

Pionium Lifetime in DIRAC

Analysis of the 2001, 2002 and 2003 data

What is new in this method?

GEM/MSGC built at the Santiago de Compostela University

Spatial resolution $\sim 50\mu\text{m}$

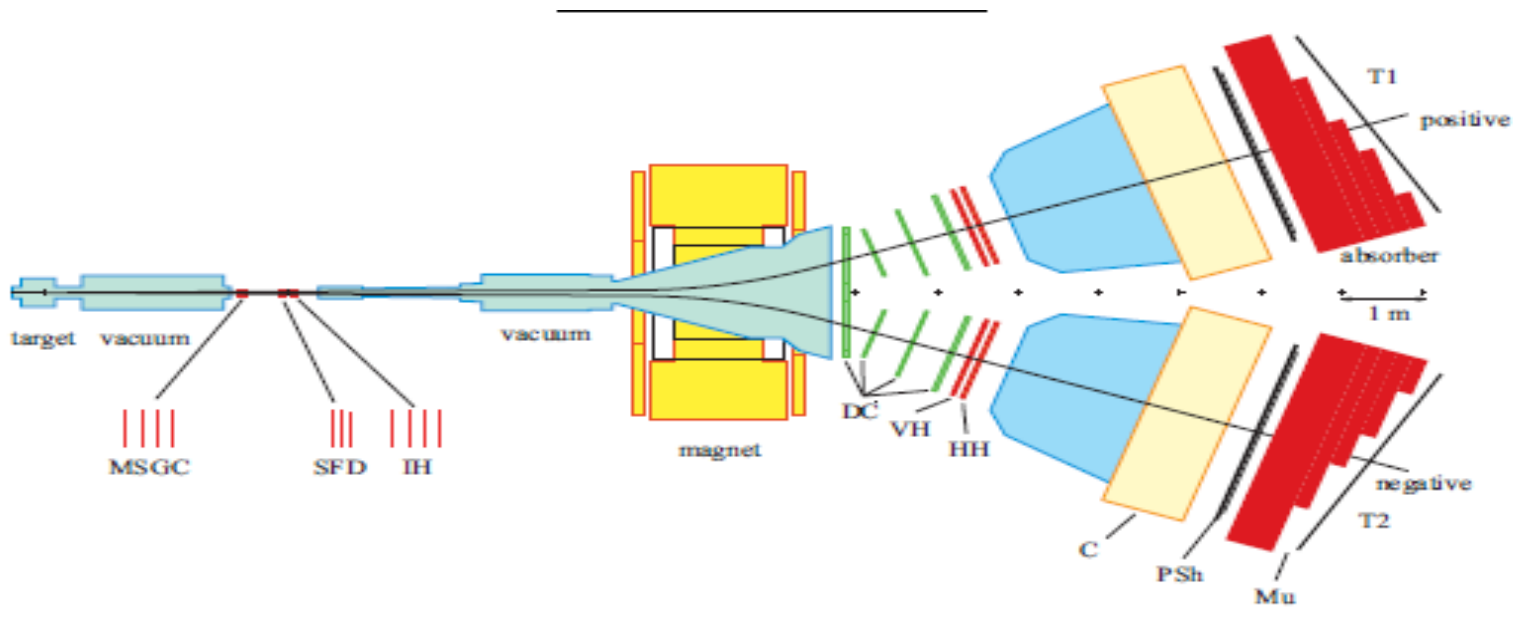
QT resolution $\sim 0.1\text{MeV}/c$ (in QL is $0.55\text{MeV}/c$)

Systematics due to upstream multiple scattering reduced to almost zero.

20 and 24 GeV/c proton beams at PS accelerator.

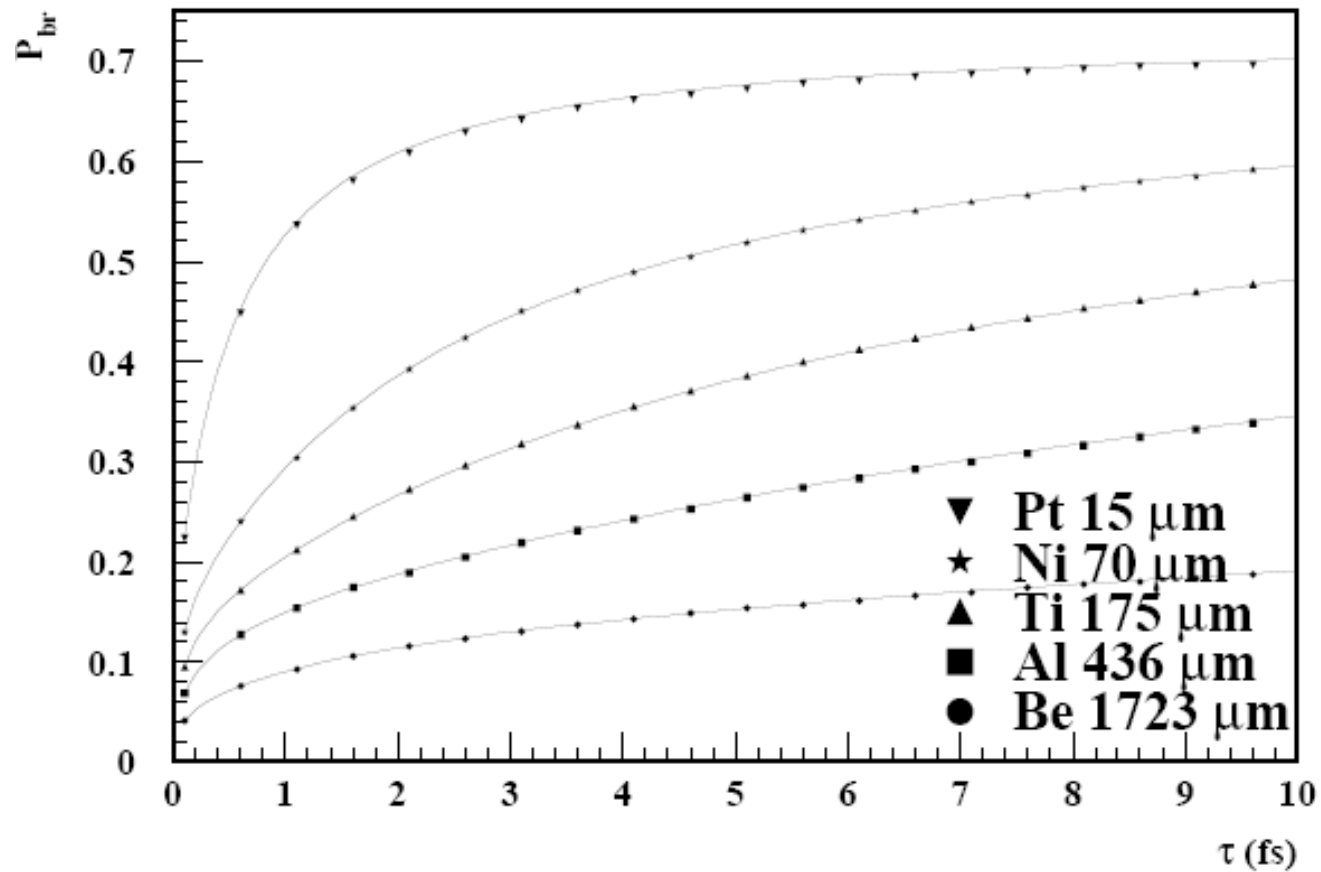
94 and 98 μm Ni targets

22200 pion pairs from ponium ionization



Breakup probability versus pionium lifetime

The relation between the P_{br} and the lifetime is known with a precision better than a 1%



Breakup probability

$$P_{Br} = \frac{n_A}{N_A} = \frac{1}{K^{th}} \frac{n_A}{N_C} \quad P_{Br} = \frac{N_{AT}(\Omega)}{N_{CC}(\Omega)} \frac{1}{K^{exp}(\Omega)} \quad K^{exp} = \frac{\epsilon_{CC}(\Omega)}{\epsilon_{AT}(\Omega)} K^{th}(\Omega)$$

QM analytical factor :

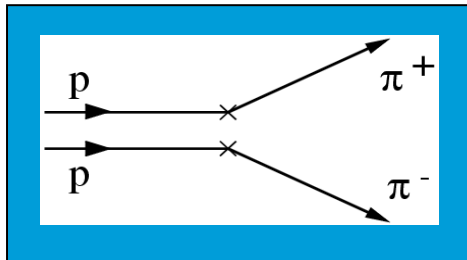
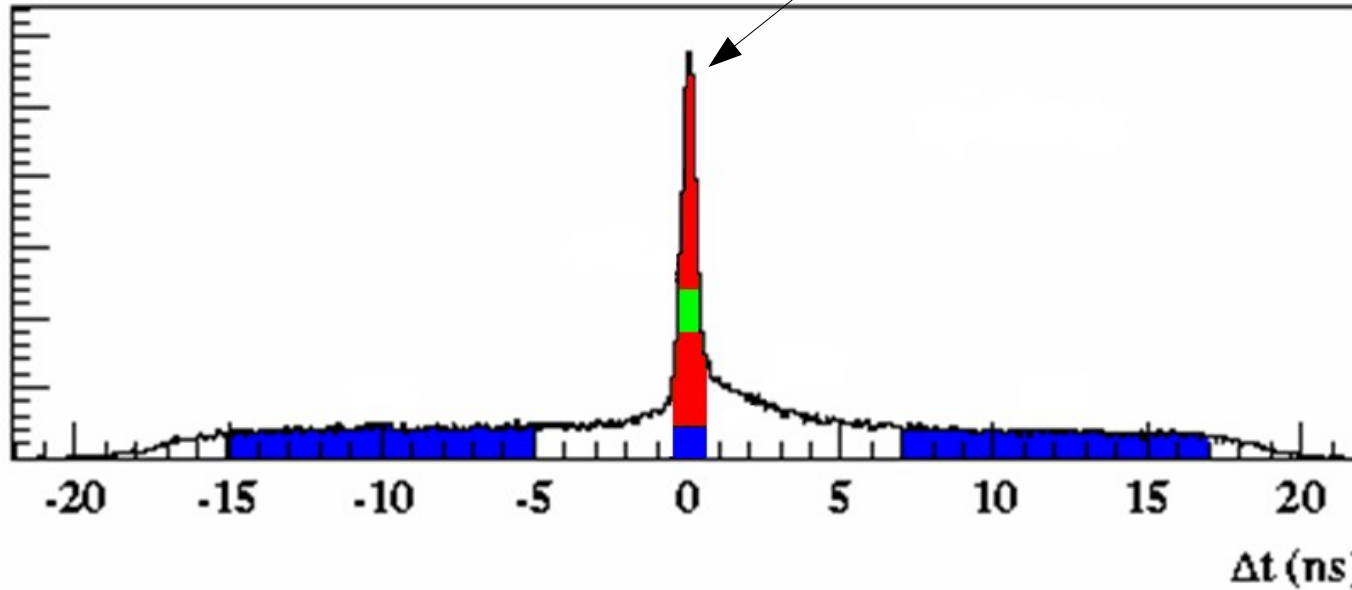
$$K^{th}(\Omega) = \frac{(2\pi\alpha M_\pi)^3}{\pi} \frac{\sum 1/n^3}{\int_\Omega A_C(Q) d^2Q}$$

· Acceptance factors $\epsilon_{i,j}$ determined by our Monte Carlo method.

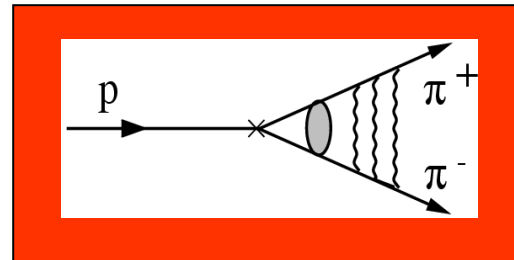
· Standard choice for $\Omega = (0, Q_T^C) \times (0, Q_L^C)$
is $Q_{Tc}=2$ MeV/c and $Q_{Tc}=5$ MeV/c.

Difference of TOF in the VH

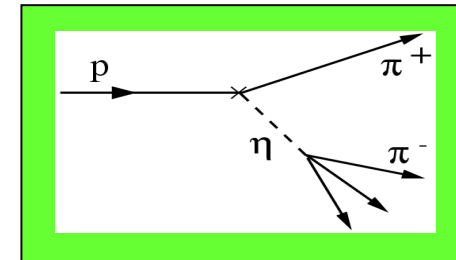
Prompt events =
 $\Delta t < 0.5$ ns
 (13% accidentals contamination)



Accidental pairs,
 different proton interactions in the target.



Coulomb pairs.
 From short lived sources.
 $r < 3$ fm, $< R(A^{2/3})$

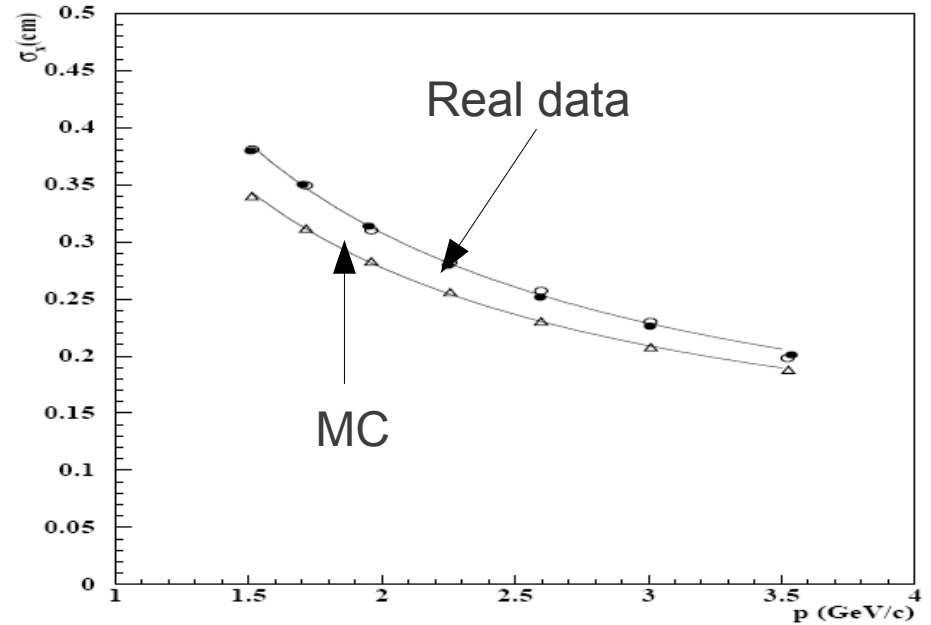
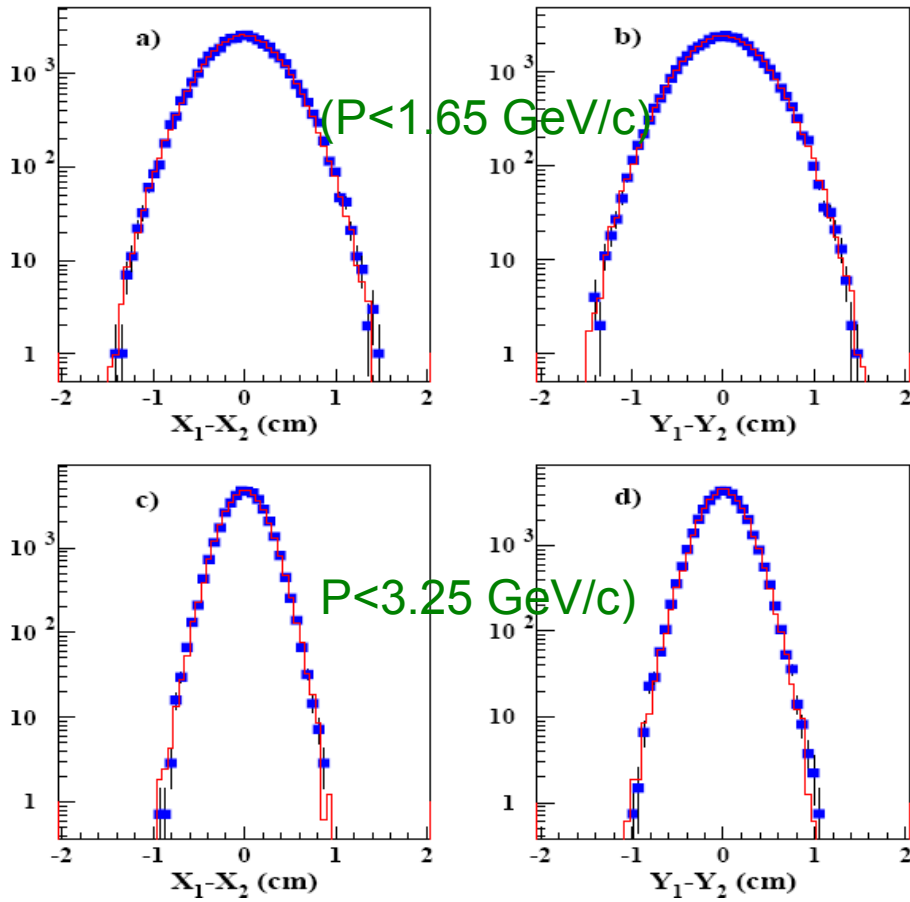
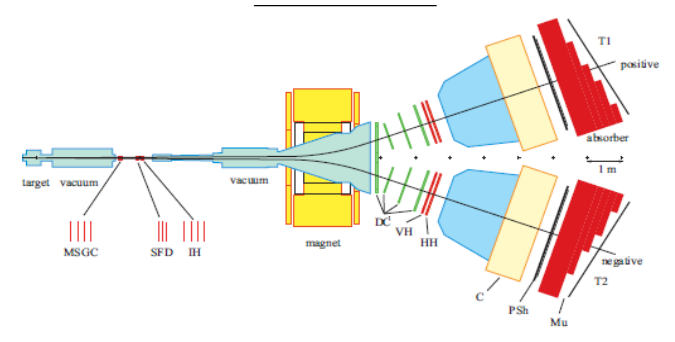


Non Coulomb pairs.
 From long lived sources.
 $r \sim 1000$ fm.

Monte Carlo

<u>Sample</u>	<u>Coulomb</u>	<u>Non Coulomb</u>	<u>Atomic pairs</u>
2001 94um	200,000,000	50,000,000	10,000,000
2001 98um	50,000,000	15,000,000	10,000,000
2002 20GeV/c	110,000,000	30,000,000	10,000,000
2002 24GeV/c	160,000,000	45,000,000	10,000,000
2003 20GeV/c	50,000,000	15,000,000	10,000,000
Total	570,000,000	155,000,000	50,000,000

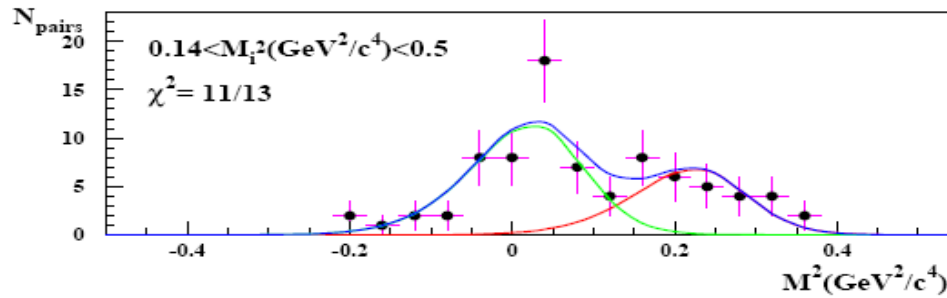
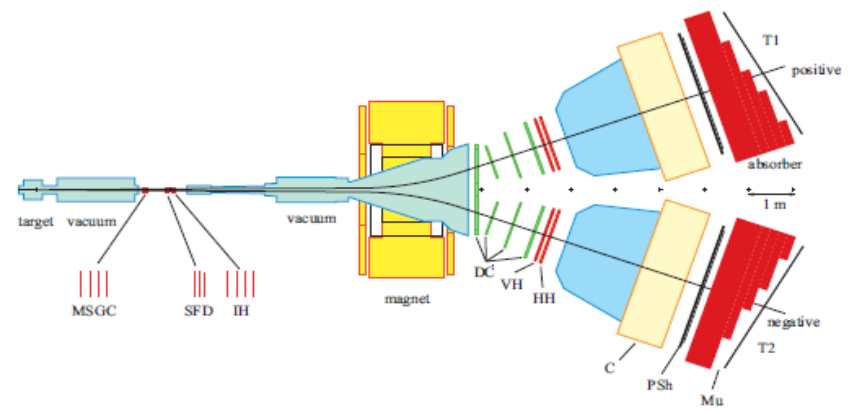
Upstream multiple scattering



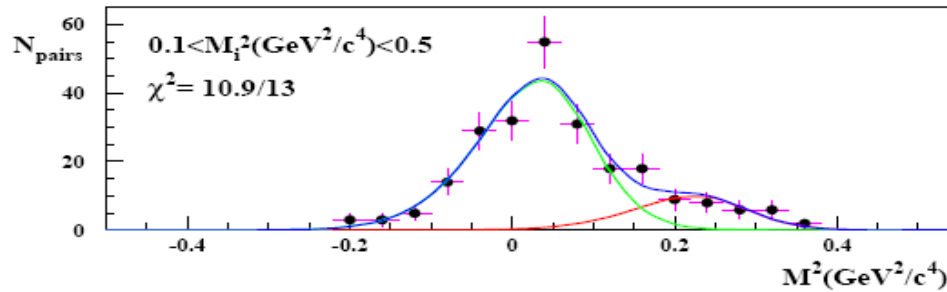
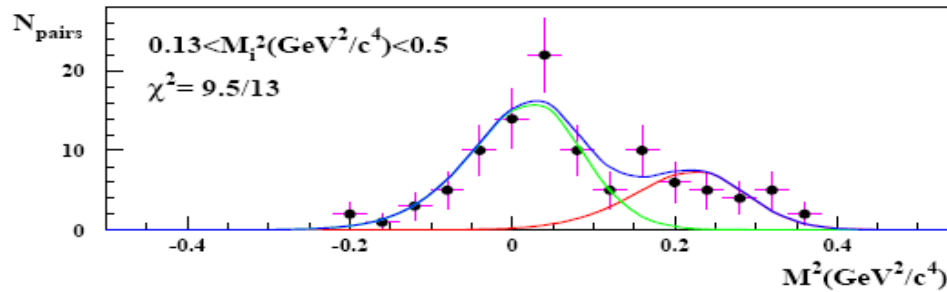
Systematic error in Pbr \rightarrow 0.04 %

Necessary to increase upstream multiple scattering in a 15% !! (1.5% of precision)

KK contamination

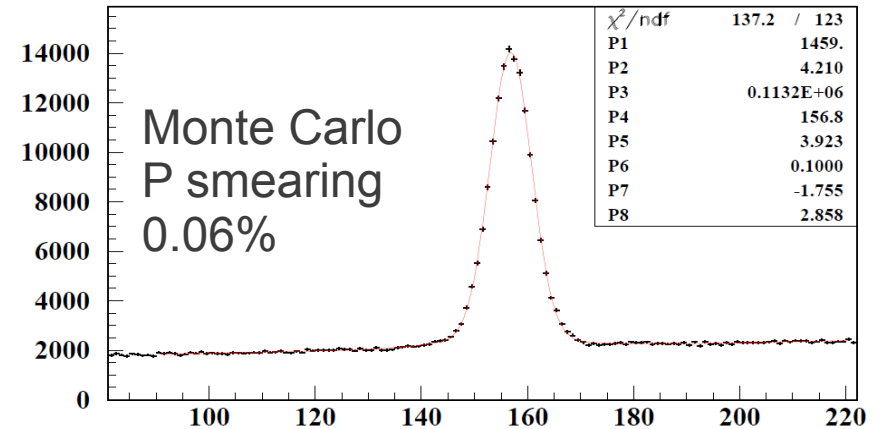
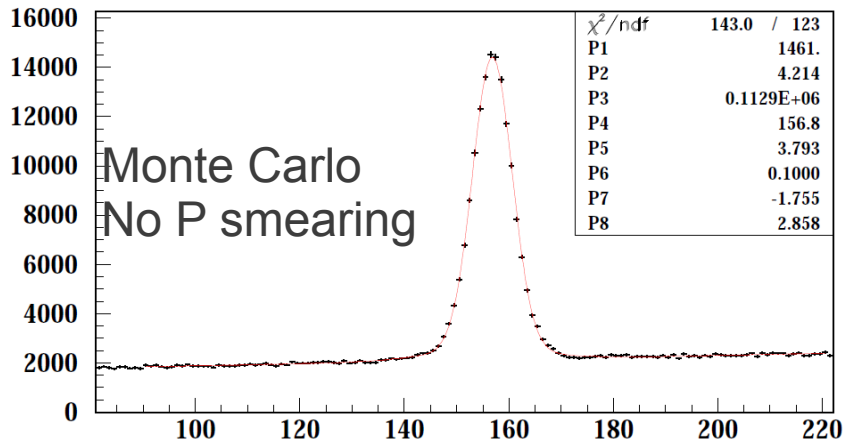
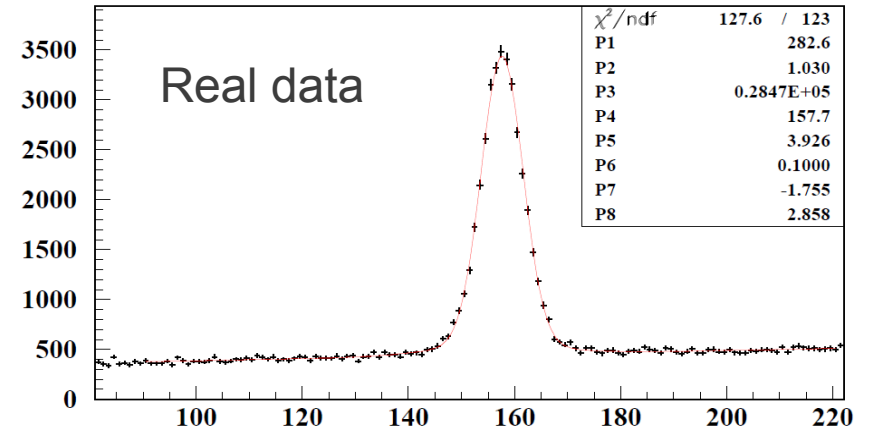
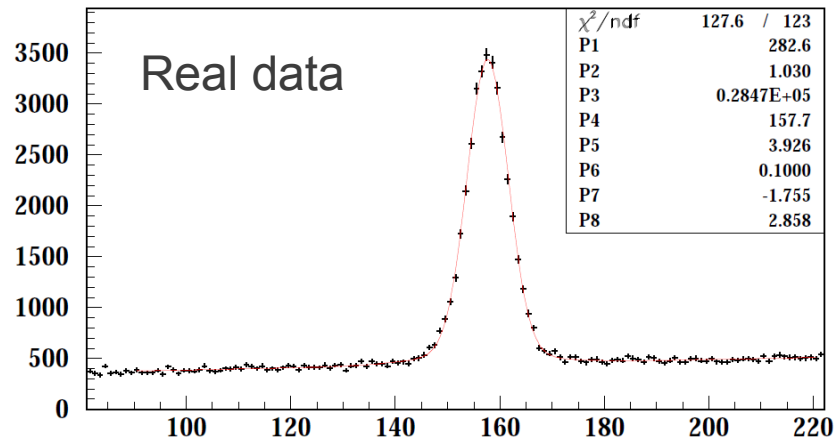


KK/pipi at 2.9 GeV/c \rightarrow 0.238 \pm 0.035 %



Systematic error in Pbr \rightarrow 0.24 %

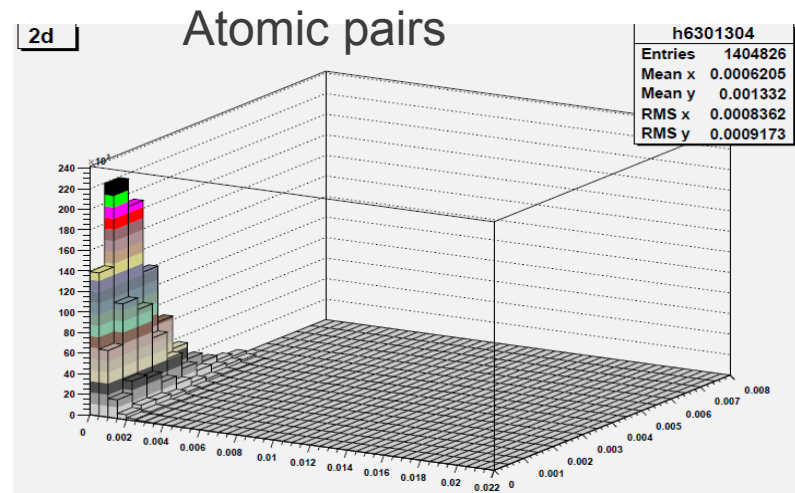
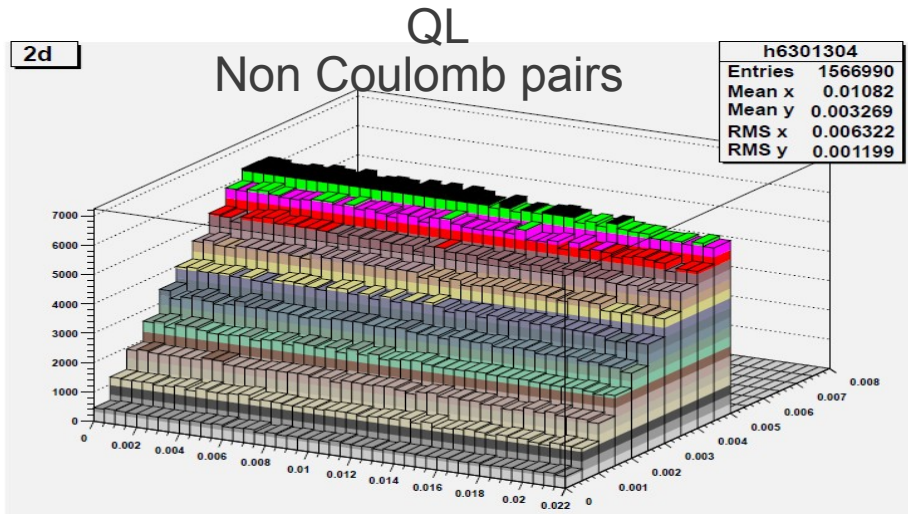
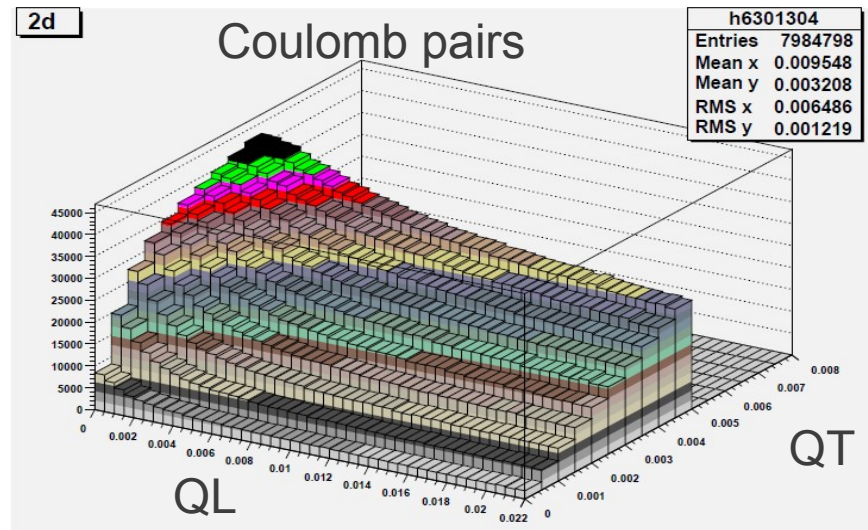
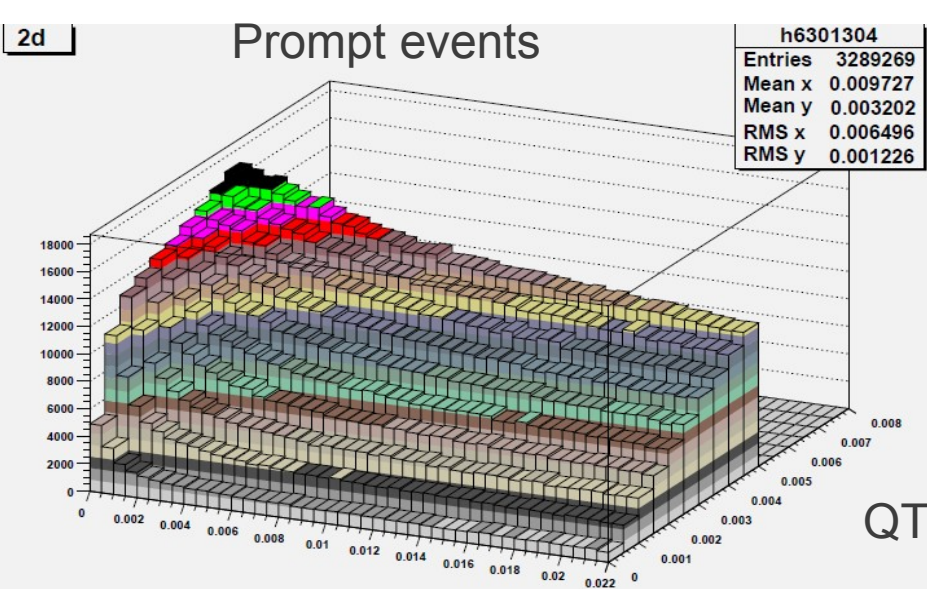
Momentum resolution. Lambda analysis



Systematic error in Pbr \rightarrow 0.6 %

Method

$$\chi^2 = \sum_k \frac{\left(N_p^k - \beta \left(\alpha_1 \left[\epsilon \frac{N_{KK}^k}{N_{KK}} + (1 - \epsilon) \frac{N_{CC}^k}{N_{CC}} \right] - \alpha_2 \frac{N_{AC}^k}{N_{AC}} - \alpha_3 \frac{N_{NC}^k}{N_{NC}} - \gamma \frac{N_{AA}^k}{N_{AA}} \right) \right)^2}{N_p^k + \beta^2 \left(\alpha_1^2 \left[(1 - \epsilon)^2 \frac{N_{CC}^k}{N_{CC}^2} + \epsilon^2 \frac{N_{KK}^k}{N_{KK}^2} \right] + \alpha_2^2 \frac{N_{AC}^k}{N_{AC}^2} + \alpha_3^2 \frac{N_{NC}^k}{N_{NC}^2} + \gamma^2 \frac{N_{AA}^k}{N_{AA}^2} \right)}$$



22200 atomic pairs

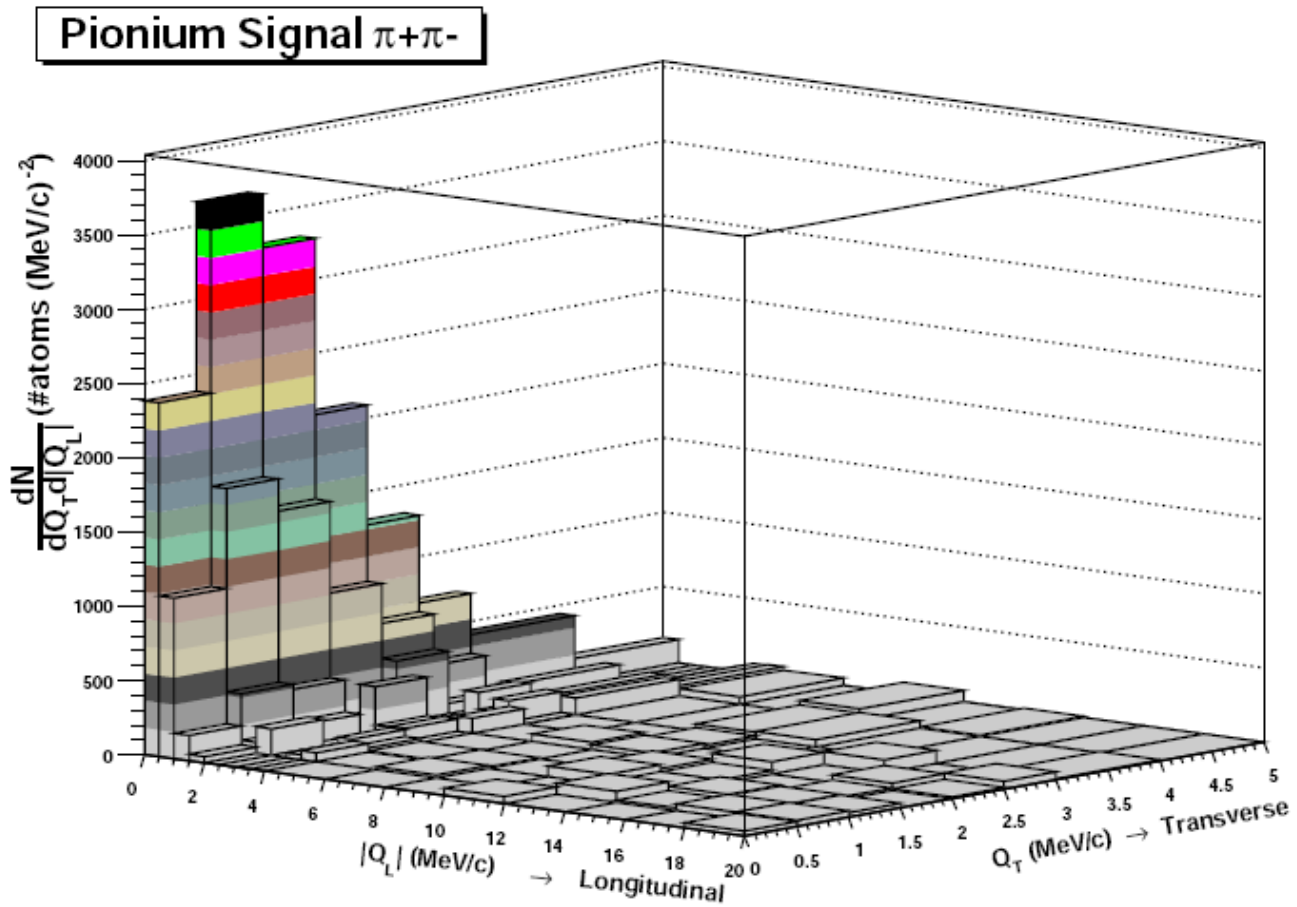
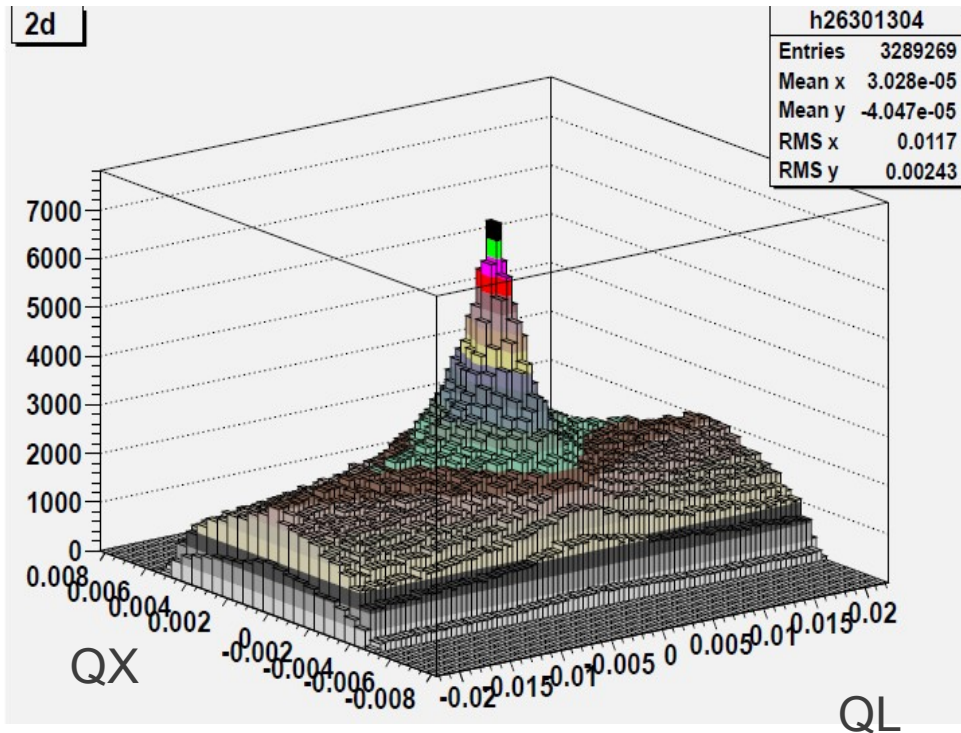


Figure 7.8: Lego plot showing the pionium break-up spectrum in Ni in the $(Q_T, Q_L = |Q_Z|)$ plane, after subtraction of the Coulomb background.

QL vs QX

Prompt real data



Atomic pairs signal

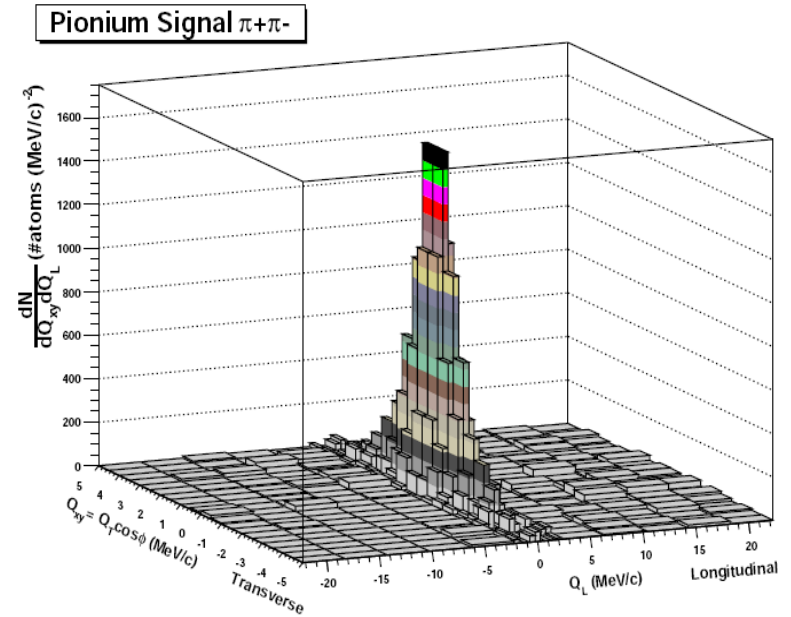
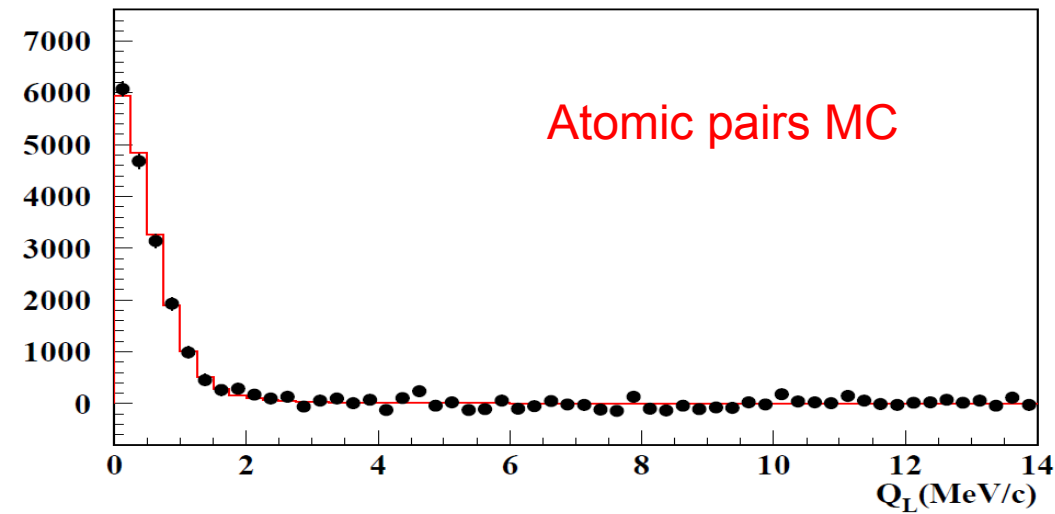
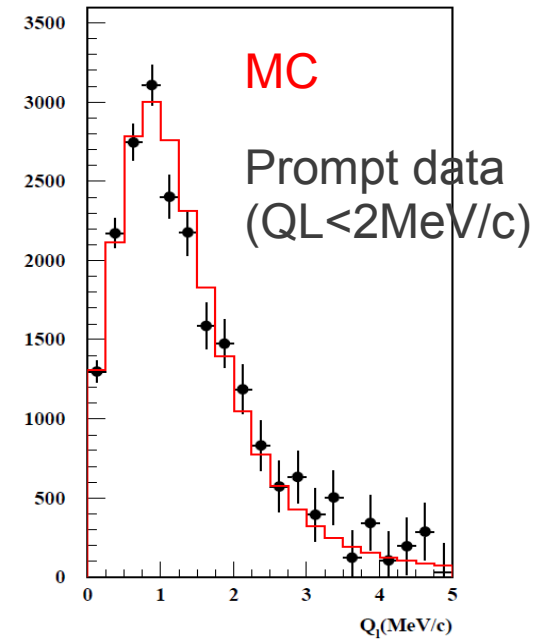
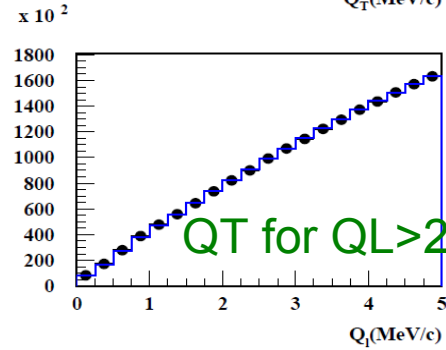
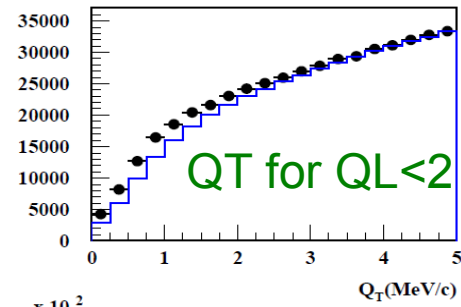
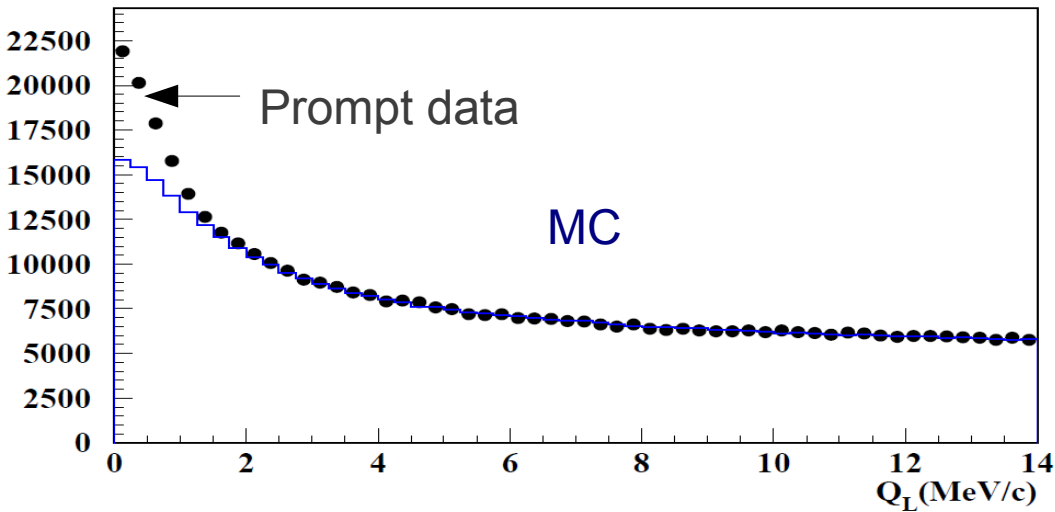


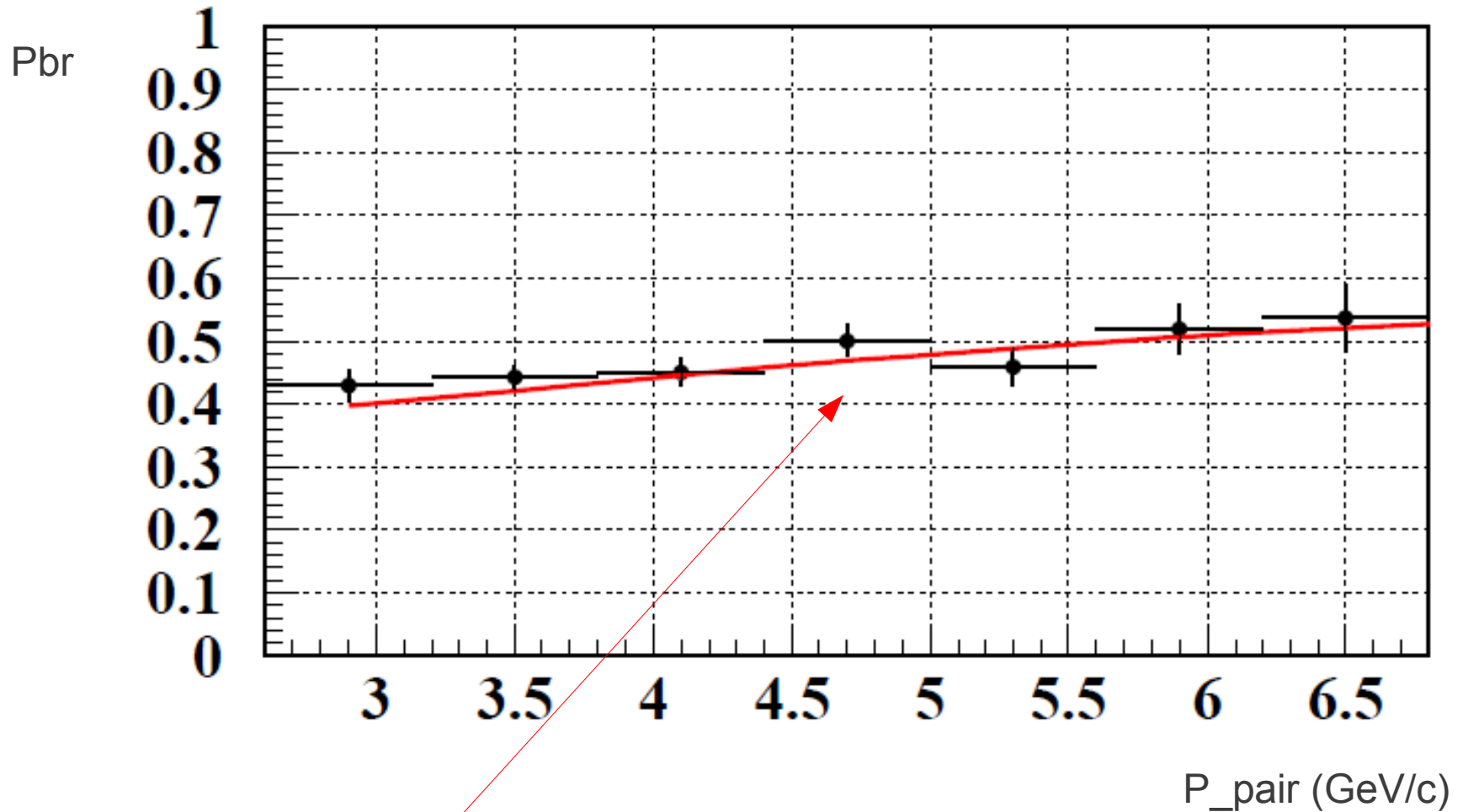
Figure 7.9: Lego plot showing the pionium break-up spectrum in Ni in the (Q_{xy}, Q_L) plane, after subtraction of Coulomb background. The transverse component $Q_{xy} = Q_T \cos\phi$ is defined as the product of the measured Q_T value times the cosine of a random azimuth.

Projections

QL for QT<2MeV/c

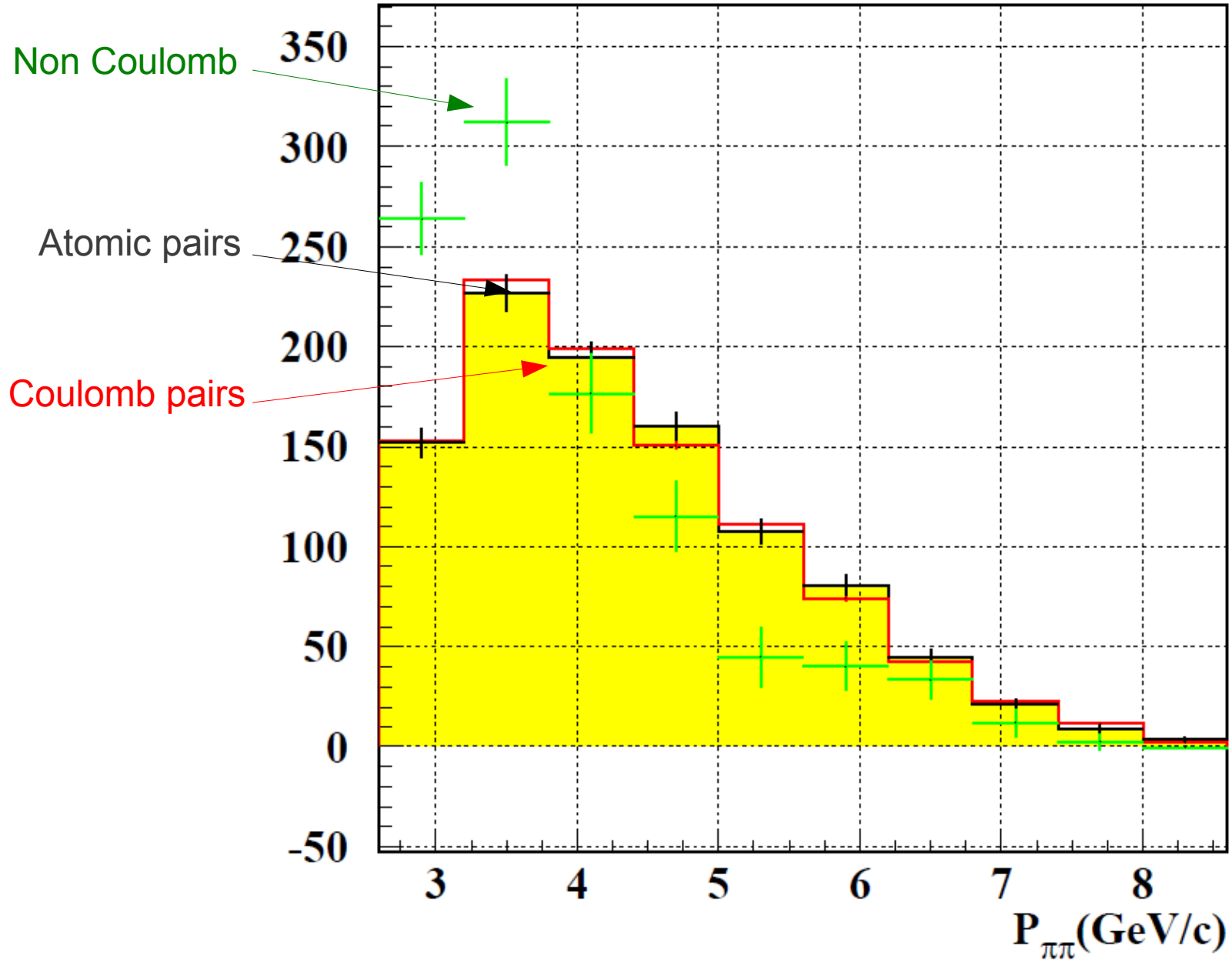


Fit results: Breakup probability versus laboratory momentum

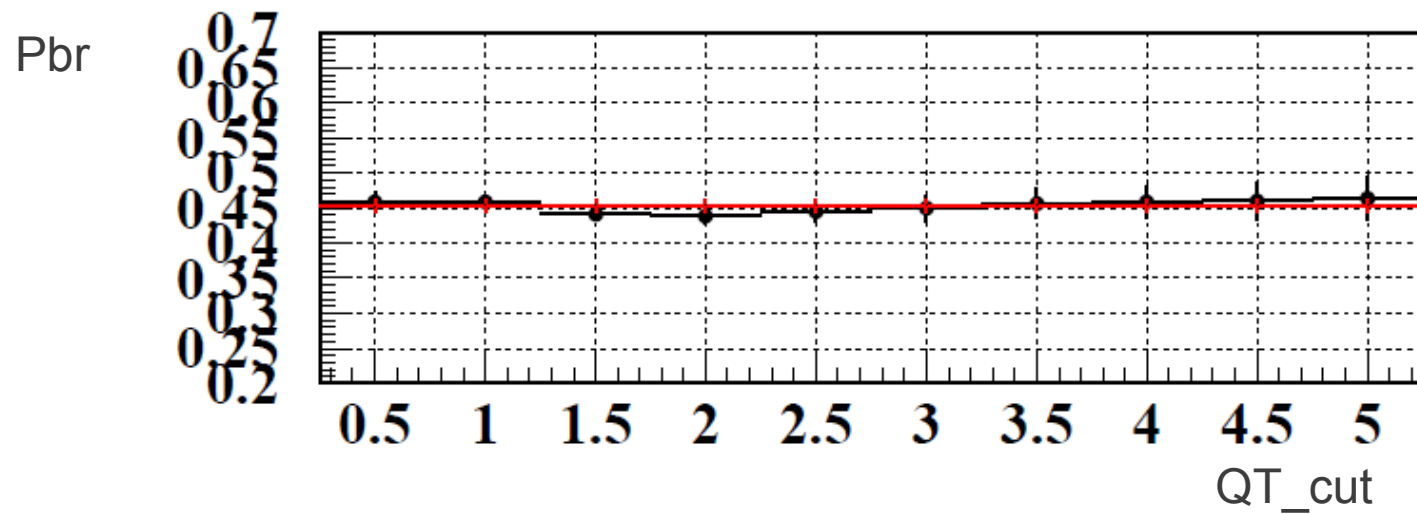
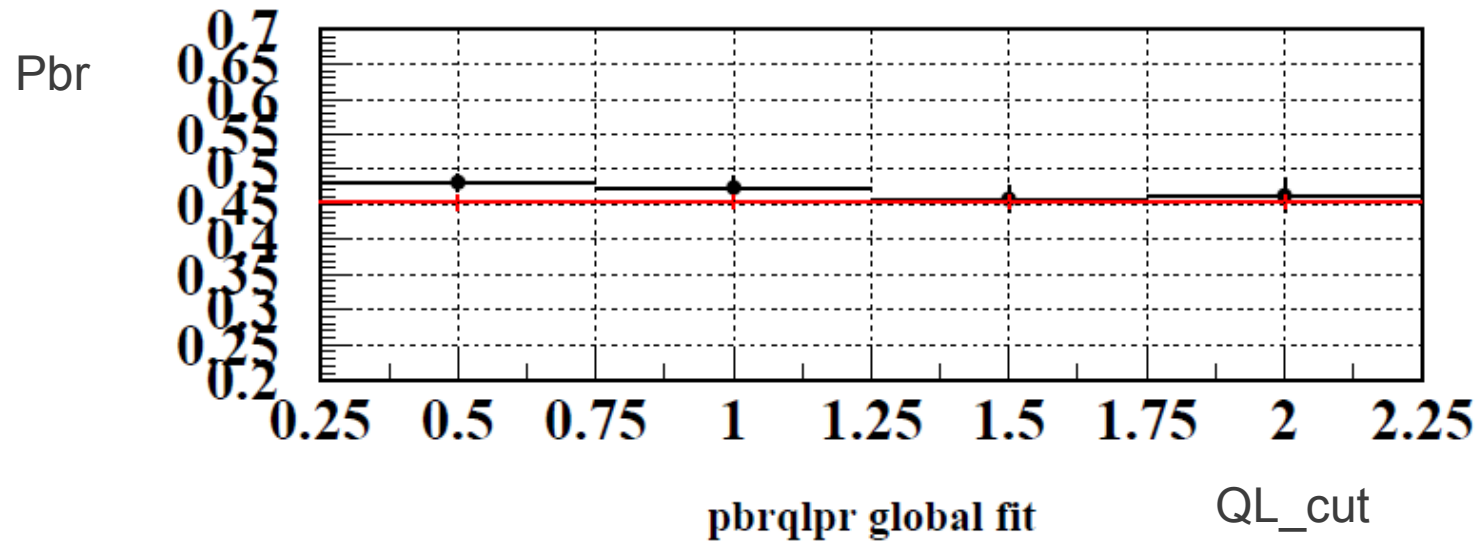


Pbr vs P for a tau=2.99 fs

Fit results: Laboratory momentum



Stability of Pbr with QL and QT cut



Systematic errors table

Source	Systematic error
(1) MS Ni (1%)	0.00767
MS Up (8%)	0.00017
Collapsed tracks	0.00144
Finite size	0.00108
Background	0.00014
Trigger simulation	0.00042
KK & pp	0.00110
Lambda (0.00066)	0.00260
Target impurity	0.00131
A2pi-Ni cross section (0.5%)	0.00224
A2pi transport eq. (0.8%)	0.00358
Total ($\sqrt{\sum es_i^2}$)	0.00939

(statistical error is 0.0093)

Summary for the Pbr measurements and results

Data Sample	PBR	Chi2/ndf
2001 94um	0.4195 +- 0.0165	267/280
2001 98um	0.4747 +- 0.0280	316/280
2002 20 GeV/c	0.4808 +- 0.0231	301/280
2002 24 GeV/c	0.4311 +- 0.0161	267/280
2003 20 GeV/c	0.4708 +- 0.0295	266/280

DIRAC results

Tau (fs) = 2.99 +0.18 -0.17 (stat) +0.19 -0.17 (syst)

Tau (fs) = 2.99 +0.26 -0.24 (8.7%)

|a0-a2| = 0.2606 +- 0.011 (4.2%)

ChPT calculations

Tau = 2.9 +- 0.1 (3.4%)

|a0-a2| = 0.265 +- 0.004 (1.5%)

Conclusions:

- A new final state, the Pionium, has been copiously produced in the laboratory (**22287 atomic pairs**), and its ionization spectrum has been fully mapped in both the longitudinal and transverse projections.
- Making no assumptions on the physics of pNi collisions, we have determined the pionium lifetime (in 1S state), to be **$\tau_{1s} = 2.99 + 0.26 - 0.24 \text{ fs}$** , using the full DIRAC experiment data sample.
- Given the existence of a rigorous next-to-leading order calculation in QCD and QED, the pionium lifetime determination has been converted into a 4% measurement of the s-wave isospin $\pi\pi$ scattering length difference $|a_0 - a_2|$ in the process $\pi^+\pi^- \rightarrow \pi^0\pi^0$ at threshold, with the result **$|a_0 - a_2| = 0.261 \pm 0.011 \text{ M}\pi^{-1}$**