
Electroweak Precision Data Global Higgs Analysis

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Outline

Overview on precision measurements

Tests of the electroweak Standard Model

Caveat: Low Higgs Masses

Conclusions

Thanks to the members of the LEPWWG and the CDF, DØ, SLD, OPAL, L3, DELPHI, ALEPH and NuTeV experiments!

Visit <http://www.cern.ch/LEPEWWG>

Electroweak Precision Data

More than 1000 measurements with (correlated) uncertainties:

Reduced to 20 precision pseudo-observables:

Z-pole (SLD, LEP-1):

- 5 Z lineshape and leptonic forward-backward asymmetries
- 2 Polarised lepton asymmetries P_τ , $A_{LR}(\text{FB})$
- 6 Heavy flavour results (b,c)
- 1 Hadronic charge asymmetry

Other:

- 2 W mass and width (Tevatron, LEP-2) (New LEP-2 M_W)
- 1 Top-quark mass (Tevatron)
- 1 Neutrino-nucleon scattering (NuTeV)
- 1 Atomic parity violation (Caesium) (New corrections)
- 1 Hadronic vacuum polarisation (Z-pole / g-2?)

20

plus "constants" such as the Fermi constant G_F

Atomic Parity Violation

Electron-nucleus interaction:

Parity-violating t-channel contribution due to γ/Z interference

Weak charge Q_W of the nucleus (Z protons, N neutrons)

$$Q_W(Z,N) = -2 [(2Z+N)C_{1u} + (Z+2N)C_{1d}]$$

with $C_{1q} = 2g_{Ae}g_{Vq}$ at $Q^2 \rightarrow 0$ (q=u,d)

Most precise measurement for Caesium (Z=55, N=78)

Progress in theoretical corrections applied to measurements:

QED self-energy and vertex radiative corrections $Z\alpha^2$ and $Z^2\alpha^3$

hep-ph/0204134, 0206124, 0208196, 0208227

$$Q_W(\text{Cs}) = -72.18 \pm 0.29 \text{ (exp.)} \pm 0.36 \text{ (theo.)}$$

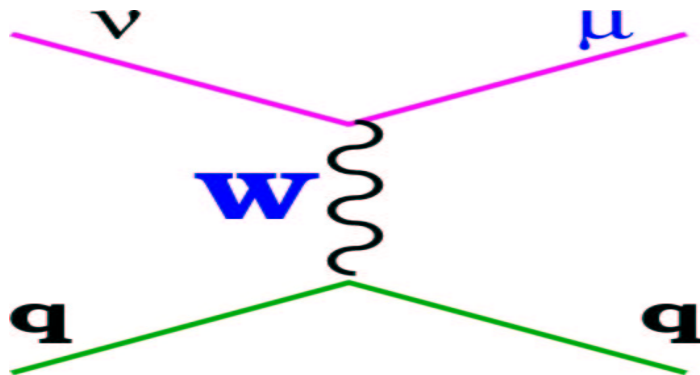
$$\rightarrow -72.83 \pm 0.29 \text{ (exp.)} \pm 0.39 \text{ (theo.)}$$

Now perfect agreement with SM expectation!

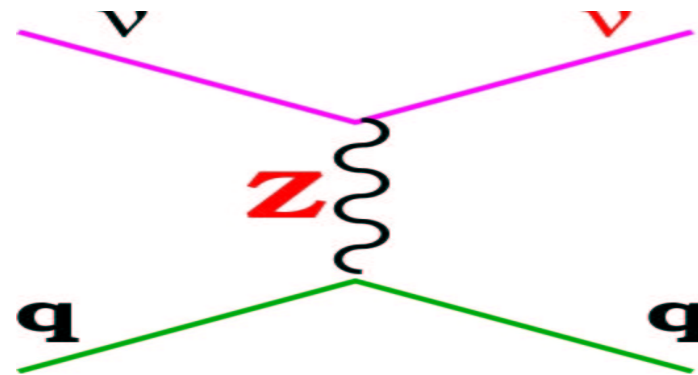
NuTeV Neutrino-Nucleon Scattering

Muon-(anti-)neutrino quark scattering:

charged current (CC)



neutral current (NC)



Paschos-Wolfenstein relation (iso-scalar target):

$$R_- = \frac{\sigma_{NC}(\nu) - \sigma_{NC}(\bar{\nu})}{\sigma_{CC}(\nu) - \sigma_{CC}(\bar{\nu})} = 4g_{Lv}^2 \sum_{qv} [g_{Lq}^2 - g_{Rq}^2] = \rho_\nu \rho_{ud} \left[\frac{1}{2} - \sin^2 \theta_W^{(on-shell)} \right]$$

+ electroweak radiative corrections

Effective couplings: g_L, g_R at $\langle Q^2 \rangle \sim 20 \text{ GeV}^2$

Historically result quoted in terms of: $\sin^2 \Theta_W = 1 - (M_W/M_Z)^2$

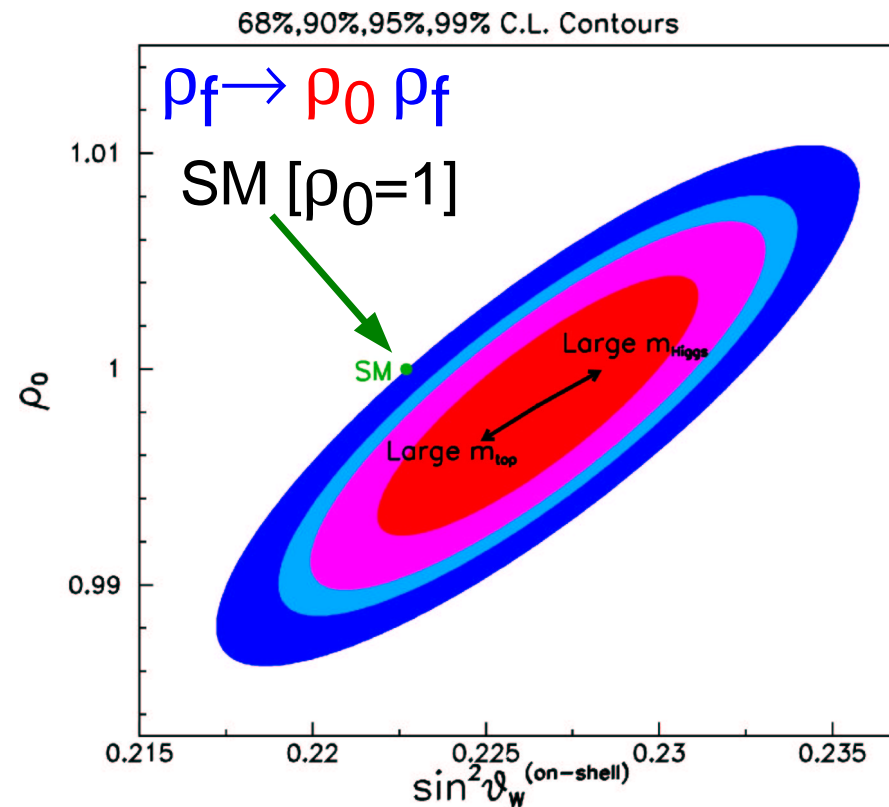
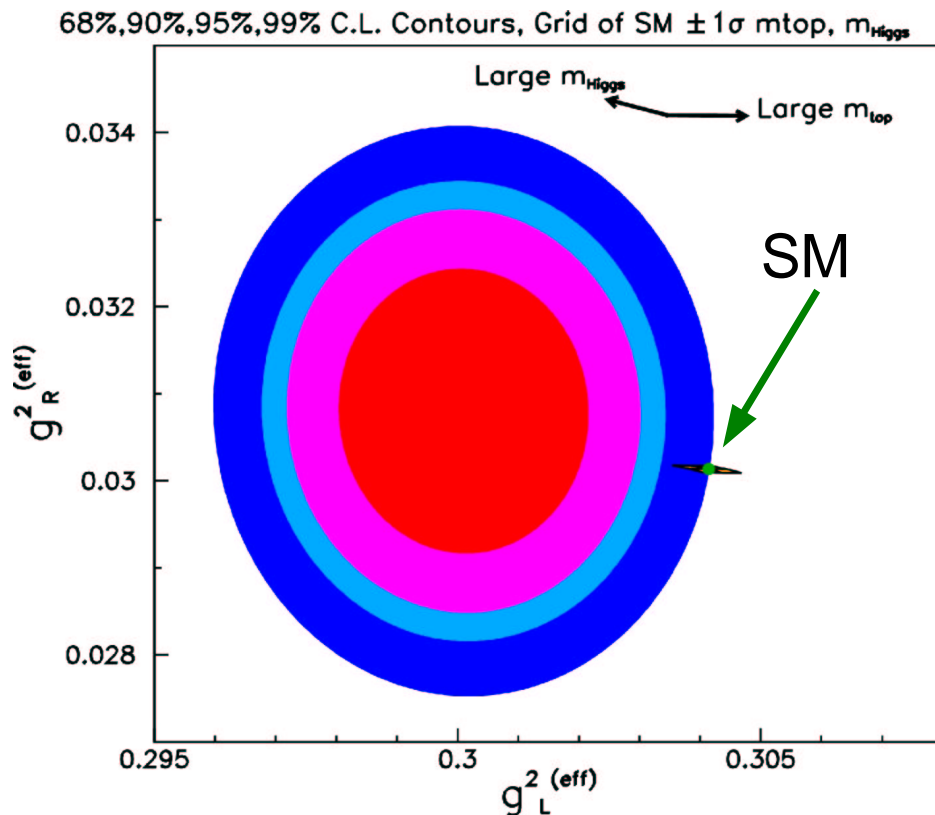
Factor two more precise than previous νN world average

NuTeV's Result

$$\sin^2 \theta_W^{(on-shell)} = 1 - \frac{M_W^2}{M_Z^2} = 0.2277 \pm 0.0013 (stat.) \pm 0.0009 (syst.)$$

$$- 0.00022 \frac{M_{top}^2 - (175 GeV)^2}{(50 GeV)^2} + 0.00032 \ln \frac{M_{Higgs}}{150 GeV} \quad [\rho = \rho_{SM}]$$

Global SM analysis predicts: 0.2229(4) Difference of 2.9 σ !



Quote result in terms of effective couplings, not $\sin^2 \theta_W$ nor M_W !

Mass of the Top Quark

Tevatron (CDF, DØ):

$p\bar{p} \rightarrow t\bar{t}X$, $t\bar{t} \rightarrow b\bar{b}WW$

No results from Run-II yet

Final Run-I results in RPP

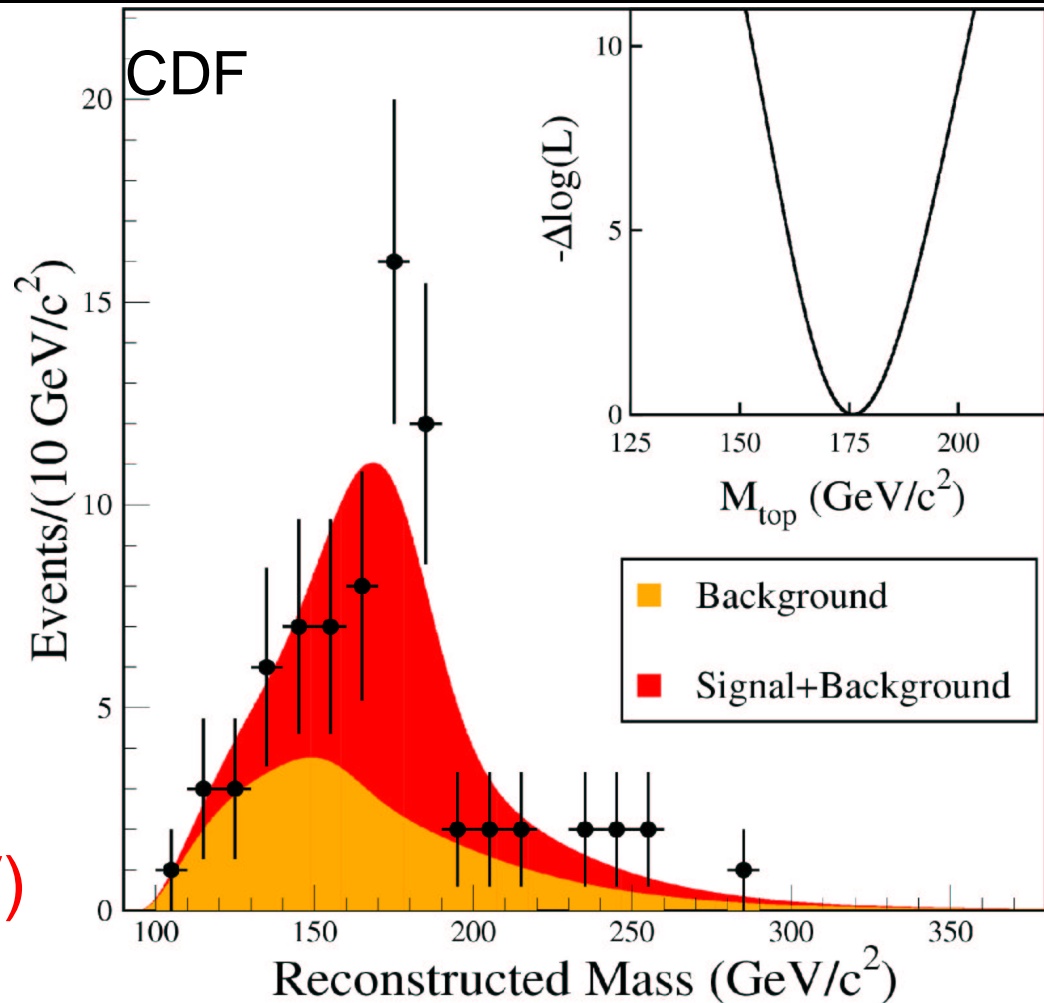
Systematic uncertainties
dominated by:

Jet energy scale (2-5 GeV)
will reduce with more data

Signal model (2-3 GeV)

Background model (~2 GeV)

MEs, PDFs, MC generators



Run-I result: $M_{\text{top}} = 174.3 \pm 3.2$ (stat.) ± 4.0 (syst.) GeV

Run-II expectation: $\delta M_{\text{top}} < 2.5$ GeV

W Boson - Mass and Width

Tevatron (CDF, DØ):

$p\bar{p} \rightarrow WX, W \rightarrow e\nu, \mu\nu$

Transverse mass M_T

No results from Run-II yet

Final Run-I results

Uncertainties dominated by:

Statistics

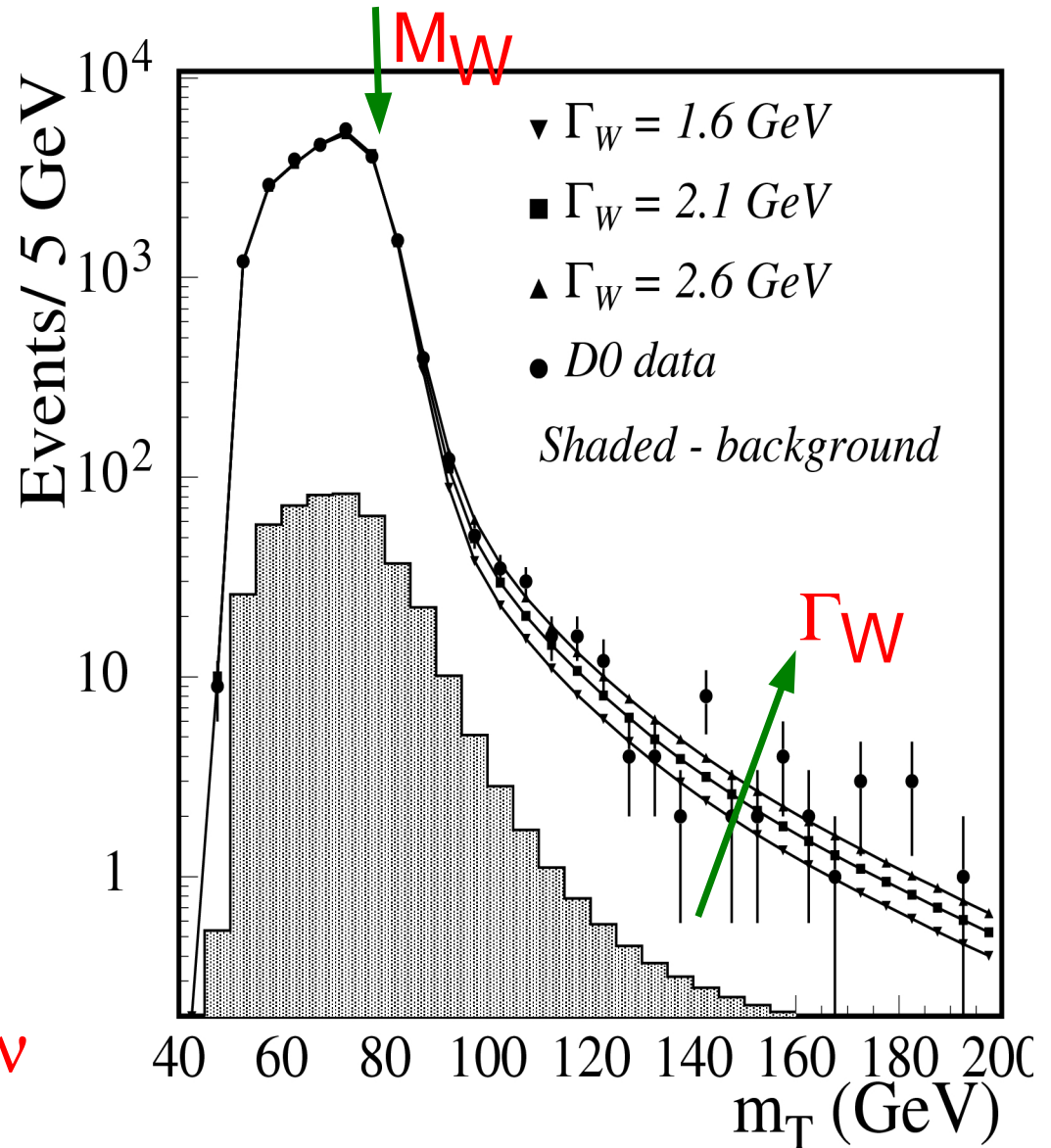
Lepton energy scale

will reduce with more data

Then: Signal model

PDFs, gluon radiation

QED corrections in $W \rightarrow l\nu$



Run-II expectation: $\delta M_W < 25 \text{ MeV}$

W Boson - Mass and Width

LEP-2: $e^+e^- \rightarrow W^+W^-$

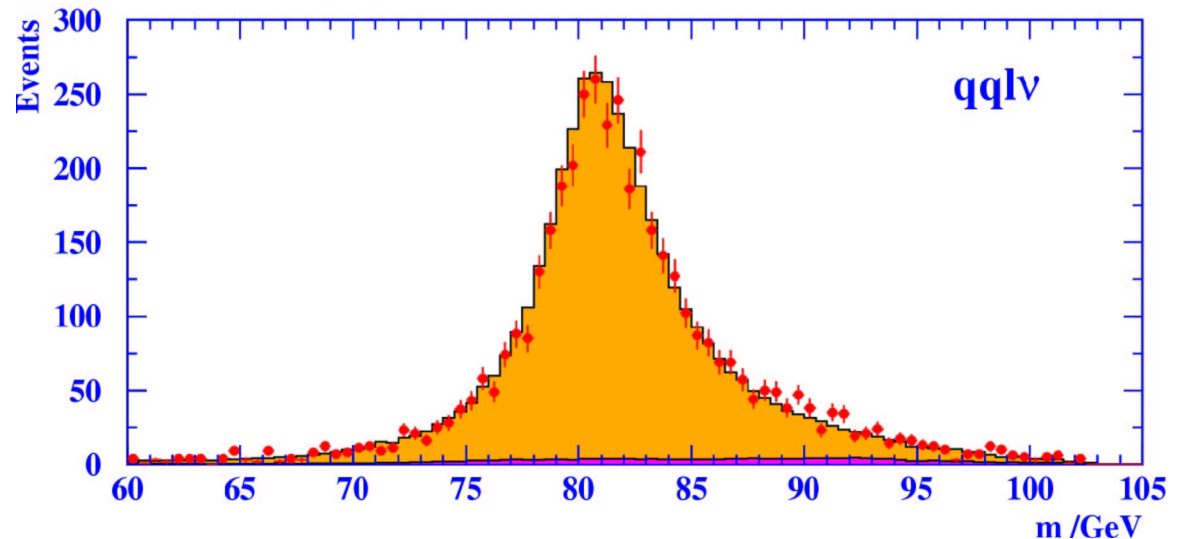
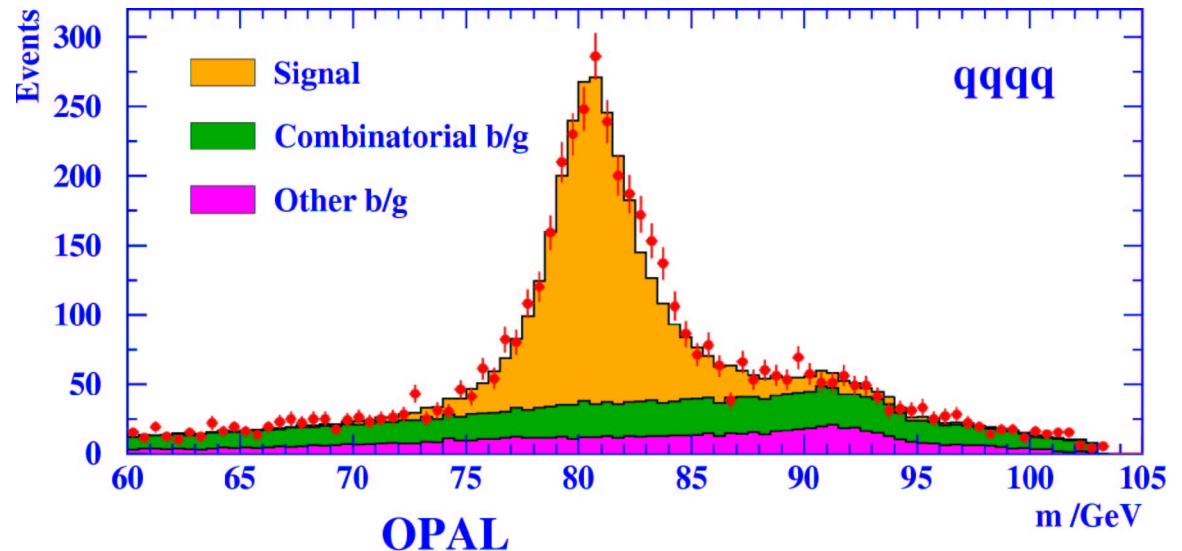
$\rightarrow q\bar{q}q\bar{q}, q\bar{q}l\nu, l\nu l\nu$

Invariant mass M_{inv}

Preliminary results

Currently large FSI systematics (BE,CR) in the $q\bar{q}q\bar{q}$ channel:

Average dominated by $M_{WW}(q\bar{q}l\nu)$



Mass difference (calculated without FSI errors):

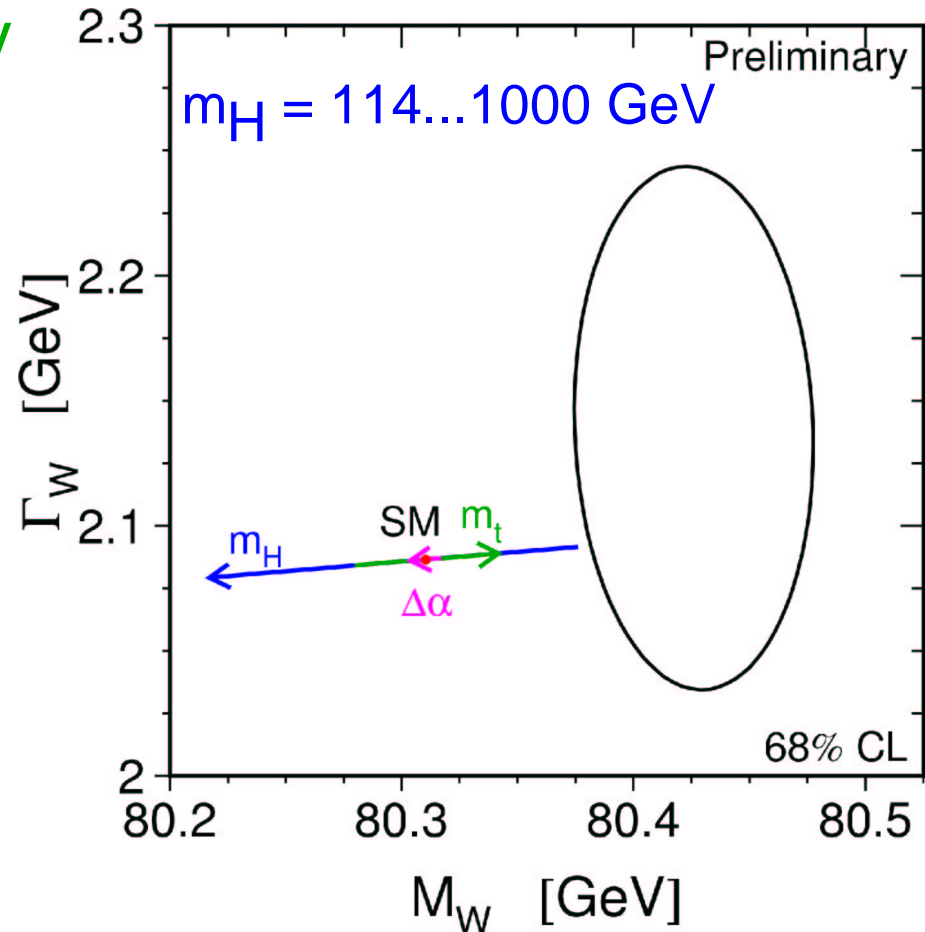
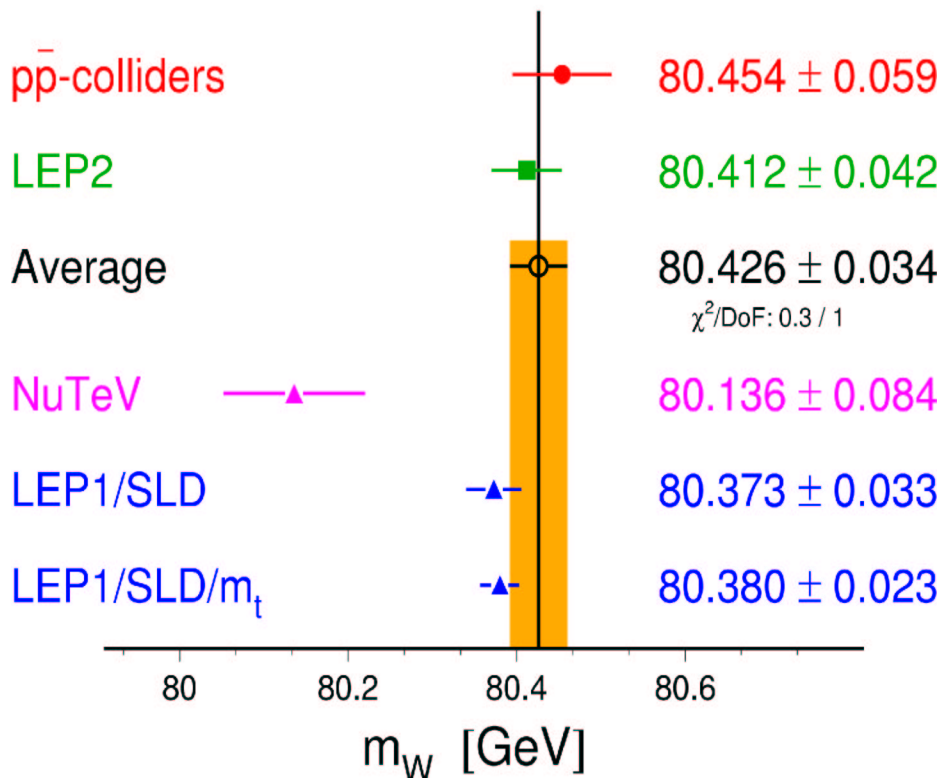
$$M_{WW}(q\bar{q}q\bar{q}) - M_{WW}(q\bar{q}l\nu) = 22 \pm 43 \text{ MeV}$$

W Boson - Mass and Width

Very good agreement between the experiments

M_W (LEP-2) reduced by 35 MeV

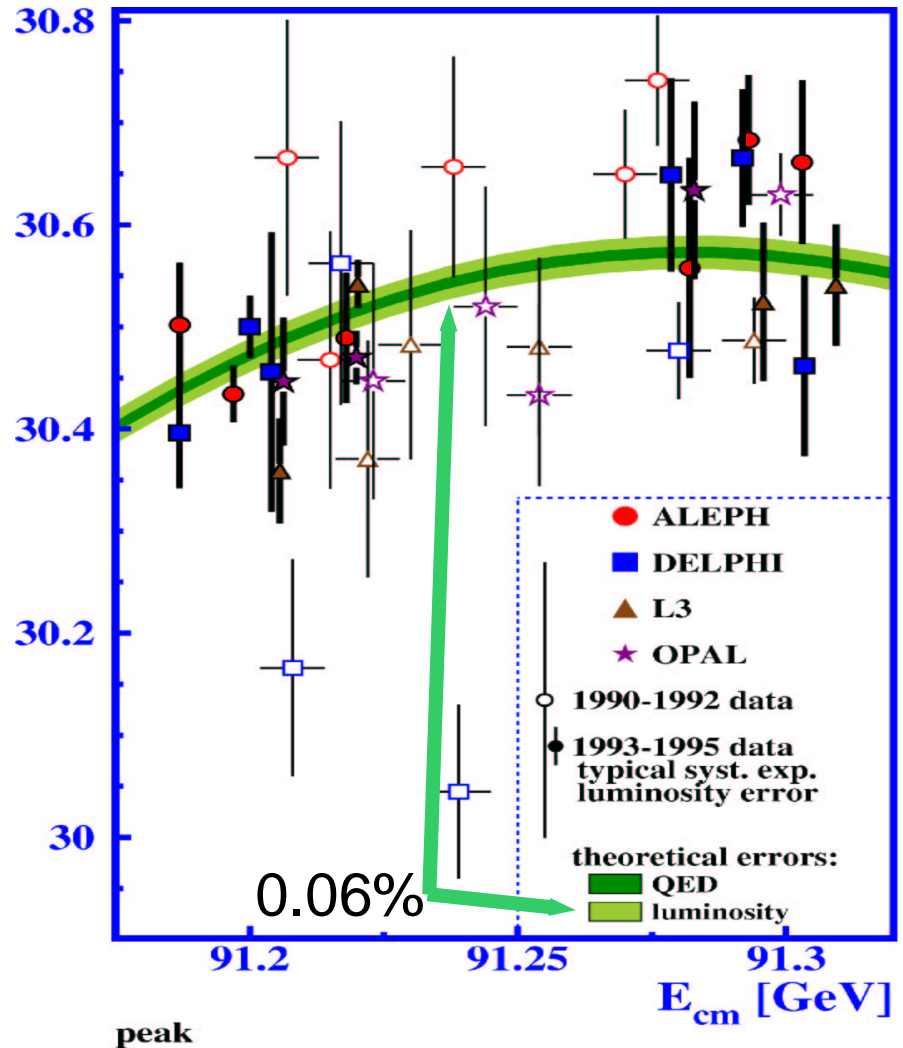
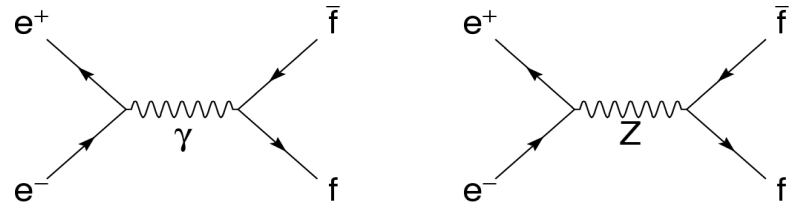
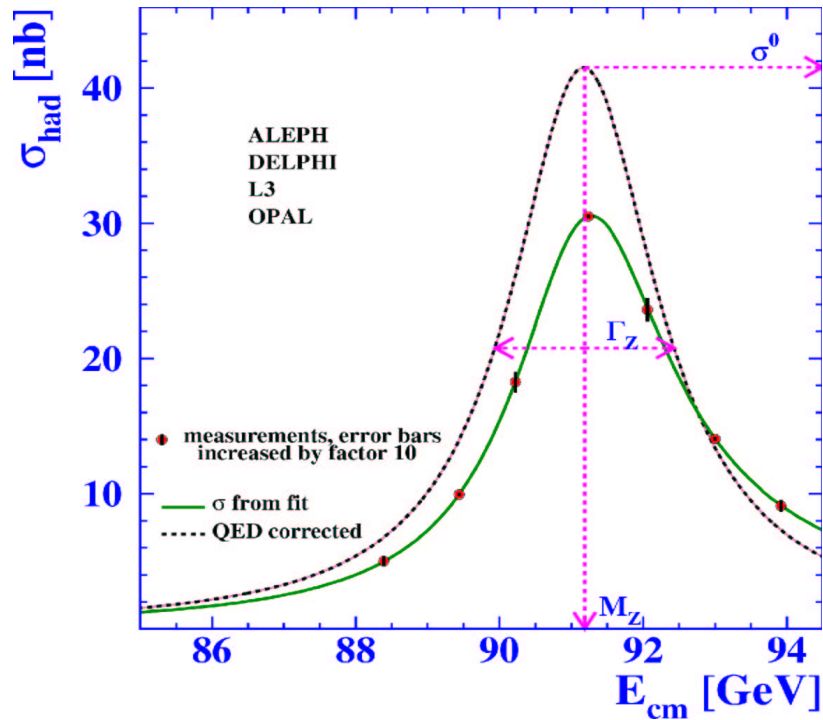
W-Boson Mass [GeV]



SM comparison:

Small Higgs-boson mass¹⁰

Z Lineshape and Leptonic F/B Asymmetries



χ^2/dof :

ALEPH: 169 / 176

DELPHI: 177 / 168

L3: 158 / 166

OPAL: 155 / 194

LEP: 36.5 / 31 (23%)

Z Lineshape and Leptonic F/B Asymmetries

Final LEP-1 results: hep-ex/0101027

$$M_Z = 91.1875 (21) \text{ GeV}$$

$$\Gamma_Z = 2.4952 (23) \text{ GeV}$$

LEP beam energy:

1.7 MeV on mass

1.2 MeV on width

$$N_\nu = 2.9841 (83)$$

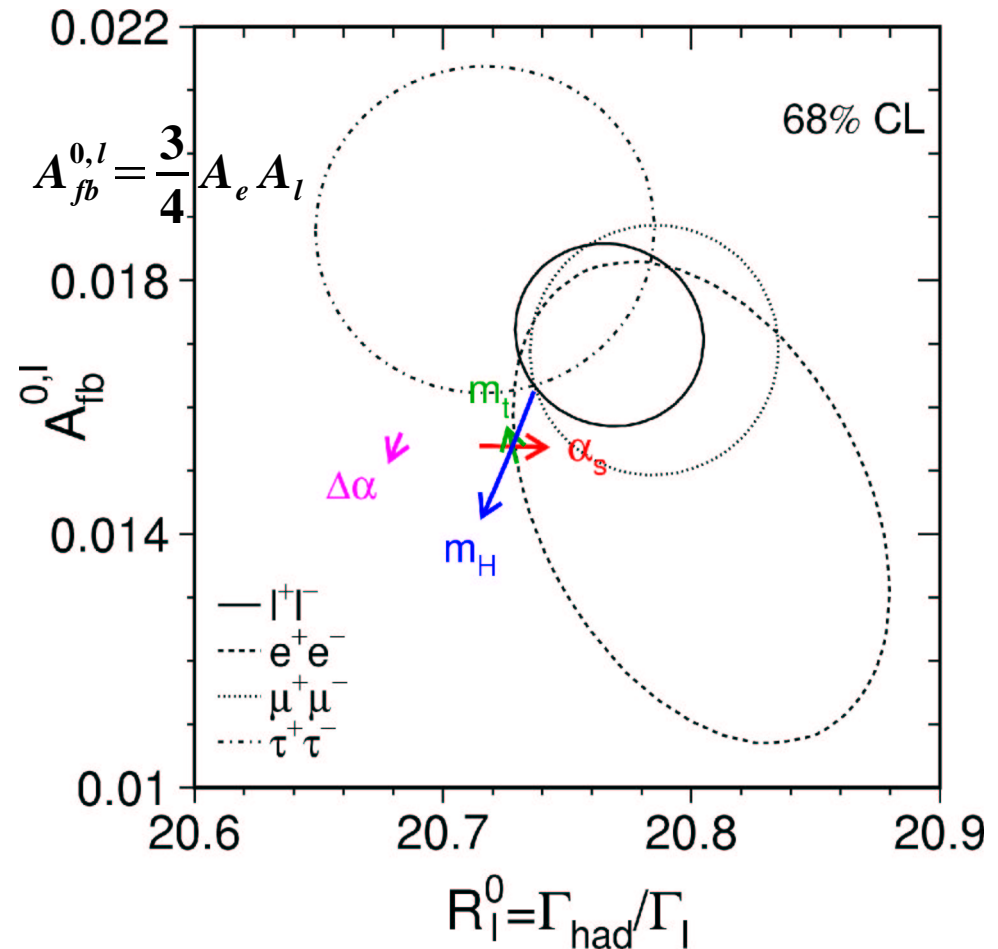
$$\delta N_\nu = 10.5 \frac{\delta N_{had}}{N_{had}} \oplus 3.0 \frac{\delta N_{lep}}{N_{lep}} \oplus 7.5 \frac{\delta L}{L}$$

Luminosity: ± 0.0046 on N_ν

Lepton universality:

$$R_l = 20.767 (25)$$

$$A_{fb}(l) = 0.0171 (10)$$



MSM prediction shown for:

$$\alpha_s = 0.118 \pm 0.002 \quad \Delta \alpha_{had} = 0.02761 \pm 0.0036$$

$$M_{top} = 174.3 \pm 5.1 \text{ GeV} \quad M_{Higgs} = 114 \dots 1000 \text{ GeV}$$

Low Higgs mass preferred!

Polarised Lepton Asymmetries

Asymmetry parameter:

$$A_f = 2 \frac{g_{Vf} / g_{Af}}{1 + (g_{Vf} / g_{Af})^2}$$

LEP-1:

Leptonic f/b asymmetry

$$A_l = 0.1512 \text{ (42)}$$

Final state τ polarisation

$$A_l = 0.1465 \text{ (33)}$$

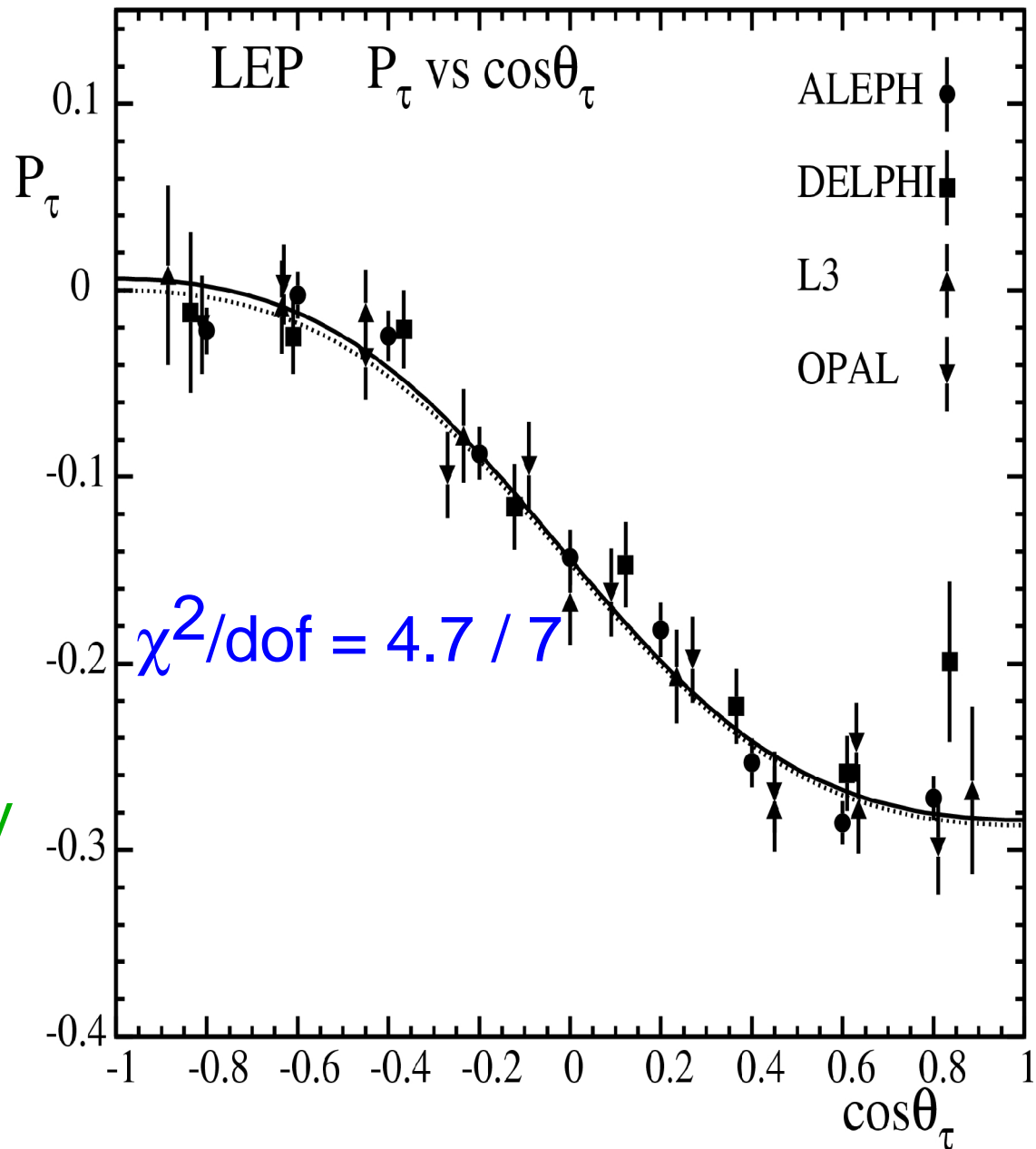
SLD:

Left/right (f/b) asymmetry

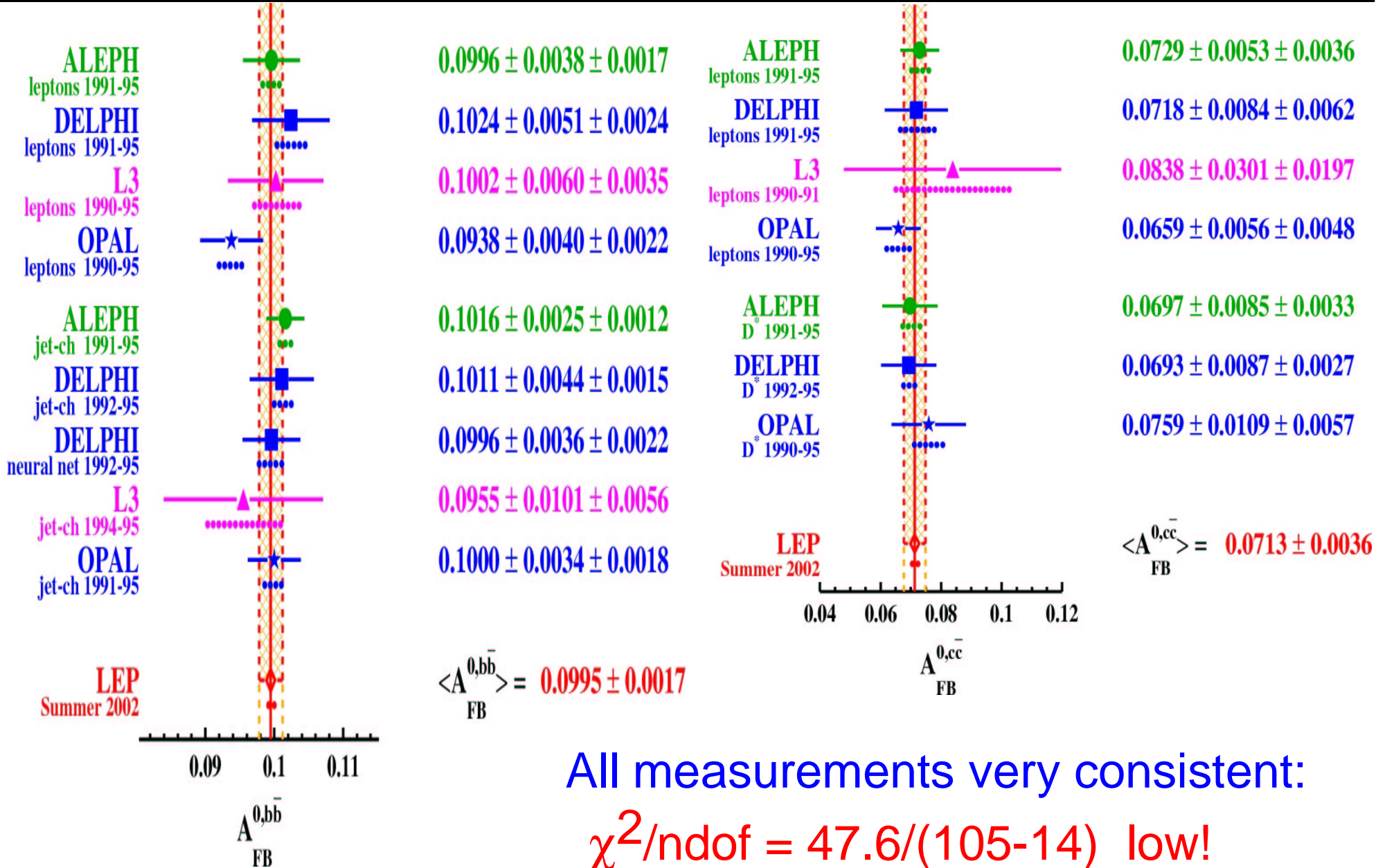
$$A_l = 0.1513 \text{ (21)}$$

Final SLD+LEP-1 result:

$$A_l = 0.1501 \text{ (16)}$$



Heavy Flavour Results at the Z Pole

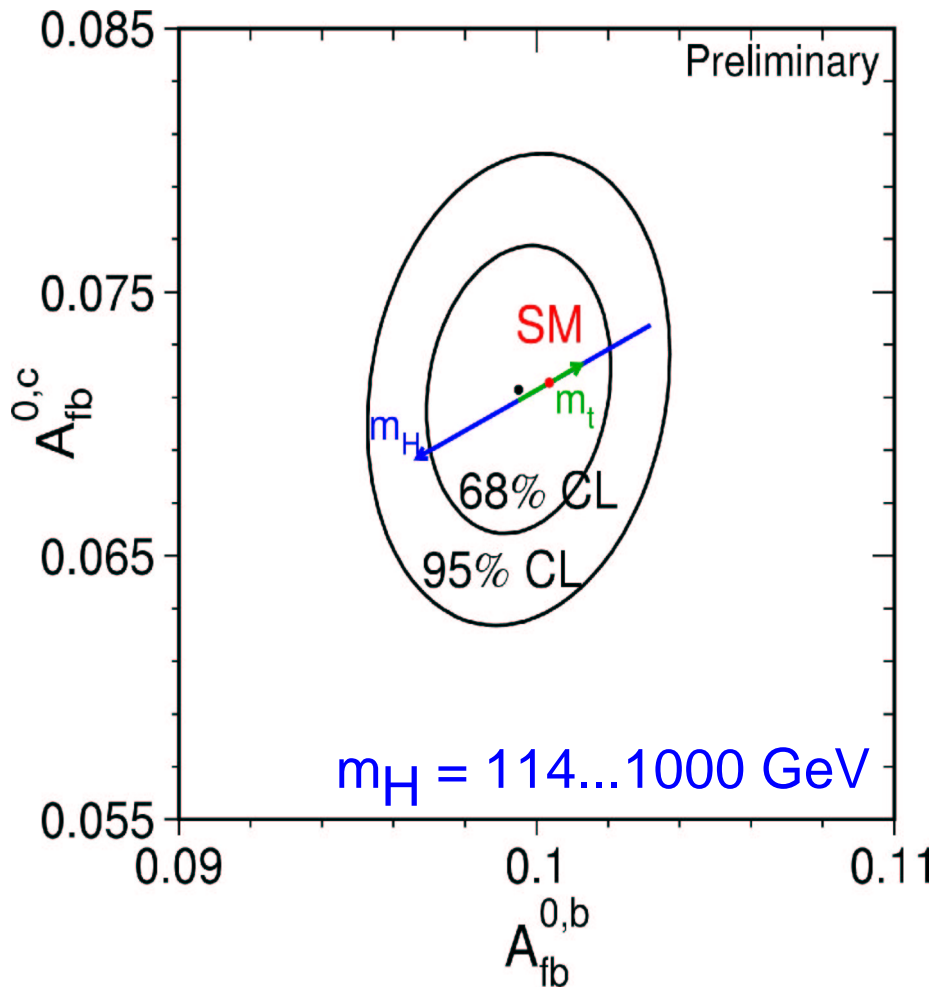


All measurements very consistent:

$$\chi^2/\text{ndof} = 47.6/(105-14) \text{ low!}$$

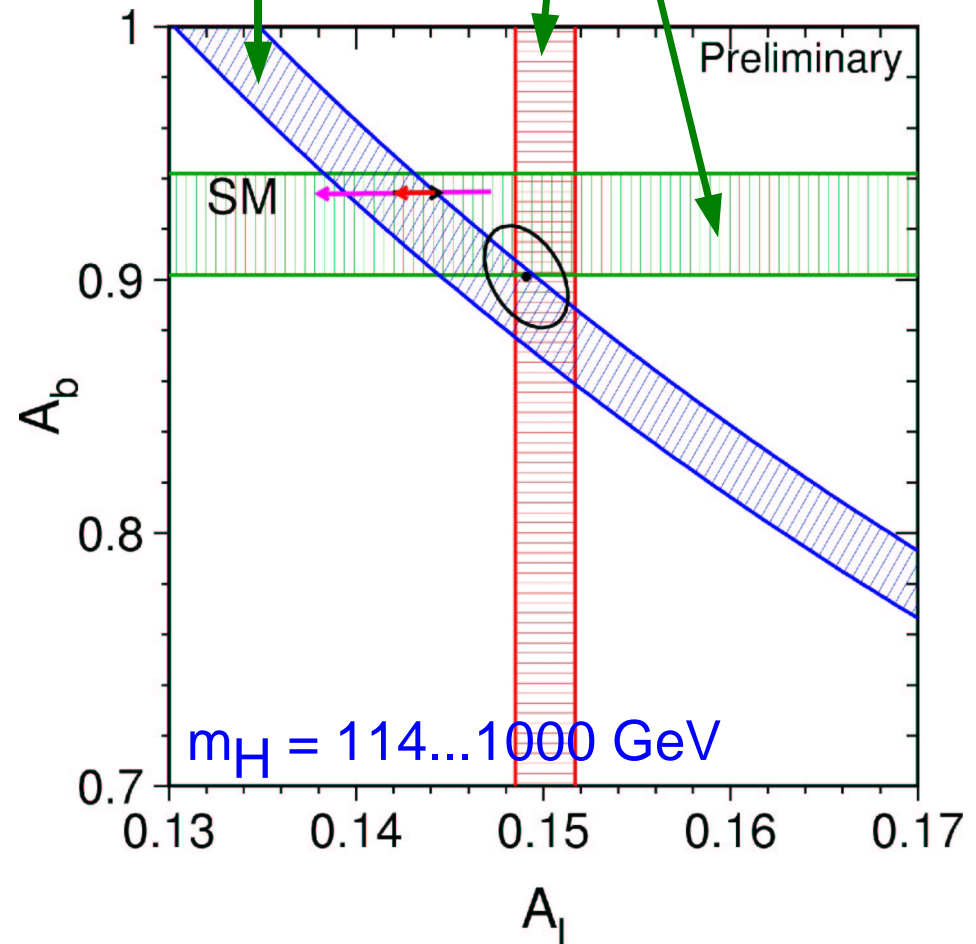
F/B asymmetries statistics dominated

Heavy Flavour Results at the Z Pole



Compare with leptons:

$$A_{fb}(b) = \frac{3}{4} A_e A_b$$



SM comparison:

Higher Higgs-boson mass

Comparison of all Z-Pole Asymmetries

Effective electroweak
mixing angle:

$$\sin^2\Theta_{\text{eff}} = 0.23148 \quad (17)$$

$$\chi^2/\text{ndof} = 10.2/5 \quad [7.0\%]$$

A-posteriori observation:

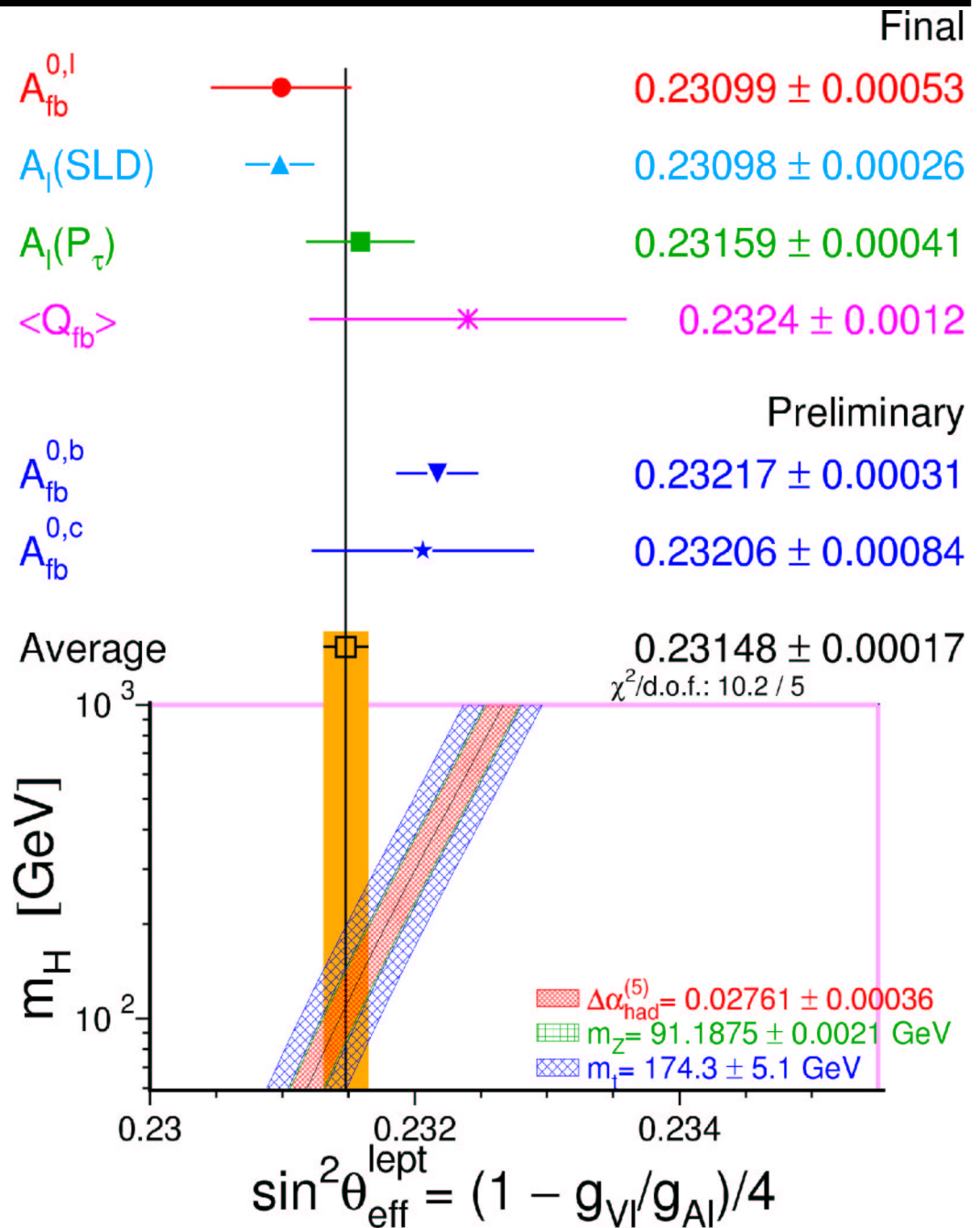
$$0.23113 \quad (21) \quad \text{leptons}$$

$$0.23217 \quad (29) \quad \text{hadrons}$$

But is really:

$$A_I(\text{SLD}) \text{ vs. } A_{\text{fb}}^b(\text{LEP})$$

Both: 2.9σ difference



Global Standard-Model Analysis

SM: Each observable calculated as a function of:

$\Delta\alpha_{\text{had}}, \alpha_s(M_Z), M_Z, M_{\text{top}}, M_{\text{Higgs}}$ (and G_F)

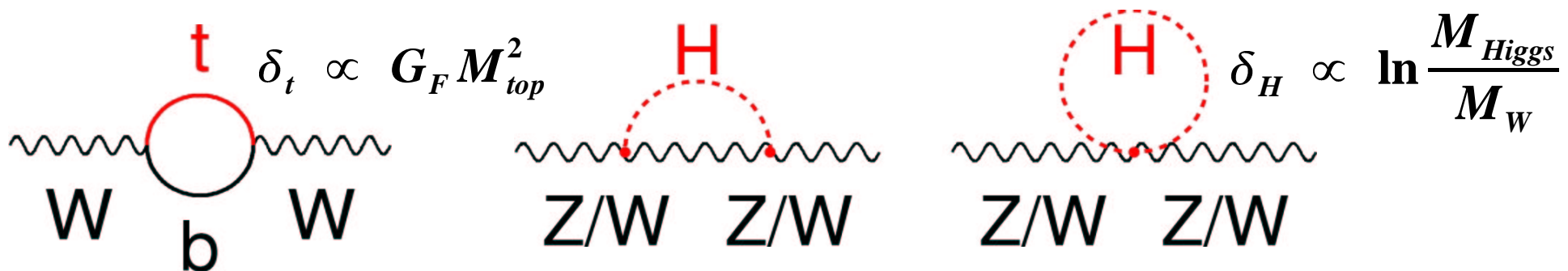
$\Delta\alpha_{\text{had}}$: hadronic vacuum polarisation [0.02761(36)]

$\alpha_s(M_Z)$: given by Γ_{had} and related observables

M_Z : constrained by LEP-1 lineshape

Precision requires 1st and 2nd order electroweak and mixed radiative correction calculations (QED to 3rd)

$M_{\text{top}}, M_{\text{Higgs}}$ enter through electroweak corrections!



Calculations by programs TOPAZ0 and ZFITTER

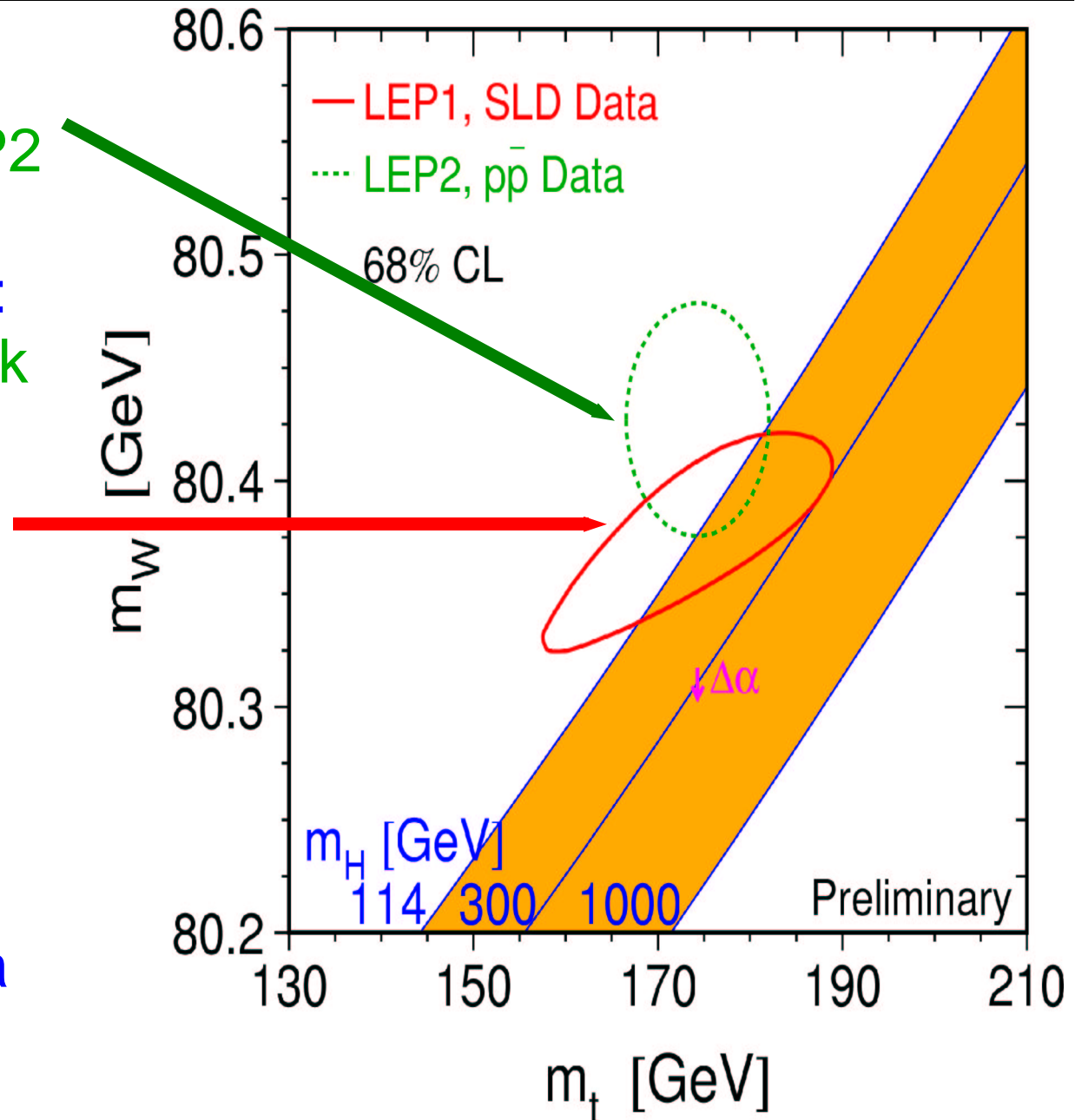
Heavy Particle Masses W and Top

Direct measurements:
TEVATRON and LEP2

Z-Pole measurements:
Constrain electroweak
radiative corrections
Allows to predict M_W
and M_{top} within SM

Now good agreement
Successful SM test

Both data sets prefer a
light Higgs boson



Global Standard-Model Analysis



Fit to all data:

$$\chi^2/\text{ndof} = 25.5/15 \text{ (4.4\%)}$$

Largest χ^2 contribution:

$$\sin^2\theta_W(\text{NuTeV}, \rho = \rho_{\text{SM}})$$

Spread of $\sin^2\theta_{\text{eff}} \rightarrow A_{\text{fb}}(b)$

Fit without NuTeV:

$$\chi^2/\text{ndof} = 16.7/14 \text{ (27.3\%)}$$

Fit result is robust:

Fitted parameters
almost unchanged!

Constraints on the SM Higgs-Boson Mass

$$M_{\text{Higgs}} = 91^{+58}_{-37} \text{ GeV}$$

Incl. theory uncertainty:

$$M_{\text{Higgs}} < 211 \text{ GeV (95\%CL)}$$

Strongly correlated:

-0.5 (-0.2) with fitted $\Delta\alpha_{\text{had}}$

+0.7 with fitted M_{top}

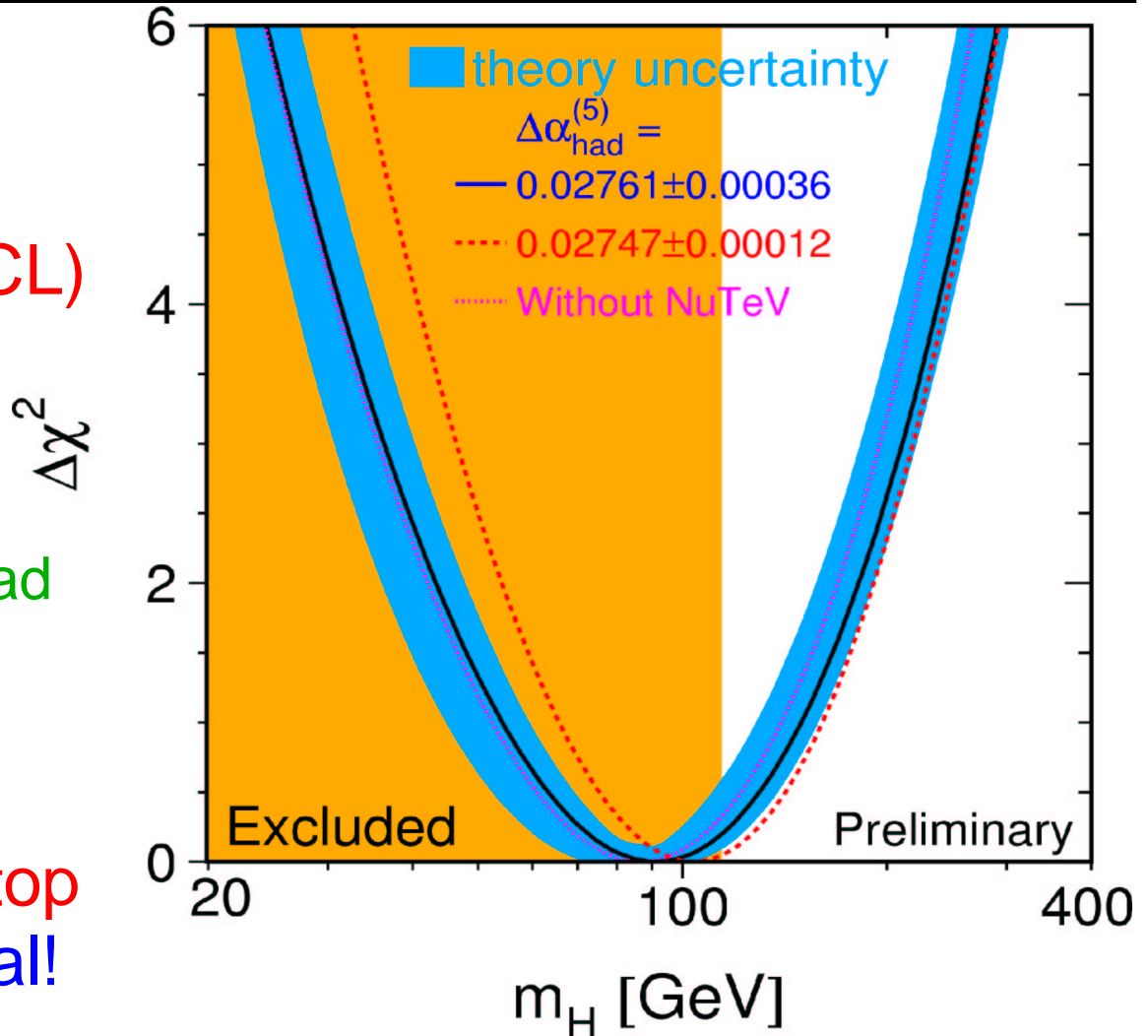
35% shift in M_{Higgs} for

5 GeV shift in meas. M_{top}

M_{top} measurement crucial!

Direct Higgs search limit:

No contradiction!

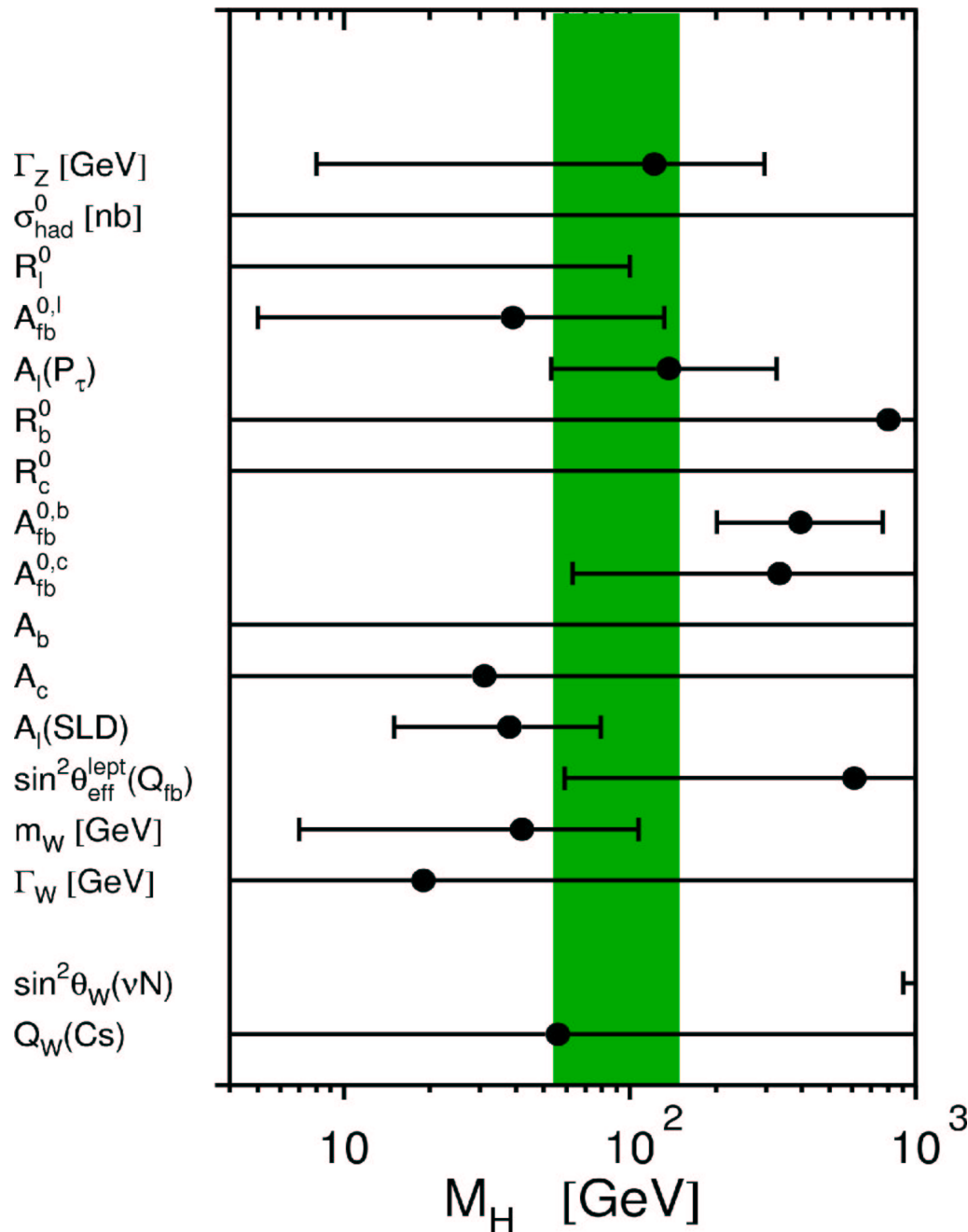


Theory uncertainty:

Need two-loop

calculations for $\sin^2\Theta_{\text{eff}}^{20}$

Higgs Mass from each Observable



For each observable:

Fit for M_{Higgs} with the constraints:

$$\Delta\alpha_{had} = 0.02761(36)$$

$$\alpha_s(M_Z) = 0.118(2)$$

$$M_Z = 91187.5(2.1) \text{ MeV}$$

$$M_{top} = 174.3(5.1) \text{ GeV}$$

Meaningful?

Caveats

Real Higgs-Strahlung (Z^*+H) not taken into account:

Experimental analyses:

Higgs-mass dependent effects in cross sections and asymmetries

Calculation of predictions:

Total Z decay width increases

Cross sections and asymmetries change (2f vs. 4f)

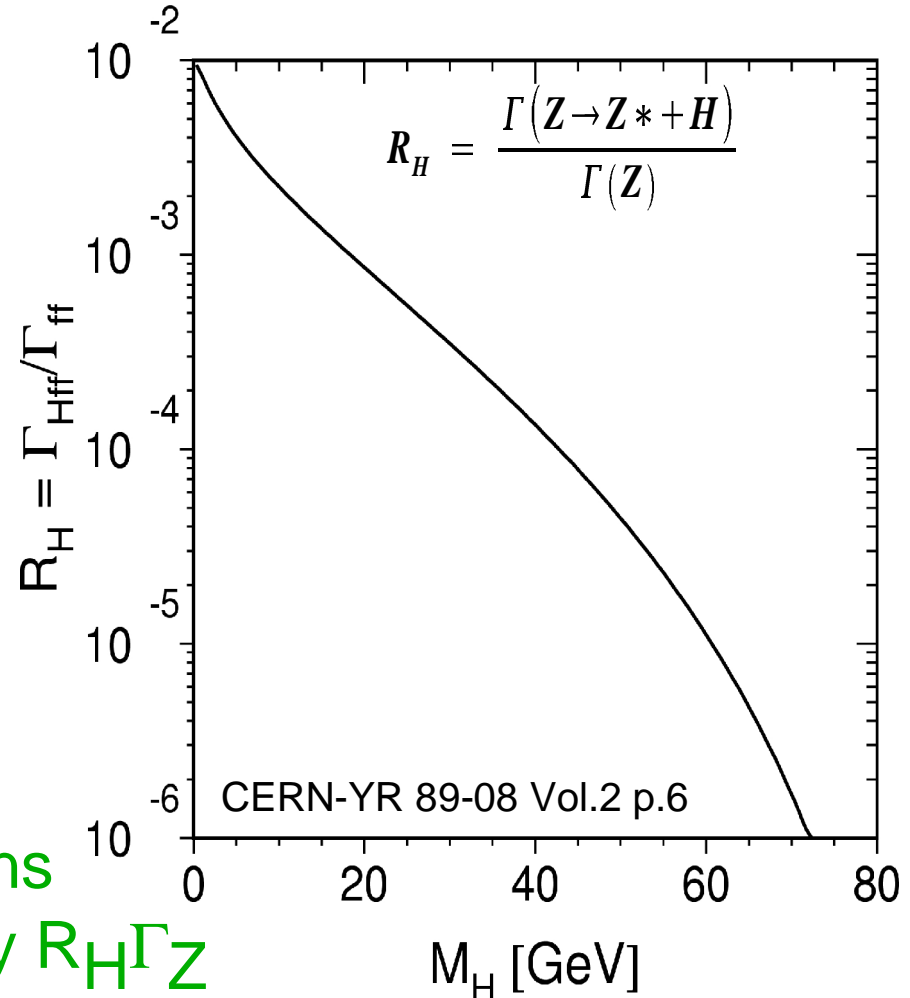
Simple considerations at the Z-pole:

All Z^*+H decays selected as hadrons

Measured Γ_Z and Γ_{had} increase by $R_H \Gamma_Z$

Increase of fitted α_S in SM fit neglecting Z^*+H

$\Delta\alpha_S = 4R_H$ | $\Delta\alpha_S < 0.1\delta\alpha_S \Rightarrow M_H > 22 \text{ GeV}$ is required



Caveats

What about heavy-flavour widths and f/b asymmetries?

Maximal effect if all Z^*H decays are tagged as b-production

Γ_b increased by the same amount as Γ_{had} , $A_{fb}(b)$ changed

$\Delta R_b = 1.1R_H$ | $|\Delta R_b| < 0.1\delta R_b \Rightarrow M_H > 47 \text{ GeV}$ is required

W mass reconstruction probably not affected

Z^*+H also dependent on centre-of-mass energy!

SM global fit ok for M_H central value and upper errors

Quantitative statements in low Higgs-mass regime dubious

Correct treatment requires experimental efficiencies and corrections for Z^*+H as a function of M_H

Not available!

But have limit from direct search $M_H > 114.4 \text{ GeV}$ (95% CL)

Conclusions

Wealth of high-precision measurements:

Many with high sensitivity to radiative corrections

Most measurements agree with expectations:

Successful test of SM loop corrections

But have two ~ 3 -sigma effects:

Spread in $\sin^2\Theta_{\text{eff}} \rightarrow A_{\text{fb}}(b)$, and NuTeV's R_- result

Validity of any pseudo-observable analysis: Real Higgs production or non-MSM final states must be negligible

Future:

Precise theoretical calculations - incl. theor. uncertainties

Improved measurements of top , W , $\Delta\alpha_{\text{had}}$, $\sin^2\Theta_{\text{eff}}$

Check Higgs-mass prediction