: Atomic pair numbers and breakup probabilities with $Q_{L}\left(Q_{T}<3 \mathrm{MeV} / c\right)$ with and without assuming of admixtures of $K^{+} K^{-}$and $\mathrm{p} \overline{\mathrm{p}}$. Shape of "atomic" pair was used in fit

| $Q_{L}$ | $K^{+} K^{-}$ <br> and pp | $N_{a}$ | $\mathrm{P}_{\mathrm{br}}$ | $\Delta_{\mathrm{P}_{\mathrm{br}}}$ <br> $\%$ |
| ---: | ---: | ---: | ---: | ---: |
| 0.5 | No | $3801 . \pm 260$. | $0.4487 \pm 0.0345$ | 0.00 |
| 0.5 | Yes | $3634 . \pm 262$. | $0.4251 \pm 0.0342$ | -5.27 |
| 1.0 | No | $5455 . \pm 372$. | $0.4462 \pm 0.0343$ | 0.00 |
| 1.0 | Yes | $5215 . \pm 374$. | $0.4236 \pm 0.0341$ | -5.06 |
|  |  |  |  |  |
| 1.5 | No | $5843 . \pm 398$. | $0.4465 \pm 0.0344$ | 0.00 |
| 1.5 | Yes | $5586 . \pm 400$. | $0.4247 \pm 0.0342$ | -4.88 |
| 2.0 | No | $5932 . \pm 404$. | $0.4456 \pm 0.0343$ | 0.00 |
| 2.0 | Yes | $5672 . \pm 406$. | $0.4245 \pm 0.0342$ | -4.74 |

