



# Measurement of the $\pi^+\pi^-$ atom lifetime at DIRAC

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**XII INTERNATIONAL CONFERENCE ON HADRON SPECTROSCOPY**

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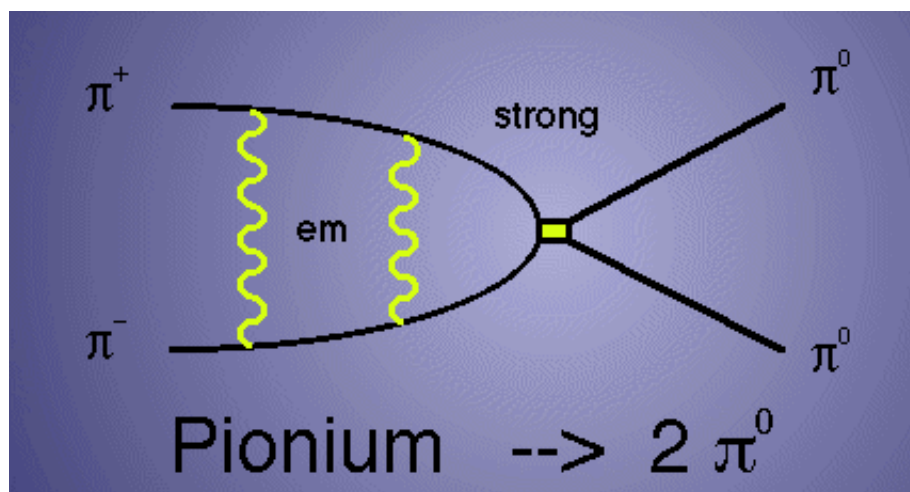
# DIRAC



## DI meson R elativistic A tomic C omplexes

Lifetime Measurement of  $\pi^+\pi^-$  atoms to test low energy QCD predictions

[www.cern.ch/DIRAC](http://www.cern.ch/DIRAC)



Basel Univ., Bern Univ., Bucharest IAP, CERN, Dubna JINR, Frascati LNF-INFN, Ioannina Univ., Kyoto-Sangyo Univ., Kyushu Univ. Fukuoka, Moscow NPI, Paris VI Univ., Prague TU, Prague FZU-IP ASCR, Protvino IHEP, Santiago de Compostela Univ., Tokyo Metropolitan Univ., Trieste Univ./INFN, Tsukuba KEK.

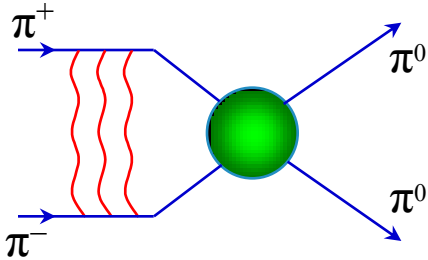
90 Physicists from 18 Institutes

# Pionium lifetime

Pionium is a hydrogen-like atom consisting of  $\pi^+$  and  $\pi^-$  mesons

$$E_B = -1.86 \text{ keV}, \quad r_B = 387 \text{ fm}, \quad p_B \approx 0.5 \text{ MeV}$$

The lifetime of  $\pi^+\pi^-$  atoms ( $A_{2\pi}$ ) is dominated by charge exchange process into  $\pi^0\pi^0$ :



$$\Gamma = \frac{1}{\tau} = \Gamma_{2\pi^0} + \Gamma_{2\gamma} \quad \frac{\Gamma_{2\gamma}}{\Gamma_{2\pi^0}} \approx 4 \times 10^{-3}$$

$$\Gamma_{1S, 2\pi^0} = \frac{1}{\tau_{1S}} \propto |a_0 - a_2|^2$$

$a_0$  and  $a_2$  are the  $\pi\pi$  S-wave scattering lengths for isospin  $I=0$  and  $I=2$ .

$$\frac{\Delta\tau}{\tau} = 10\% \quad \Rightarrow \quad \frac{\Delta(a_0 - a_2)}{a_0 - a_2} = 5\%$$

# Pionium lifetime in QCD

J.Gasser et al., Phys.Rev. D64 (2001) 016008:

$$\Gamma_{2\pi^0} = \frac{1}{\tau} = \frac{2}{9} \alpha^3 p |a_0 - a_2|^2 (1 + \delta_\Gamma), \quad \delta_\Gamma = (5.8 \pm 1.2)\%$$

The  $\pi\pi$  scattering lengths have been calculated in the framework of Chiral Perturbation Theory (ChPT):

G. Colangelo, J. Gasser and H. Leutwyler, Nucl. Phys. B603 (2001) 125:

$$a_0 = 0.220 \pm 0.005, \quad a_2 = -0.0444 \pm 0.0010,$$
$$a_0 - a_2 = 0.265 \pm 0.004$$

$$\tau = (2.9 \pm 0.1) \times 10^{-15} \text{ s}$$

# Experimental results

## $K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$ ( $K_{e4}$ ) decay

$a_0 = 0.26 \pm 0.05$  L. Rosselet et al., Phys. Rev. D 15 (1977) 574

$a_0 = 0.216 \pm 0.013$  New measurement at BNL (E865)  
 $0.003$  (syst) S. Pislak et al., Phys. Rev. D 67 (2003) 072004

$a_2 = -0.0454 \pm 0.0031$   
 $0.0013$  (syst)

## $\pi N \rightarrow \pi \pi N$ near threshold

$a_0 = 0.26 \pm 0.05$  C.D. Froggatt, J.L. Petersen, Nucl. Phys. B 129 (1977) 89

$a_0 = 0.204 \pm 0.014$  M. Kermani et al., Phys. Rev. C 58 (1998) 3431  
 $0.008$  (syst)

## $K^+ \rightarrow \pi^+ \pi^0 \pi^0$ and $K_L \rightarrow 3\pi^0$ NA48

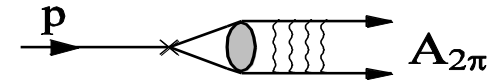
$|a_0 - a_2| = 0.268 \pm 0.010$  (stat.) NA48/2, Phys. Lett. B 633, 2006

$\pm 0.004$  (syst.)  $\pm 0.013$  (ext.)

# Production of pionium

**Atoms** are Coulomb bound state of two pions produced in one proton-nucleus collision

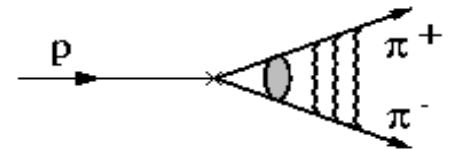
$$\frac{d\sigma_{nlm}^A}{d\vec{P}} = (2\pi)^3 \frac{E_A}{M_A} \left| \psi_{nlm}^{(C)}(0) \right|^2 \frac{d\sigma_s^0}{d\vec{p}_+ d\vec{p}_-} \Big|_{\vec{p}_+ = \vec{p}_-}$$



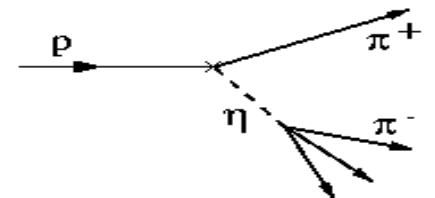
## Background processes:

**Coulomb pairs.** They are produced in one proton nucleus collision from fragmentation or short lived resonances and exhibit Coulomb interaction in the final state

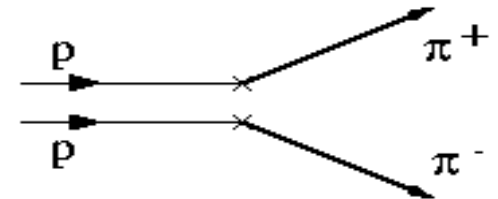
$$\frac{d^2\sigma_C}{d\vec{p}_+ d\vec{p}_-} = A_C(q) \frac{d\sigma_s^0}{d\vec{p}_+ d\vec{p}_-}, \quad A_C(q) = \frac{2\pi m_\pi \alpha / q}{1 - \exp(-2\pi m_\pi \alpha / q)}$$



**Non-Coulomb pairs.** They are produced in one proton nucleus collision. At least one pion originates from a long lived resonance. No Coulomb interaction in the final state



**Accidental pairs.** They are produced in two independent proton nucleus collision. They do not exhibit Coulomb interaction in the final state



# Method of ponium detection

L.Nemenov, Sov.J.Nucl.Phys. 41 (1985) 629

**Ponium is created in nS states then it interacts with target material:**

**Annihilation:**  $A_{2\pi} \rightarrow \pi^0 \pi^0$

$$\lambda_{\text{decay}} = \gamma c \tau \approx 15 \mu\text{m} \text{ for } \gamma \approx 17$$

**Excitation:** transitions between atomic levels

$$\lambda_{\text{int}}^{1S} \approx 20 \mu\text{m} \text{ for Ni}$$

**Break-up(ionisation):** characteristic “atomic” pairs  $n_A$

- $Q_{\text{cms}} < 3 \text{MeV}/c$
- $\rightarrow$  in laboratory system  $E_+ \approx E_-$ , small opening angle  $\theta < 3 \text{mrad}$

**Coulomb and atomic pairs are detected simultaneously**

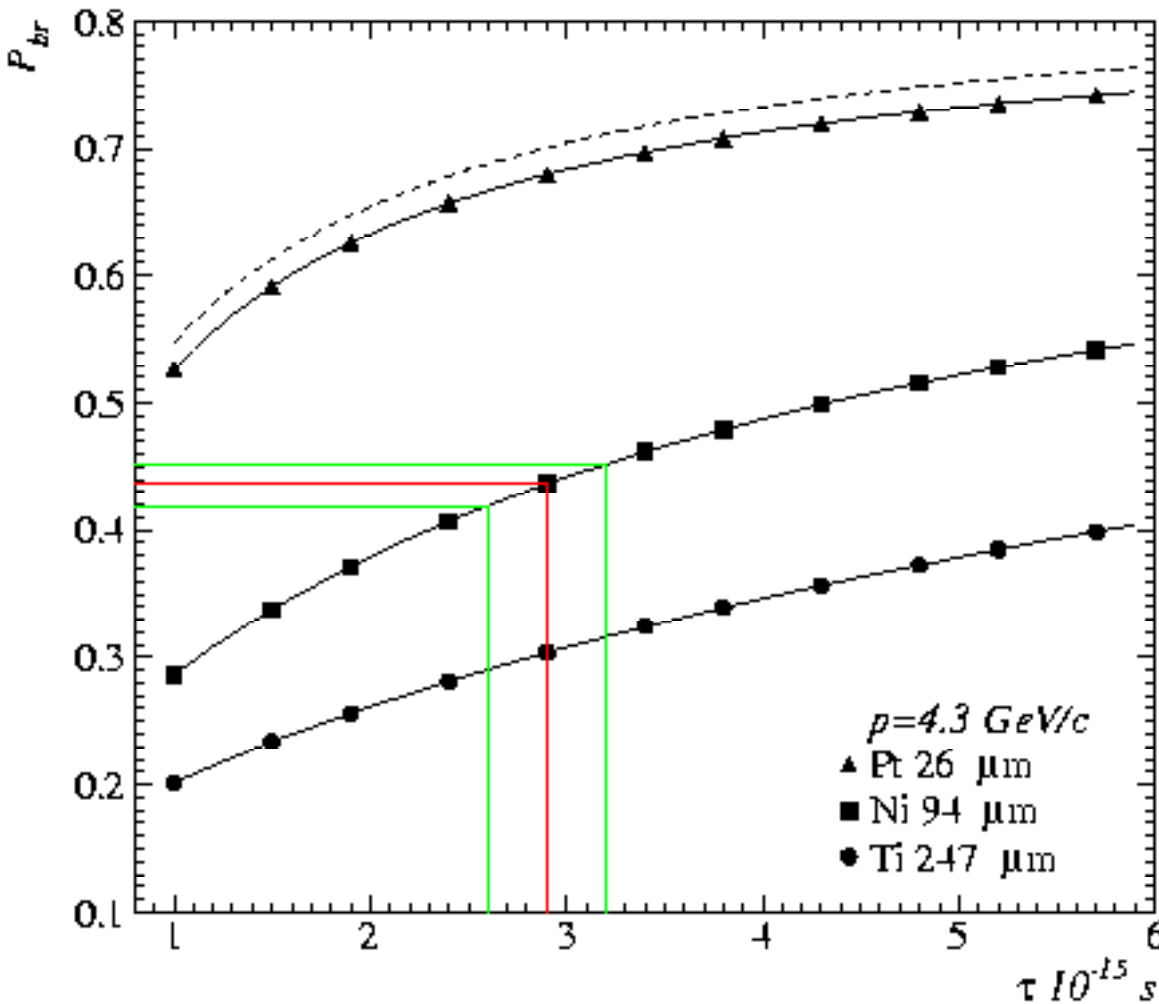
$$P_{br} = \frac{n_A}{N_A} = \frac{n_A}{k N_C}$$

# Break-up probability

Solution of the transport equations provides one-to-one dependence of the measured break-up probability ( $P_{br}$ ) on pionium lifetime  $\tau$

All targets have the same thickness in radiation lengths  $6.7 \cdot 10^{-3} X_0$

There is an optimal target material for a given lifetime



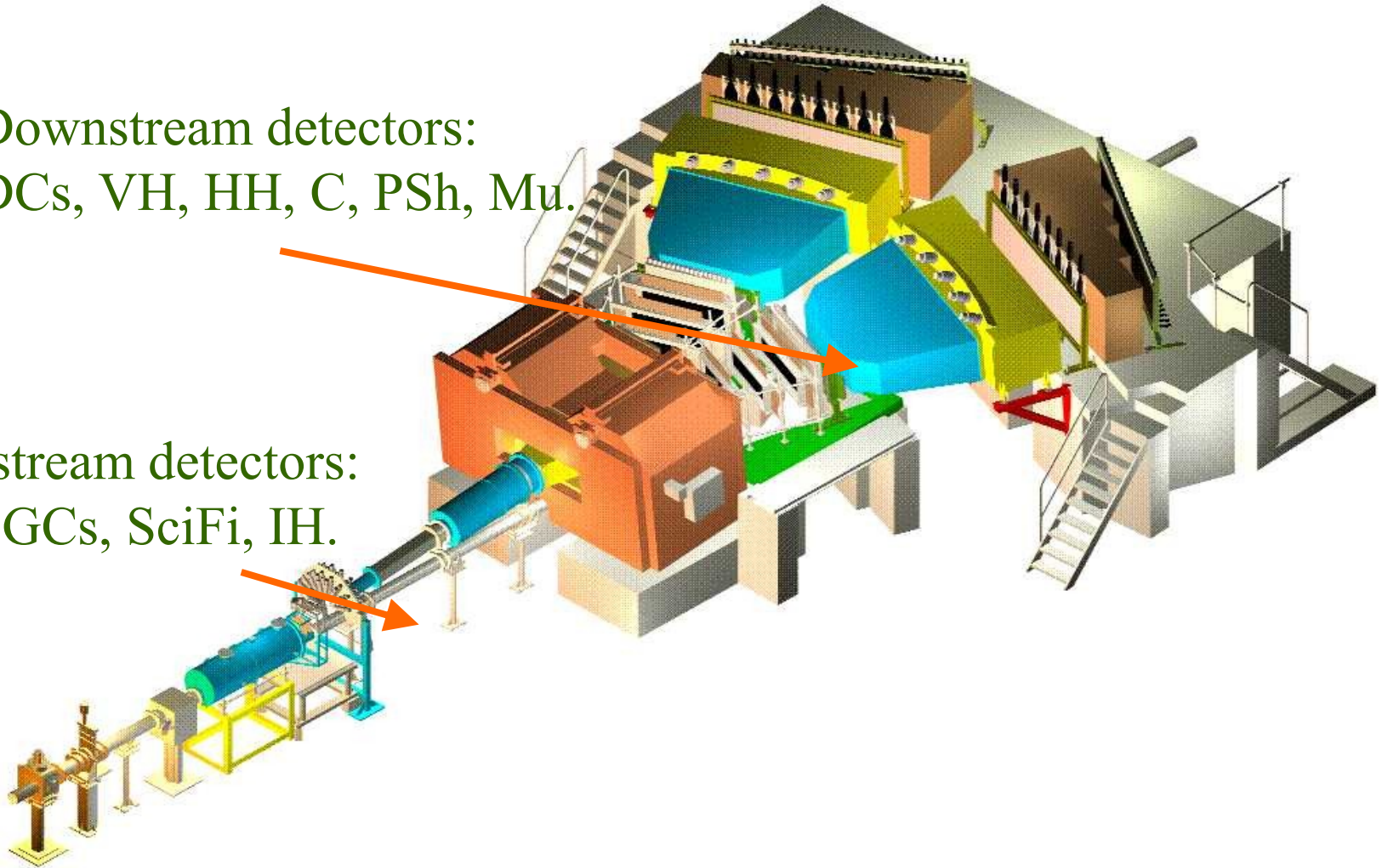
The detailed knowledge of the cross sections (Afanasyev&Tarasov; Trautmann et al) (Born and Glauber approach) together with the accurate description of atom interaction dynamics (including density matrix formalism) permits us to know the curves within 1%.



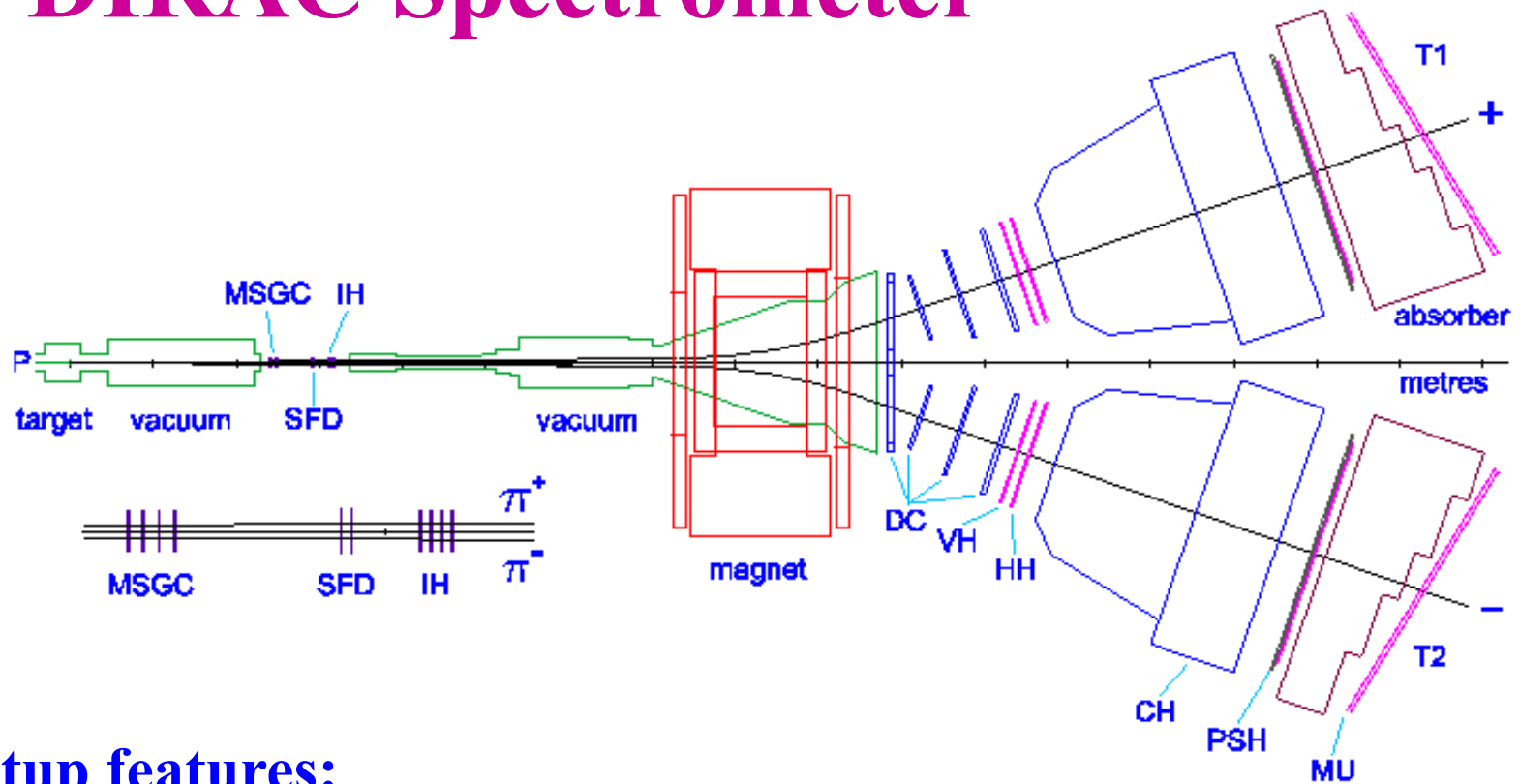
# DIRAC Spectrometer

Downstream detectors:  
DCs, VH, HH, C, PSh, Mu.

Upstream detectors:  
MSGCs, SciFi, IH.



# DIRAC Spectrometer



## Setup features:

angle to proton beam  $\Theta=5.7^\circ$

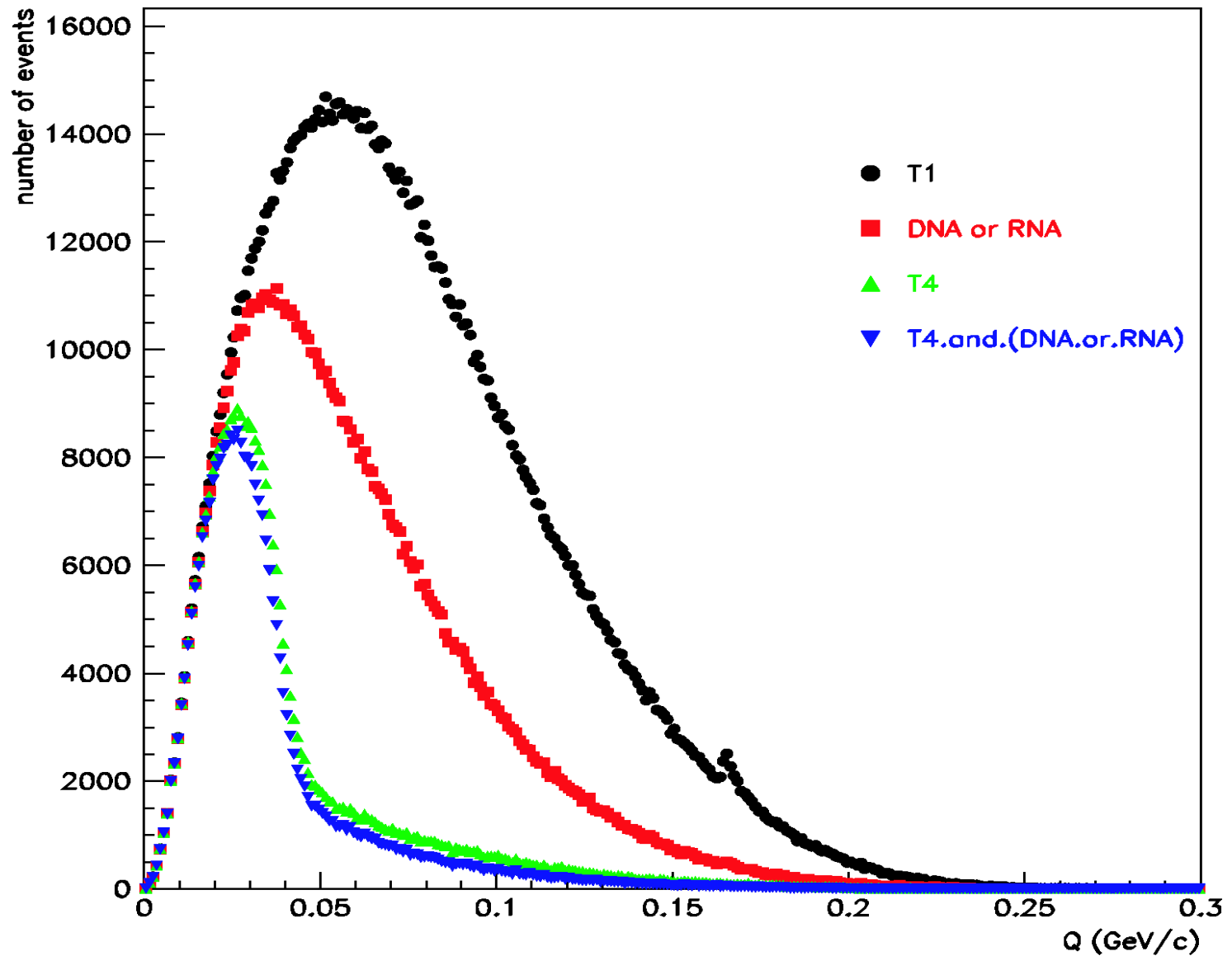
channel aperture  $\Omega=1.2 \cdot 10^{-3}$  sr

magnet 2.3 T·m

momentum range  $1.2 \leq p_\pi \leq 7$  GeV/c

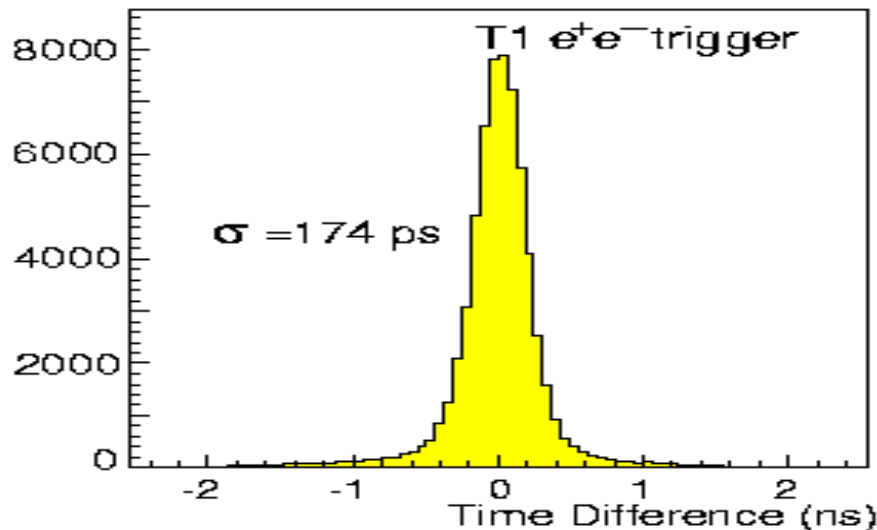
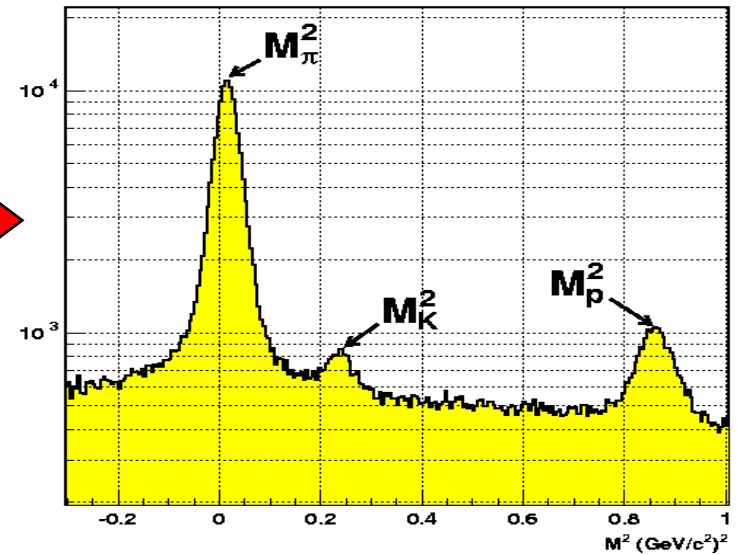
resolution on relative momentum  $\sigma_{QX} \approx \sigma_{QY} \leq 0.5$  MeV/c,  $\sigma_{QL} \approx 0.5$  MeV/c

# Trigger performance

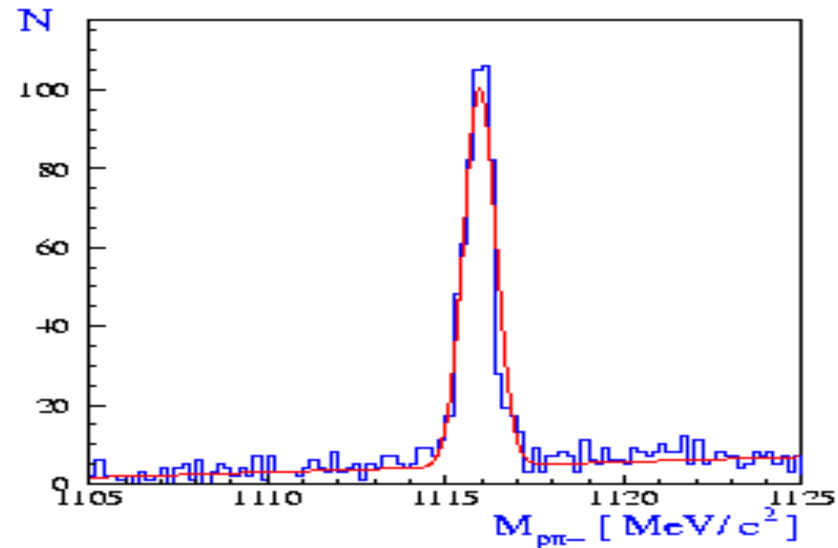


# Calibrations

Positive arm mass spectrum, obtained by TOF difference, under  $\pi^-$  hypothesis in the negative arm.



Time difference spectrum at VH with  $e^+e^-$  T1 trigger.



Mass distribution of  $p\pi^-$  pairs from  $\Lambda$  decay.  $\sigma_\Lambda = 0.43 \text{ MeV}/c^2 < 0.49 \text{ MeV}/c^2$  (Hartouni et al.).

# Analysis based on MC

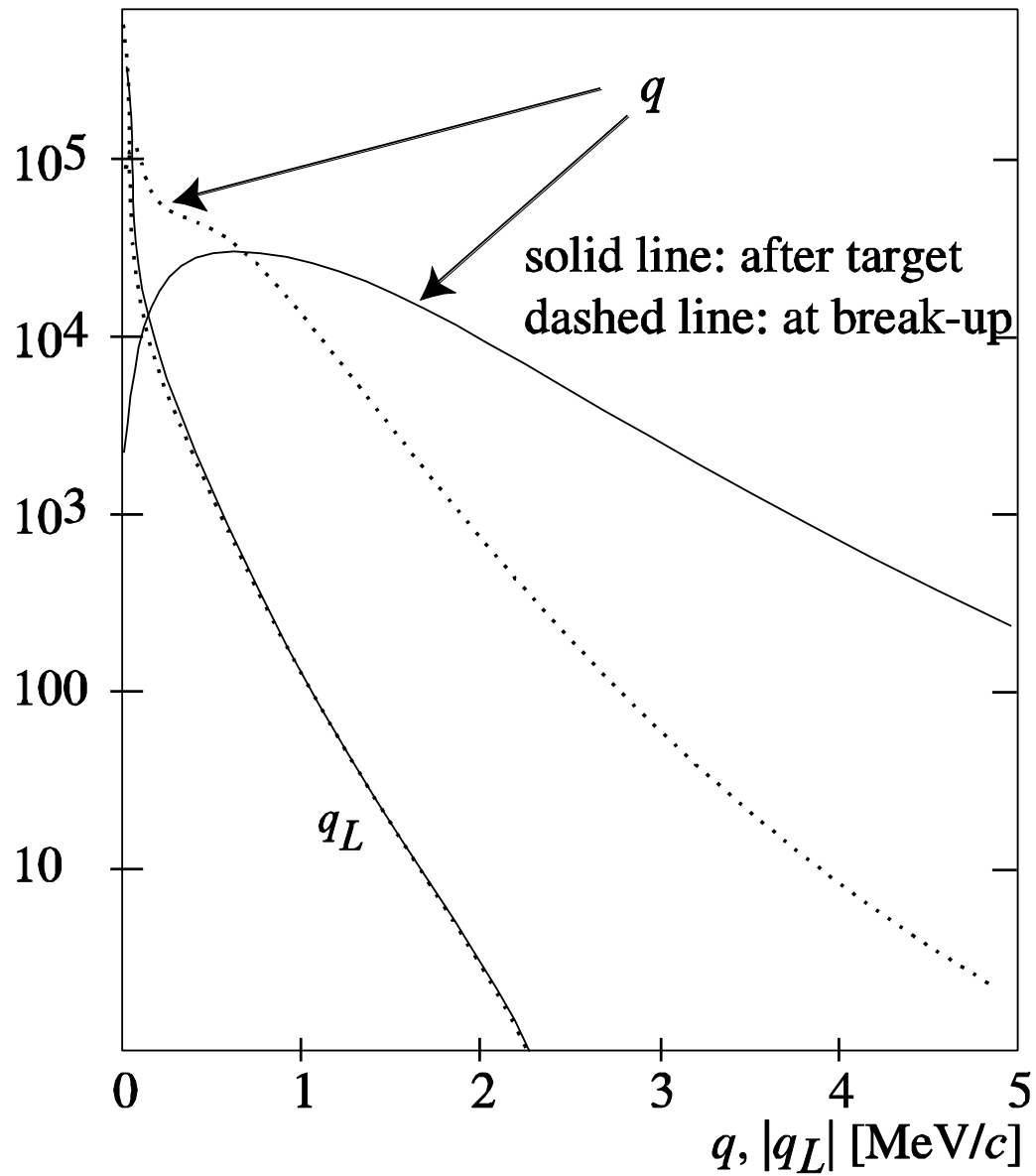
**Atoms** are generated in **nS states** using measured momentum distribution for **short-lived** sources. The atomic pairs are generated according to the evolution of the atom while propagating through the target

## Background processes:

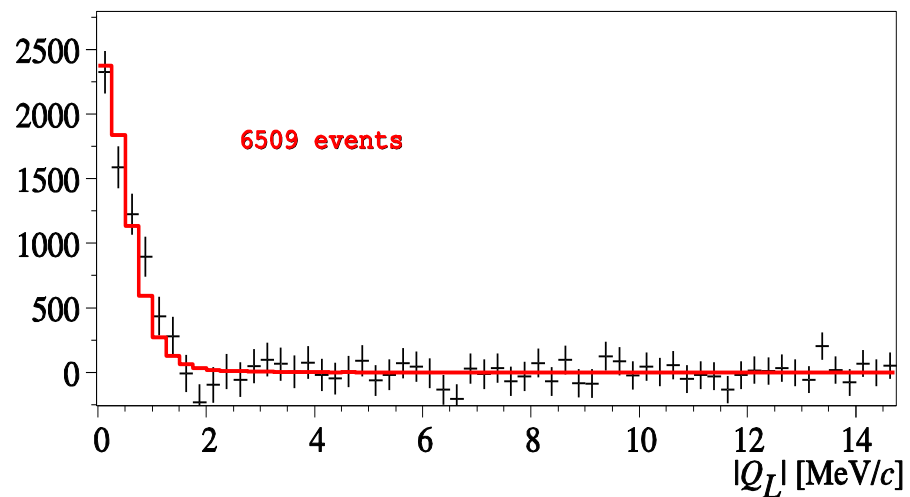
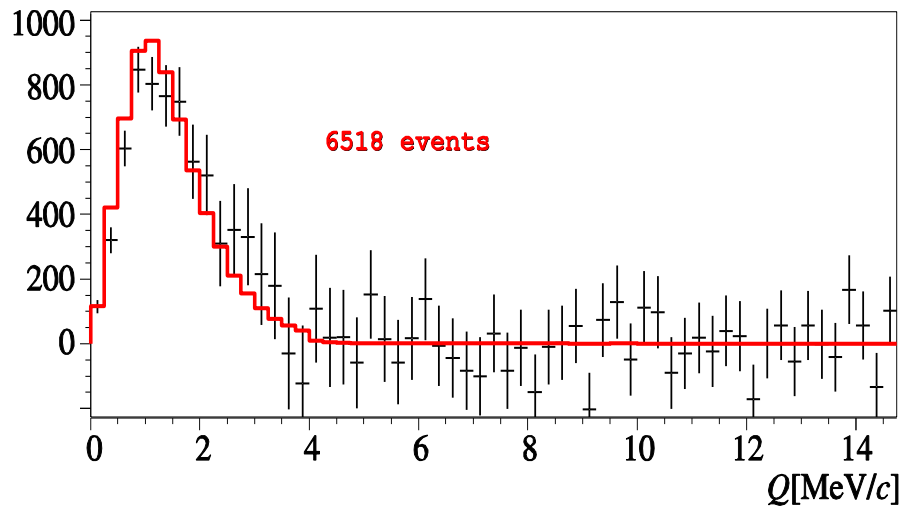
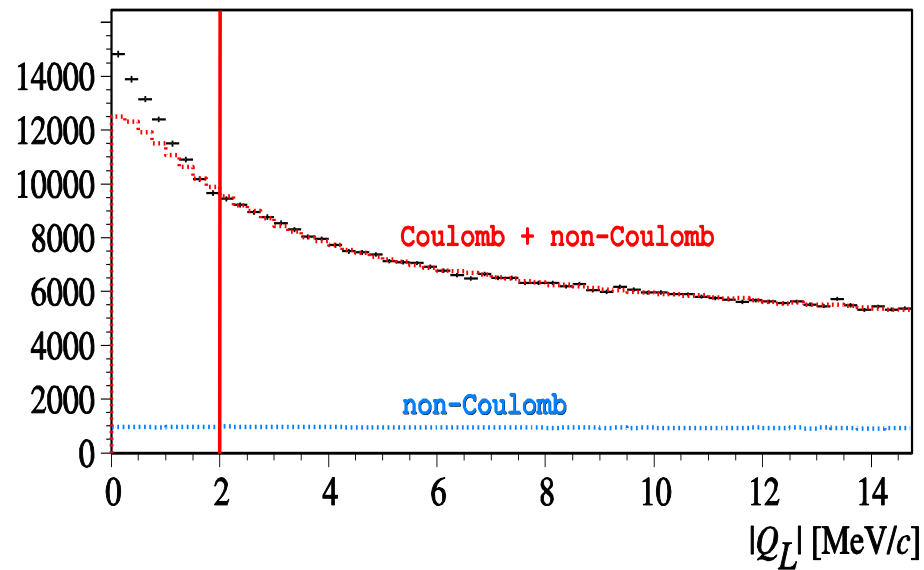
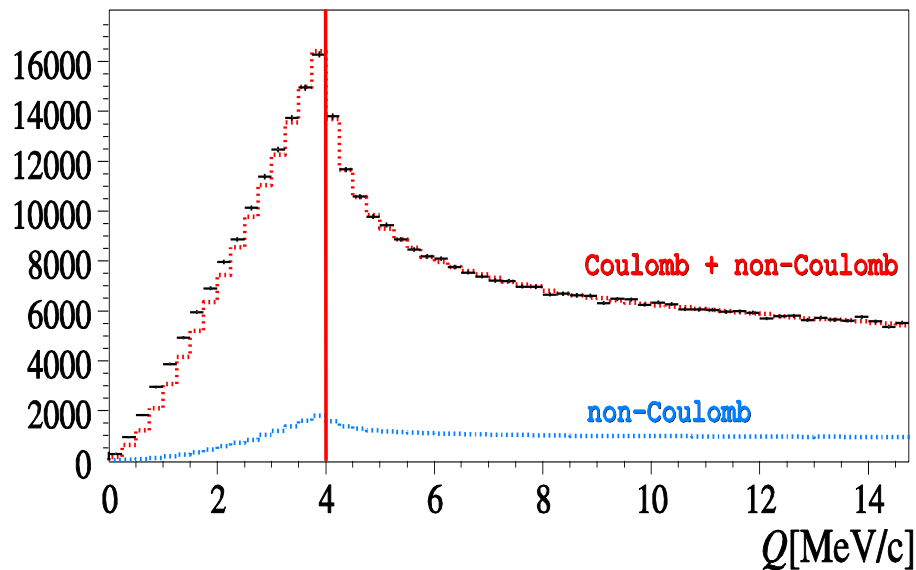
**Coulomb pairs** are generated according to  $A_C(Q)Q^2$  using measured momentum distribution for **short-lived** sources.

**Non-Coulomb pairs** are generated according to  $Q^2$  using measured momentum distribution for **long-lived** sources.

# Atomic pairs MC



# Atomic pairs (2001)



# Break-up probability

$$P_{br} = \frac{n_A}{N_A} = \frac{n_A^{rec}(Q \leq Q_{cut})}{k(Q_{cut}) N_C^{rec}(Q \leq Q_{cut})}$$

$$P_{br} = 0.452 \pm 0.023_{stat} \left. \begin{array}{l} +0.009 \\ -0.032 \end{array} \right\}_{syst} = 0.452_{-0.039}^{+0.025}$$

## Lifetime

$$\tau = \left( 2.91_{-0.38}^{+0.45} \right)_{stat} \left( \begin{array}{l} +0.19 \\ -0.49 \end{array} \right)_{syst} \text{ fs}$$

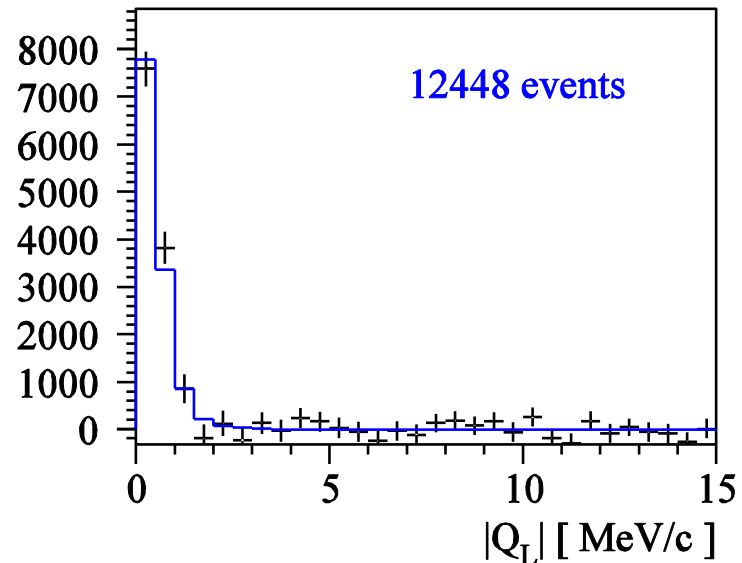
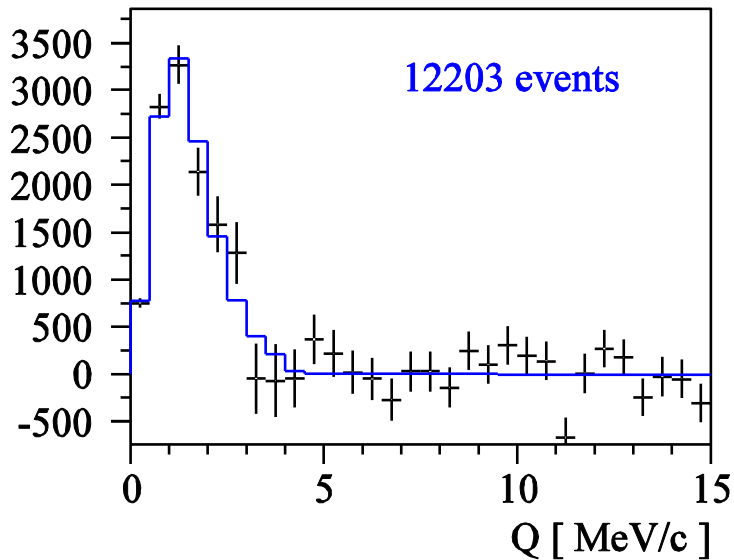
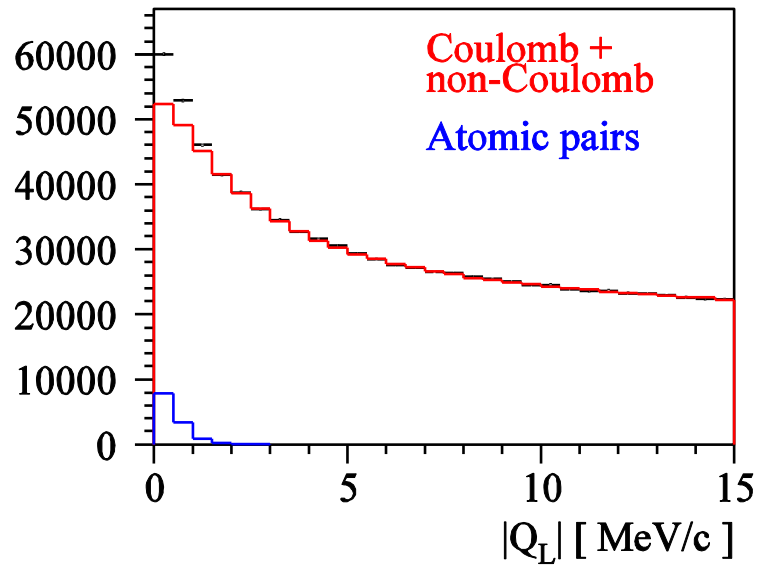
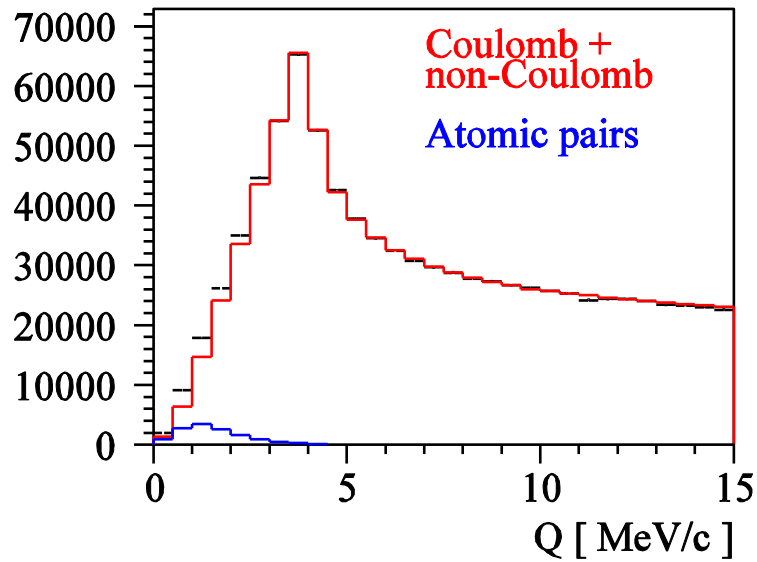
Phys. Lett. B 619 (2005) 50-60; [hep-ex/0504044](#)

**ChPT prediction:**

$$\tau = (2.9 \pm 0.1) \text{ fs}$$



# Atomic pairs (2001+2002+2003)



# Estimation of relative errors for break-up probability measurement

	$Q$	$Q_L$	$Q_L Q_T$
Statistical	0.031	0.044	0.031
Multiple scattering	0.018	0.008	0.014
Heavy particles admixture	0.001	0.008	0.001
Finite size effects	0./ -0.006	0./ -0.004	0./ -0.005/
Double track resolution	0.009	0.001	0.003
Background particles	0.002	0.003	0.002
Trigger simulation	0.002	0.002	0.003
All systematic	+0.021/ -0.022	0.012	+0.015/ -0.016

**Estimation of relative errors for lifetime**

<b>Statistical</b>	<b>0.087 - 0.122</b>
<b>Systematic</b>	<b>0.033 - 0.060</b>

# Conclusions

1. Data collected in 2001, 2002 and 2003 are analyzed. These data allows to obtain statistical accuracy better than 10%.
2. Multiple scattering and admixture of  $K^+K^-$  and  $p\bar{p}$  pairs is measured in order to decrease systematic errors.
3. Systematic errors due to detector response description are estimated.

# Break-up probability

$$P_{br} = \frac{n_A}{N_A} = \frac{n_A^{rec}(Q \leq Q_{cut})}{k(Q_{cut}) N_C^{rec}(Q \leq Q_{cut})}$$

	$n_A$		$N_C(Q_{cut})$		$P_{br}$	
<b>Q</b>	<b>6518</b>	<b>373</b>	<b>106500</b>	<b>1130</b>	<b>0.442</b>	<b>0.026</b>
<b>Q<sub>L</sub></b>	<b>6509</b>	<b>330</b>	<b>82289</b>	<b>873</b>	<b>0.445</b>	<b>0.023</b>
<b>Q&amp;Q<sub>L</sub></b>	<b>6530</b>	<b>294</b>	<b>106549</b>	<b>1004</b>	<b>0.447</b>	<b>0.023</b>

$k(Q_{cut}=4 \text{ MeV/c})=0.1384$ ,  $k(Q_{L,cut}=2 \text{ MeV/c})=0.1774$

*Due to target impurities by atoms with  $Z < 28$   $P_{br}$  has to be increased by 0.005*

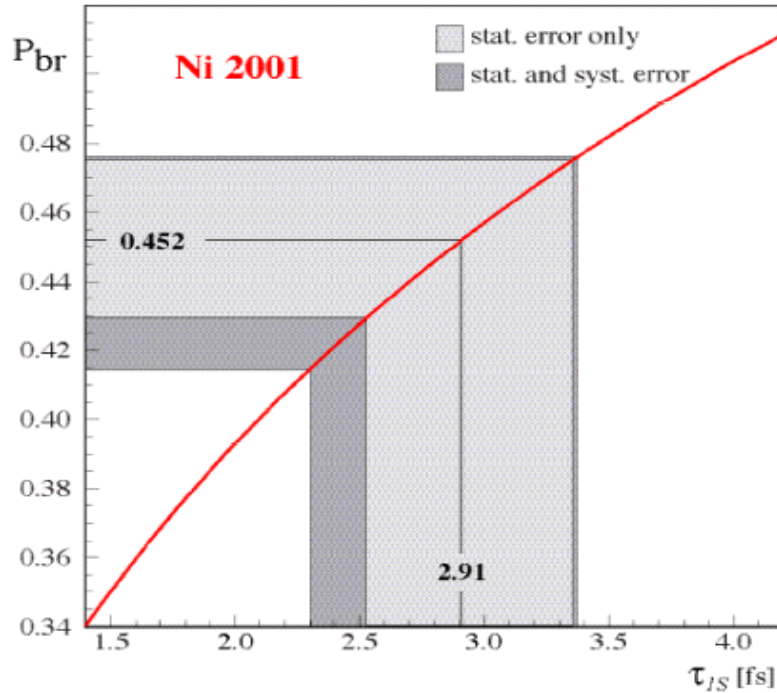
# Breakup probability

$$P_{br} = 0.452 \pm 0.023_{stat} \left. \begin{array}{l} +0.009 \\ -0.032 \end{array} \right\}_{syst} = 0.452^{+0.025}_{-0.039}$$

## Summary of systematic uncertainties:

source	$\sigma$
CC-background	$\pm 0.007$
signal shape	$\pm 0.002$
multiple scattering angle $^{+5\%}_{-10\%}$	$+0.006$ $-0.013$
$K^+K^-$ and $\bar{p}p$ pairs admixture	$+0.000$ $-0.024$
correlation function for non-point production	$+0.000$ $-0.017$
<b>Total</b>	<b><math>+0.009</math></b> <b><math>-0.032</math></b>

# Lifetime of Pionium



**Result from DIRAC:**

$$\tau = \left( 2.91^{+0.45}_{-0.38} \right)_{stat} \left( {}^{+0.19}_{-0.49} \right)_{syst} \text{ fs}$$

**ChPT prediction:**

$$\tau = (2.9 \pm 0.1) \text{ fs}$$

Phys. Lett. B 619 (2005) 50-60; hep-ex/0504044