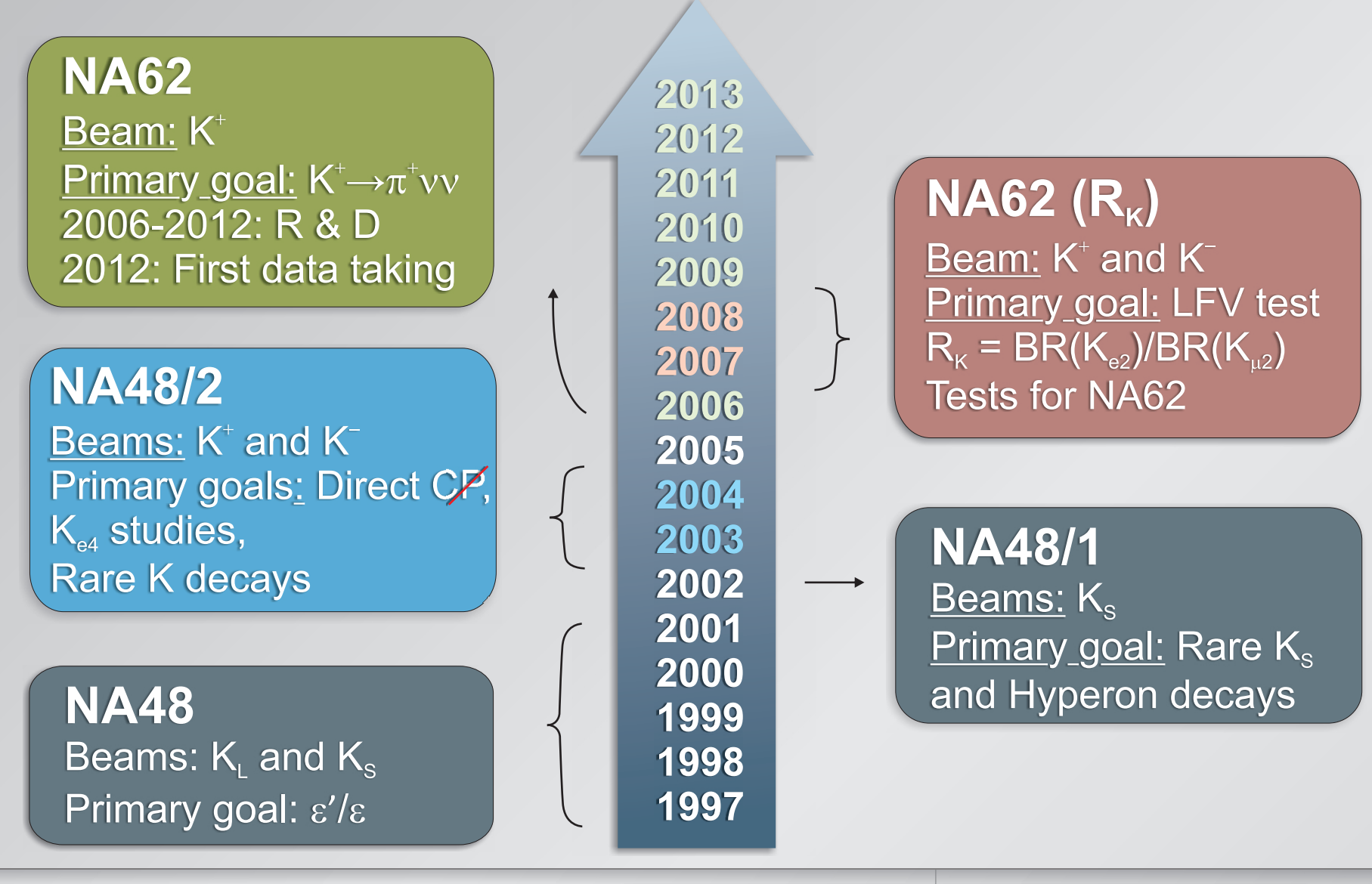


# TEST OF CHIRAL PERTURBATION THEORY

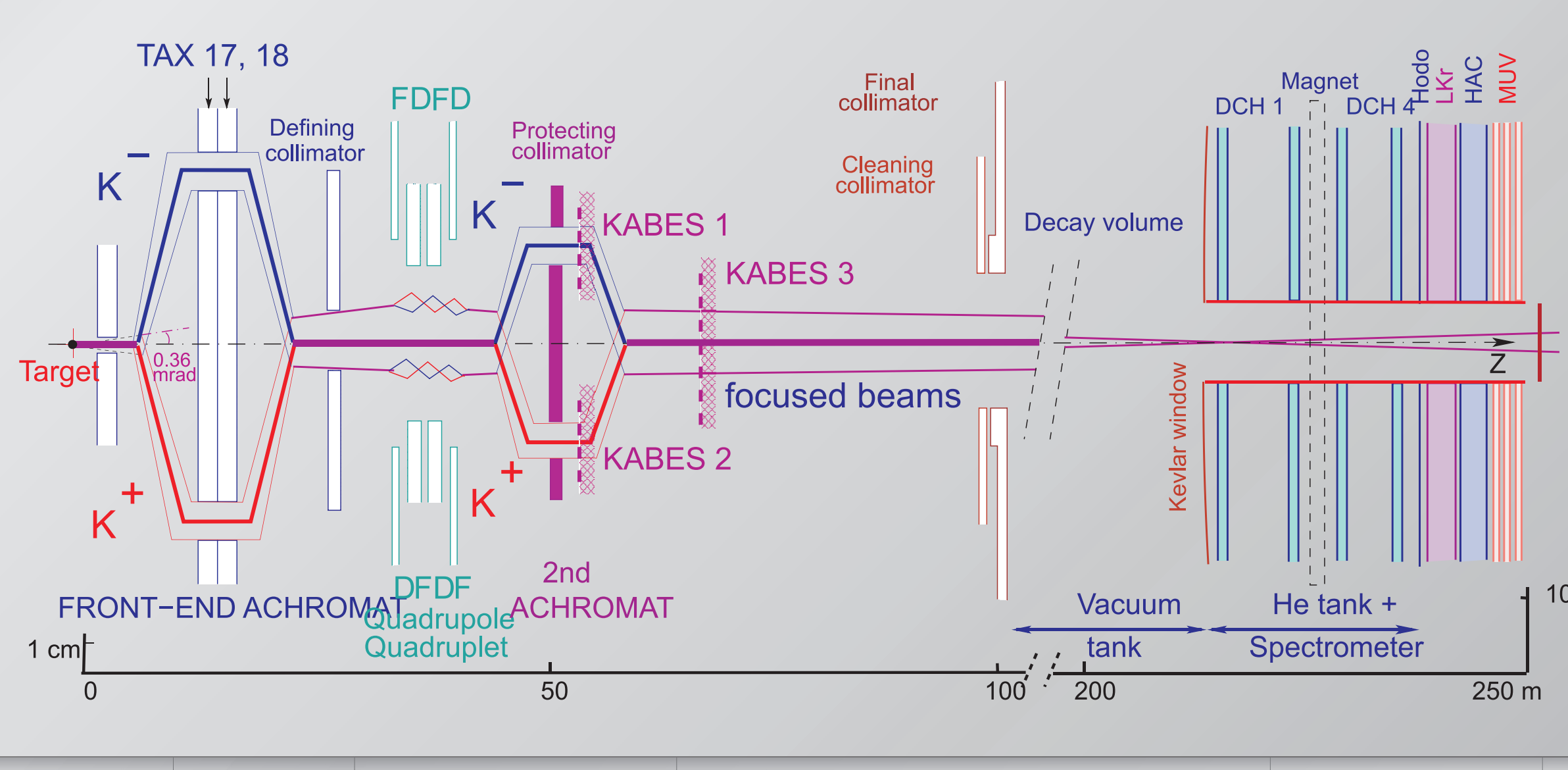
## WITH $K_{e4}^{+-}$ AND $K_{e4}^{00}$ DECAYS AT NA48/2

Cambridge, CERN, Chicago, Dubna, Edinburgh, Ferrara, Florence, Mainz, Northwestern, Perugia, Pisa, Saclay, Siegen, Turin, Vienna

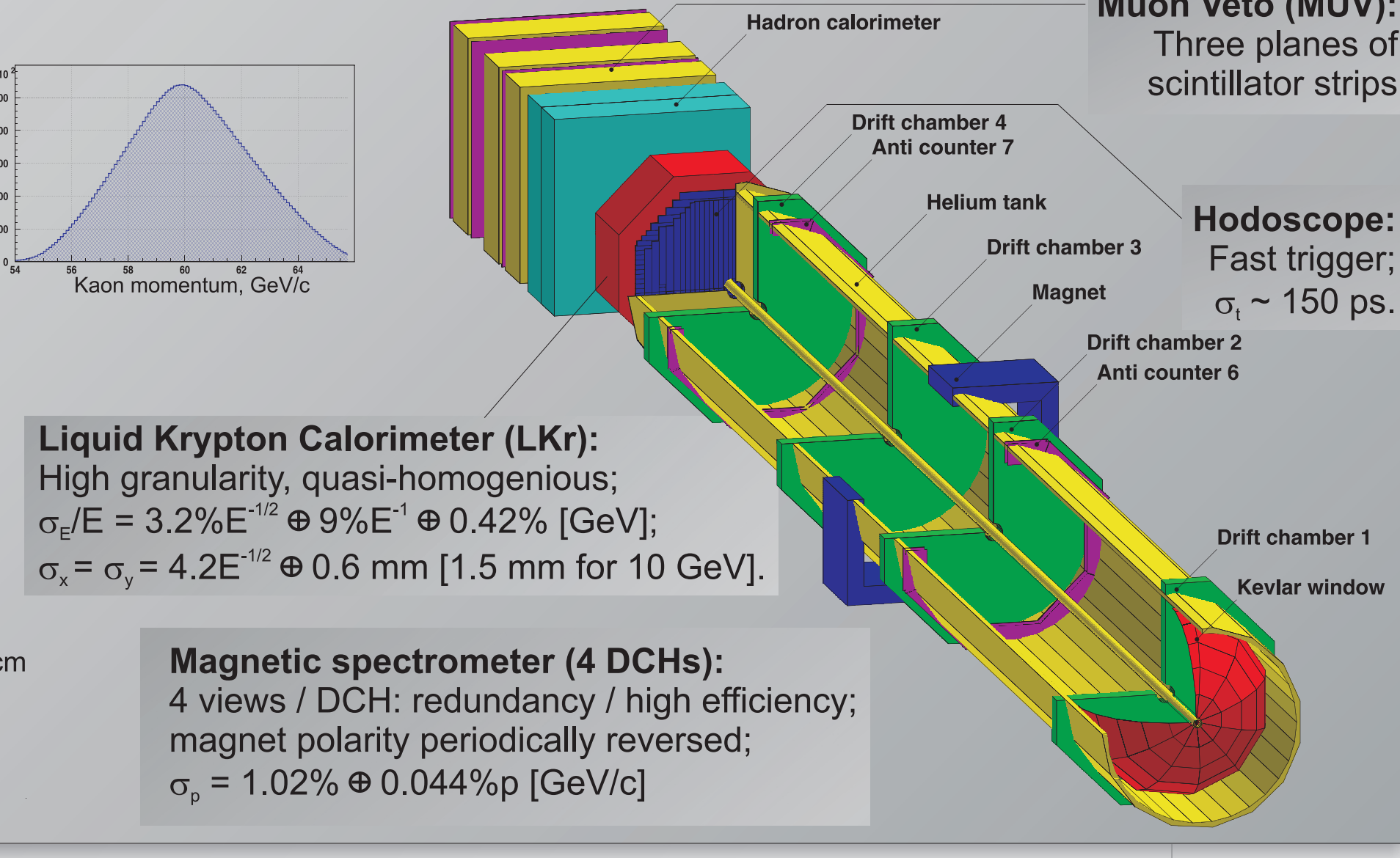
### TIMELINE OF NA48/NA62 EXPERIMENTS



### NA48/2 BEAM LINE SCHEMATICS

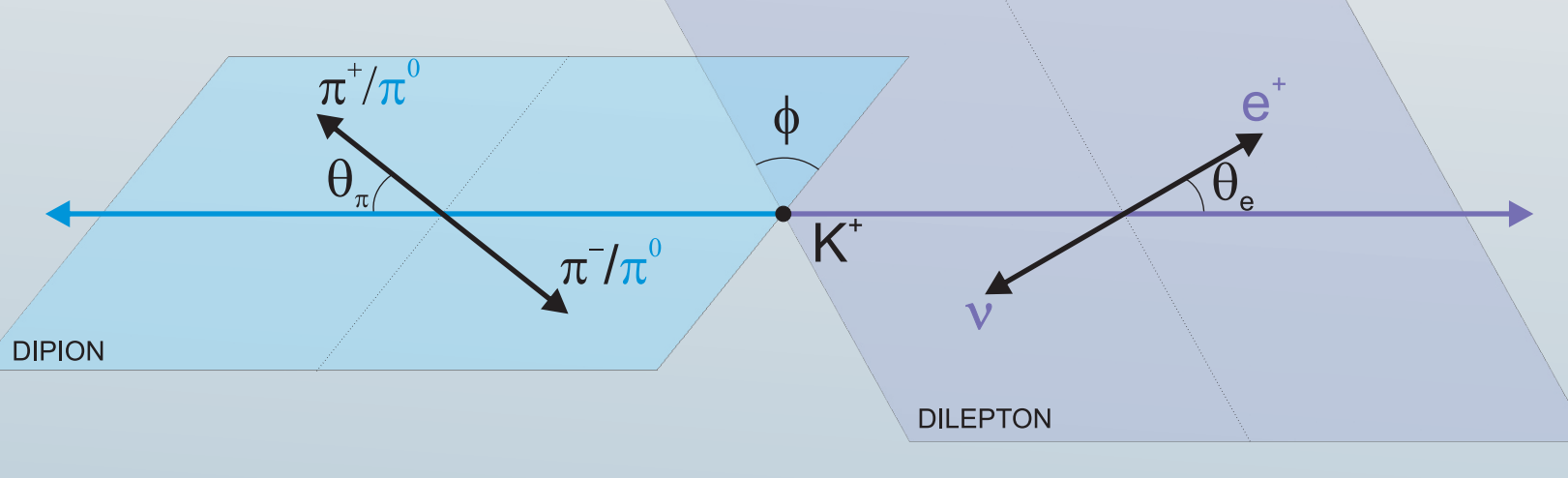


### NA48/2 DETECTOR SETUP



### FORMALISM OF $K_{e4}^{+-}$ AND $K_{e4}^{00}$ DECAYS

Four body final state, described by five kinematic variables:  $S_\pi (M_\pi^2)$ ,  $S_e (M_e^2)$ ,  $\cos\theta_\pi$ ,  $\cos\theta_e$ ,  $\phi$  (Cabibbo-Maksymowicz 1965). In  $K_{e4}^{00}$  case reduced to 3 variables:  $S_\pi (M_\pi^2)$ ,  $S_e (M_e^2)$ ,  $\cos\theta_e$ .



Partial wave expansion of the amplitude into s- and p- waves (Pais-Treiman 1968):

2 complex axial form factors:  $F = F_s e^{i\delta_s} + F_p e^{i\delta_p} \cos\theta_\pi$  and  $G = G_p e^{i\delta_p}$   
 1 complex vector form factor:  $H = H_p e^{i\delta_p}$

Expansion in  $q^2$  and  $S_i$ :  
 $F_S = f_s + f'_s q^2 + f''_s q^4 + f_s (S_e / 4m_\pi^2) + \dots$   
 $F_P = f_p + f'_p q^2 + \dots$   
 $G_P = g_p + g'_p q^2 + \dots$   
 $H_P = h_p + h'_p q^2 + \dots$

In  $K_{e4}^{00}$  case: single form factor  $F_s$ . Dalitz plot density proportional to  $F_s^2$ .

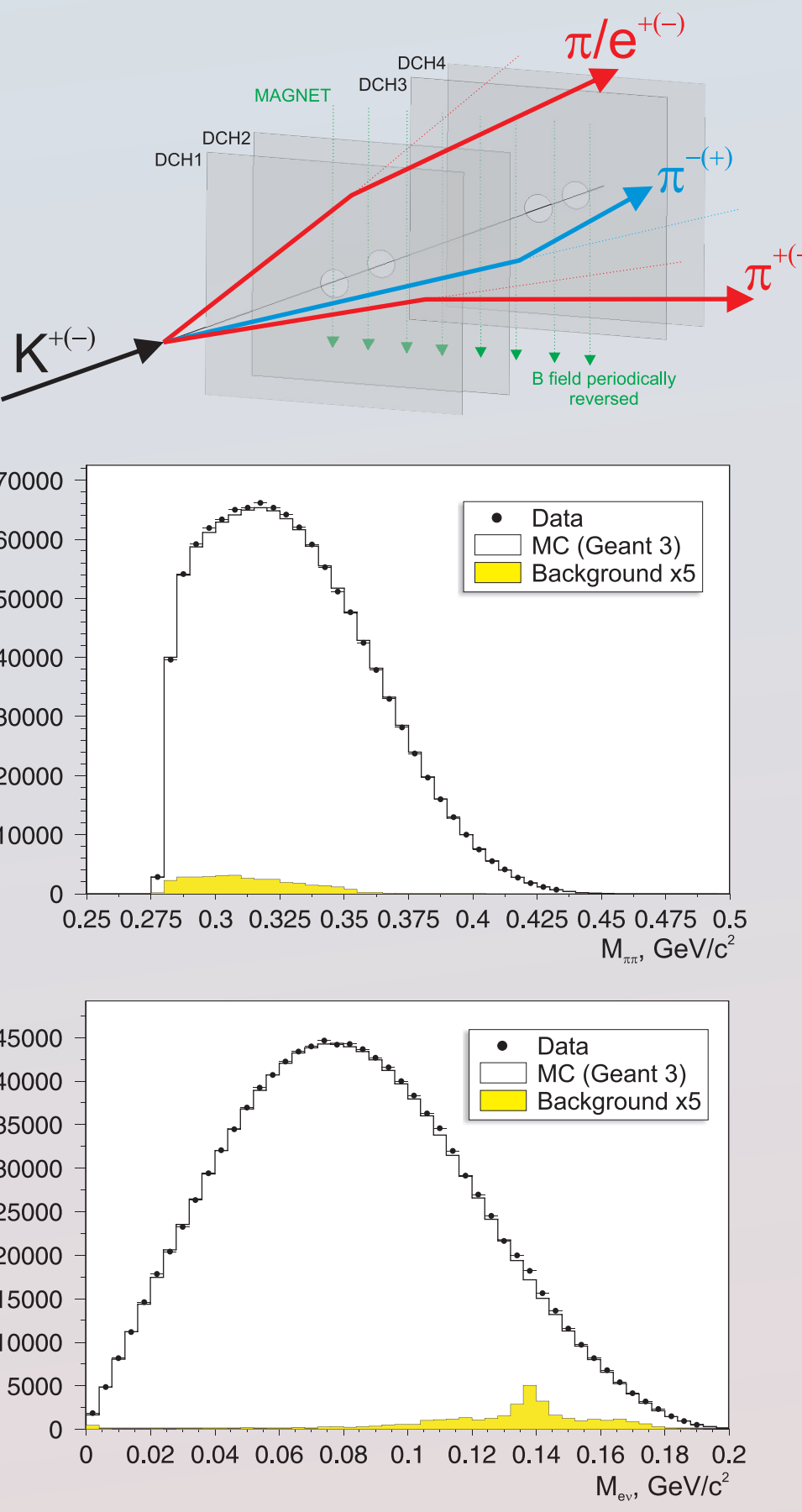
Isospin symmetry translates in relations between decay modes:  
 $\Gamma(K_{e4}^+) = 0.5 \times \Gamma(K_{e4}^{0+}) + 2 \times \Gamma(K_{e4}^{00})$  (for  $l=e,\mu$ )

**Experimental status (PDG 2010):**  
 $BR(K_{e4}^+) = (4.09 \pm 0.10) \times 10^{-5}$  (2.4%)  
 $BR(K_{e4}^{0+}) = (2.20 \pm 0.40) \times 10^{-5}$  (18.2%)  
 $BR(K_{e4}^{00}) = (5.20 \pm 0.11) \times 10^{-5}$  (2.1%)

**Predictions using FF by  $\chi$ PT at  $O(p^2, p^4, p^6)$ :**  
 $BR(K_{e4}^+) = (3.91 \pm 0.17) \times 10^{-5}$   
 $BR(K_{e4}^{0+}) = (2.01 \pm 0.11) \times 10^{-5}$   
 $BR(K_{e4}^{00}) = (4.69 \pm 0.87) \times 10^{-5}$

Improved measurements will provide tests of  $\chi$ PT predictions.

### $K_{e4}^{+-}$ SELECTION AND RECONSTRUCTION



Decay mode for normalization:  $K^+ \rightarrow \pi^+ \pi^+ \pi^-$   
 Reconstruction and selection as close as possible: Require 3 tracks, reconstructed by the magnetic spectrometer, forming a vertex within the decay volume. No MUV hit associated with tracks.

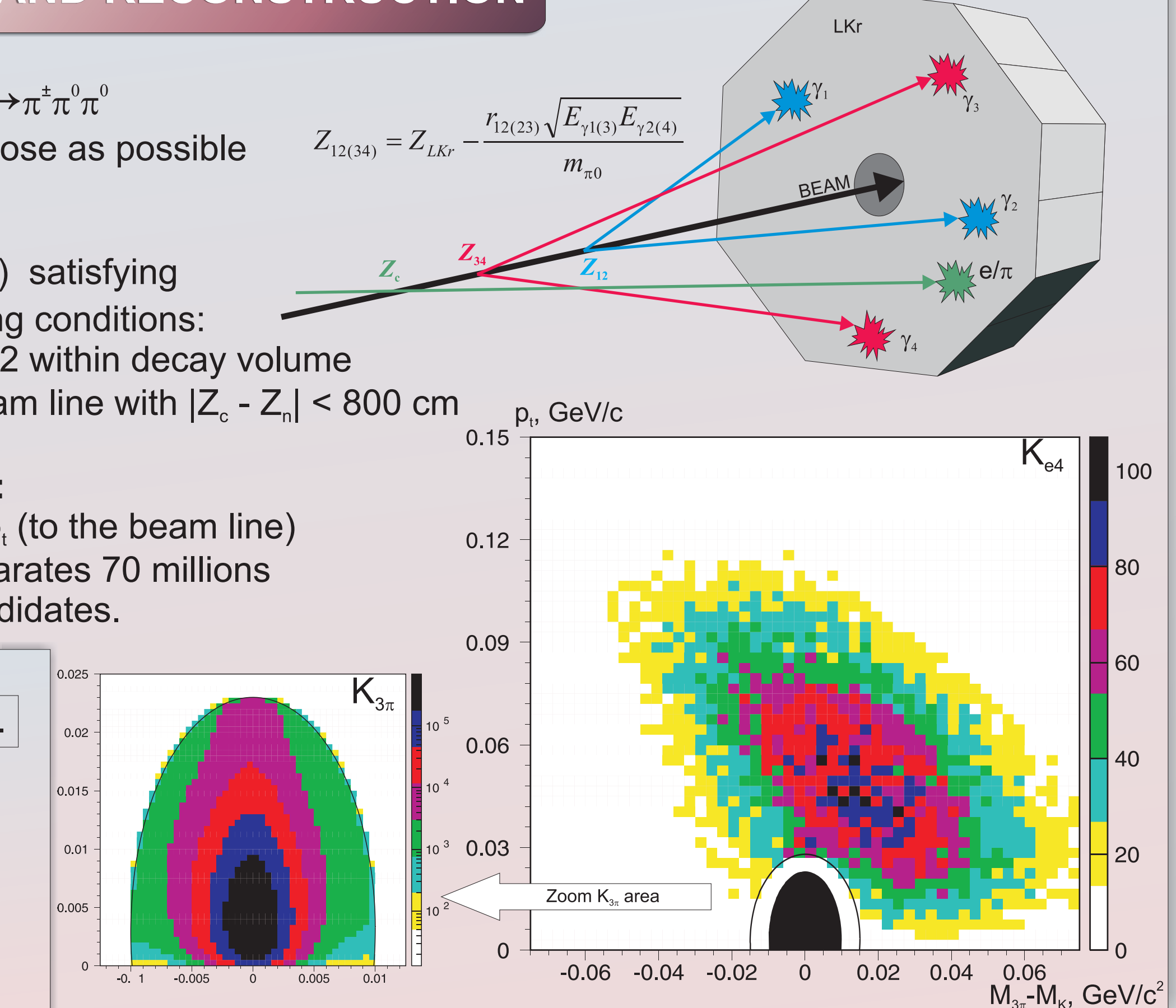
**Background suppression cuts:**  
 1) Against  $\pi^+ \pi^+ \pi^-$ : compute the 3-track invariant mass in three-pion hypothesis ( $m_{3\pi}$ ); make ellipse cut in ( $m_{3\pi}$ ,  $p_\parallel$ ) space.  
 2) Against Dalitz decays: assign  $m_{03}$  to other sign pion and calculate  $e^+ e^-$  invariant mass; cut at  $m_{ee} > 0.03 \text{ GeV}/c^2$ .  
 3) Cut on missing mass of the same sign pion against  $\pi^+ \pi^0 \pi^0$  and  $\pi^+ \pi^-$ .

**Reconstruction of  $K_{e4}$ :**  
 Impose  $m_K$  and  $m_\pi=0$  and find the two solutions for Kaon momentum. Pick the closest to the nominal beam momentum (60 GeV/c).

**Background estimation:**  
 Count "wrong sign" events:  $e^+ \pi^+ \pi^+$  (suppressed due to  $\Delta S = \Delta Q$  to  $10^{-6}$ ). Background = 2 x WS

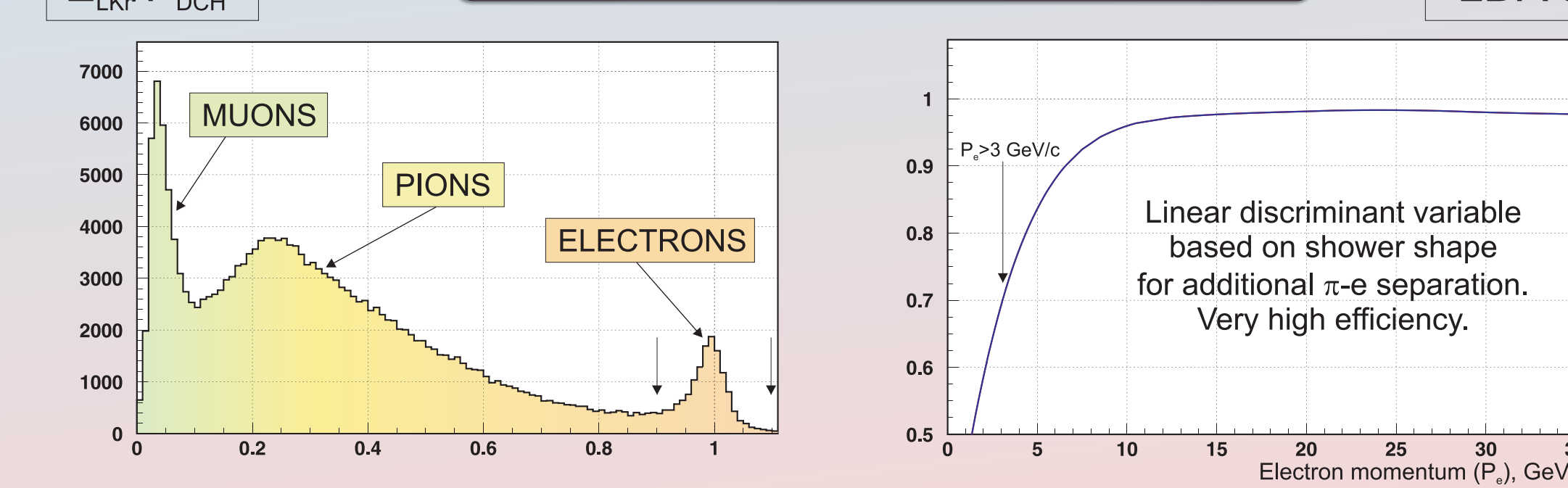
### $K_{e4}^{00}$ SELECTION AND RECONSTRUCTION

Decay mode for normalization:  $K^+ \rightarrow \pi^+ \pi^0 \pi^0$   
 Reconstruction and selection as close as possible for both modes.  
 Find 2 clusters pairs ( $\gamma_1 \gamma_2$ ) and ( $\gamma_3 \gamma_4$ ) satisfying  $\pi^0$  mass constraint and the following conditions:  
 $|Z_{12} - Z_{34}| < 500 \text{ cm}$ ;  $Z_n = (Z_{12} + Z_{34})/2$  within decay volume  
 $Z_c$  - at CDA of charged track to beam line with  $|Z_c - Z_n| < 800 \text{ cm}$



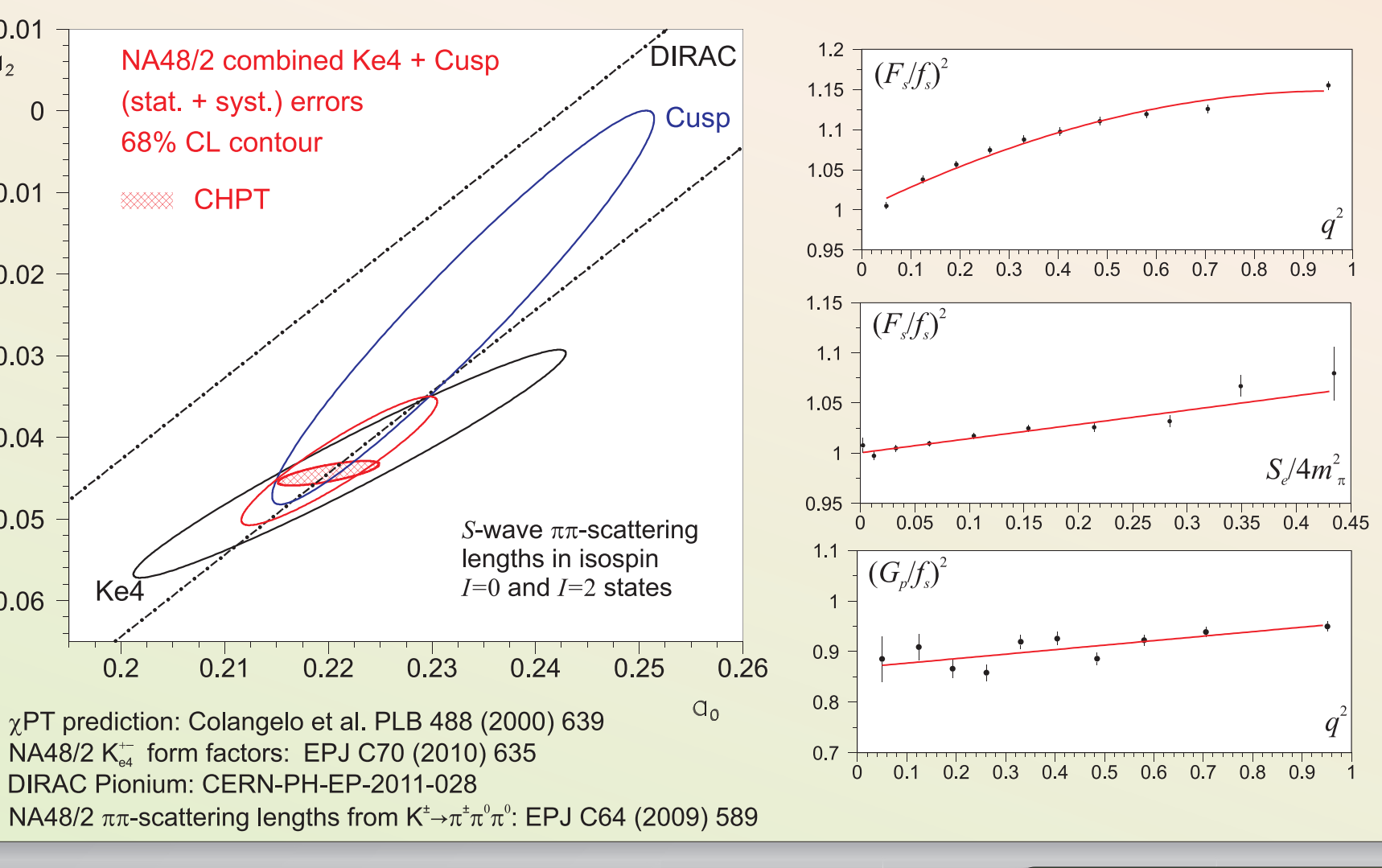
**Signal / Background separation:**  
 Compute the invariant mass and  $p_\parallel$  (to the beam line) in pion hypothesis. Elliptic cut separates 70 millions  $K_{3\pi}$  candidates from 45000  $K_{e4}$  candidates.

### PARTICLE IDENTIFICATION



### $K_{e4}^{+-}$ FORM FACTORS / FINAL

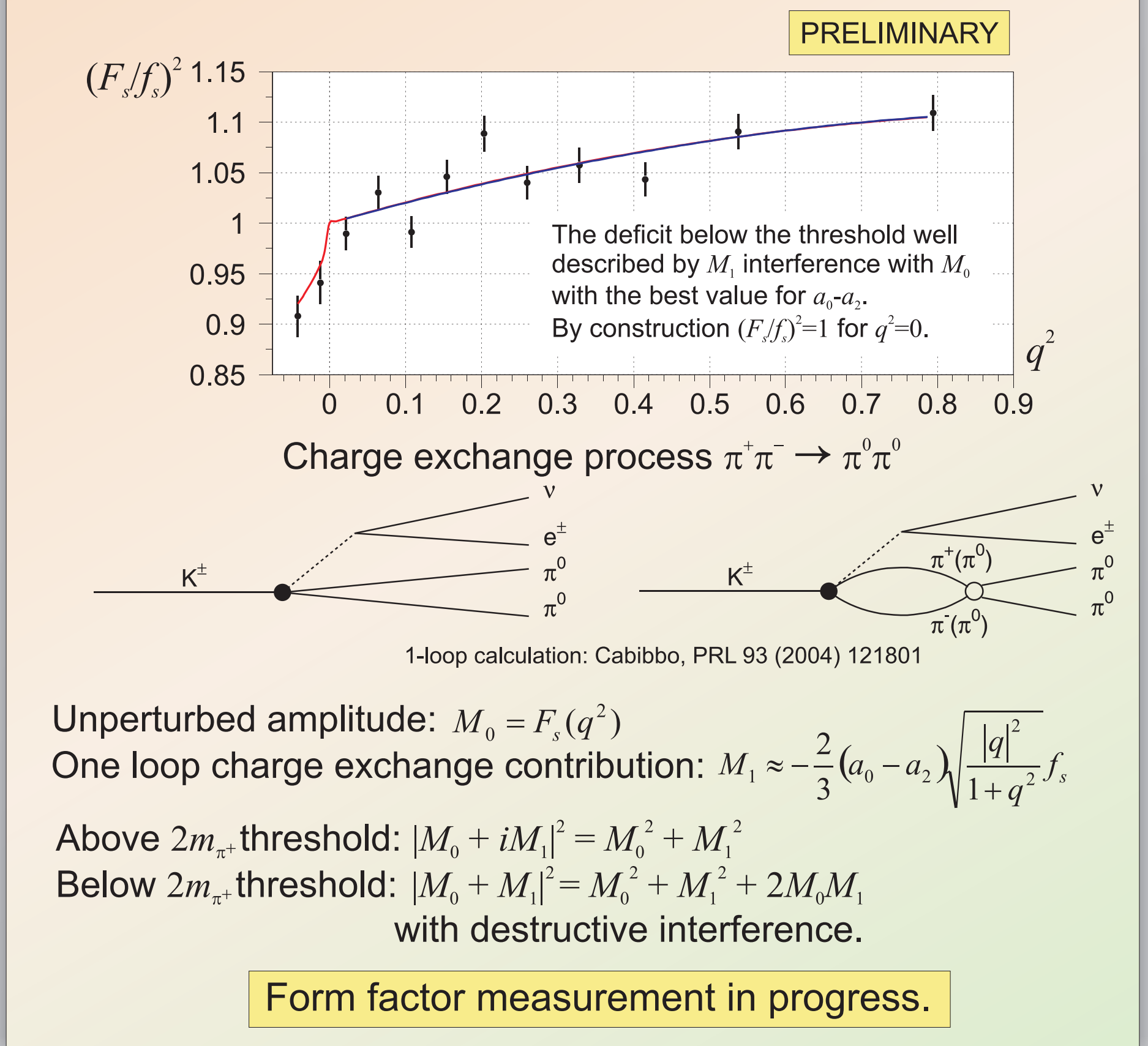
$f'_s/f_s$	$= 0.152 \pm 0.007_{\text{stat}} \pm 0.005_{\text{syst}}$
$f''_s/f_s$	$= -0.073 \pm 0.007_{\text{stat}} \pm 0.006_{\text{syst}}$
$f'_e/f_s$	$= 0.068 \pm 0.006_{\text{stat}} \pm 0.007_{\text{syst}}$
$f_p/f_s$	$= -0.048 \pm 0.003_{\text{stat}} \pm 0.004_{\text{syst}}$
$g_p/f_s$	$= 0.868 \pm 0.010_{\text{stat}} \pm 0.010_{\text{syst}}$
$g'_p/f_s$	$= 0.089 \pm 0.017_{\text{stat}} \pm 0.013_{\text{syst}}$
$h_p/f_s$	$= -0.398 \pm 0.015_{\text{stat}} \pm 0.008_{\text{syst}}$



$$BR(K_{e4}) = \frac{N_4 - N_{BG}}{N_3} \times \frac{A_3}{A_4} \times \frac{\epsilon_3}{\epsilon_4} \times BR(K_{3\pi})$$

BR( $K_{e4}^{+-}$ )	QUANTITY	BR( $K_{e4}^{00}$ )
$1.11 \times 10^6$	$N_4 = K_{e4}$ candidates	44 909
0.95% of $K_{e4}$	$N_{BG} =$ Background to $K_{e4}$	1.3% of $K_{e4}$
$1.9 \times 10^9$ ( $\pi^+ \pi^+ \pi^-$ )	$N_3 = K_{3\pi}$ candidates	( $\pi^+ \pi^0 \pi^0$ ) $70.9 \times 10^6$
18.22%	$A_4 =$ Acceptance for $K_{e4}$	1.77%
24.18%	$A_3 =$ Acceptance for $K_{3\pi}$	4.11%
98.3%	$\epsilon_4 =$ Trigger efficiency for $K_{e4}$	92% - 98%
97.5%	$\epsilon_3 =$ Trigger efficiency for $K_{3\pi}$	92% - 98%
$(5.59 \pm 0.04)\%$	$BR(K_{3\pi}) =$ Branching ratio for $K_{3\pi}$	$(1.761 \pm 0.022)\%$

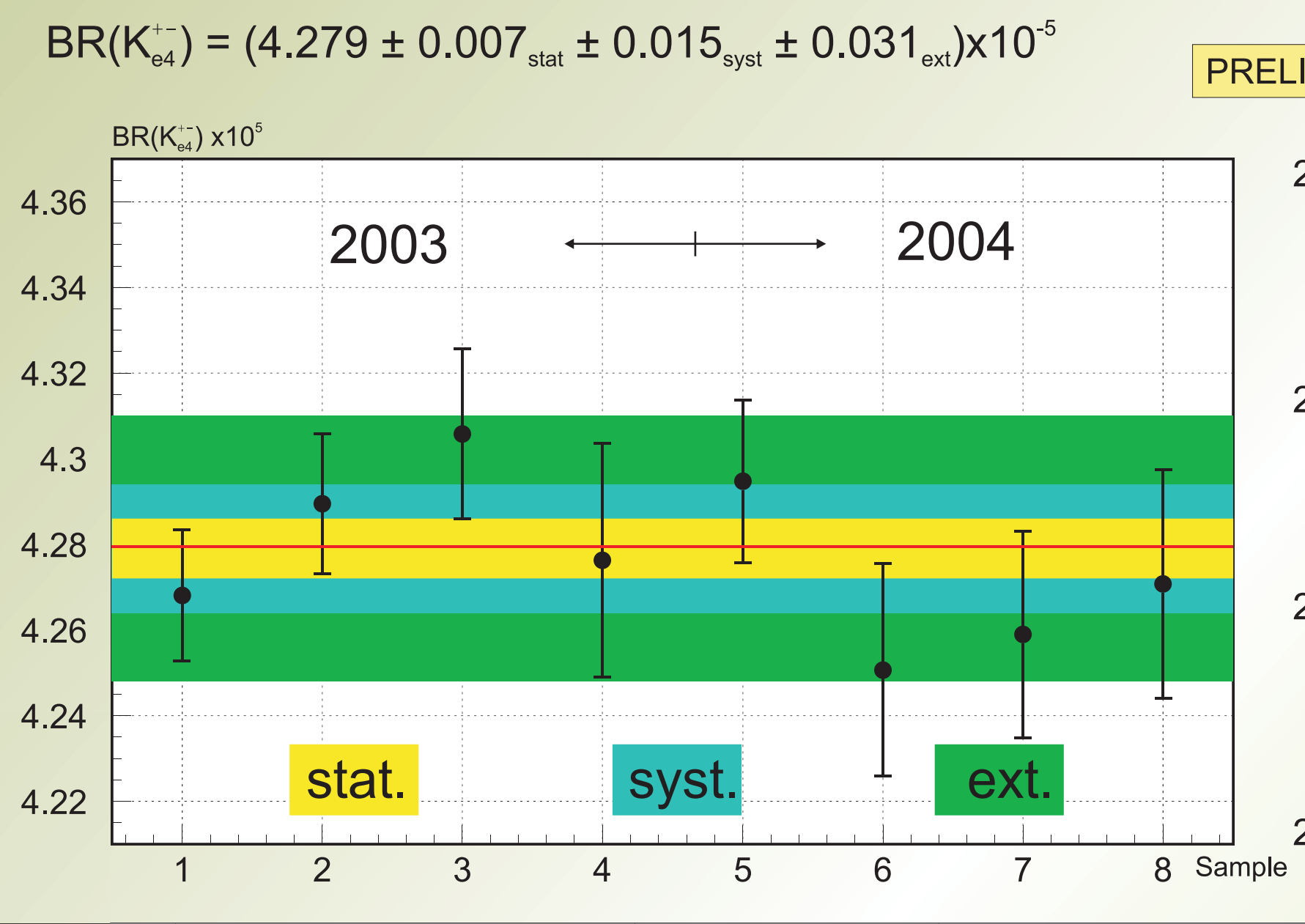
### $K_{e4}^{00}$ FORM FACTOR AND CUSP



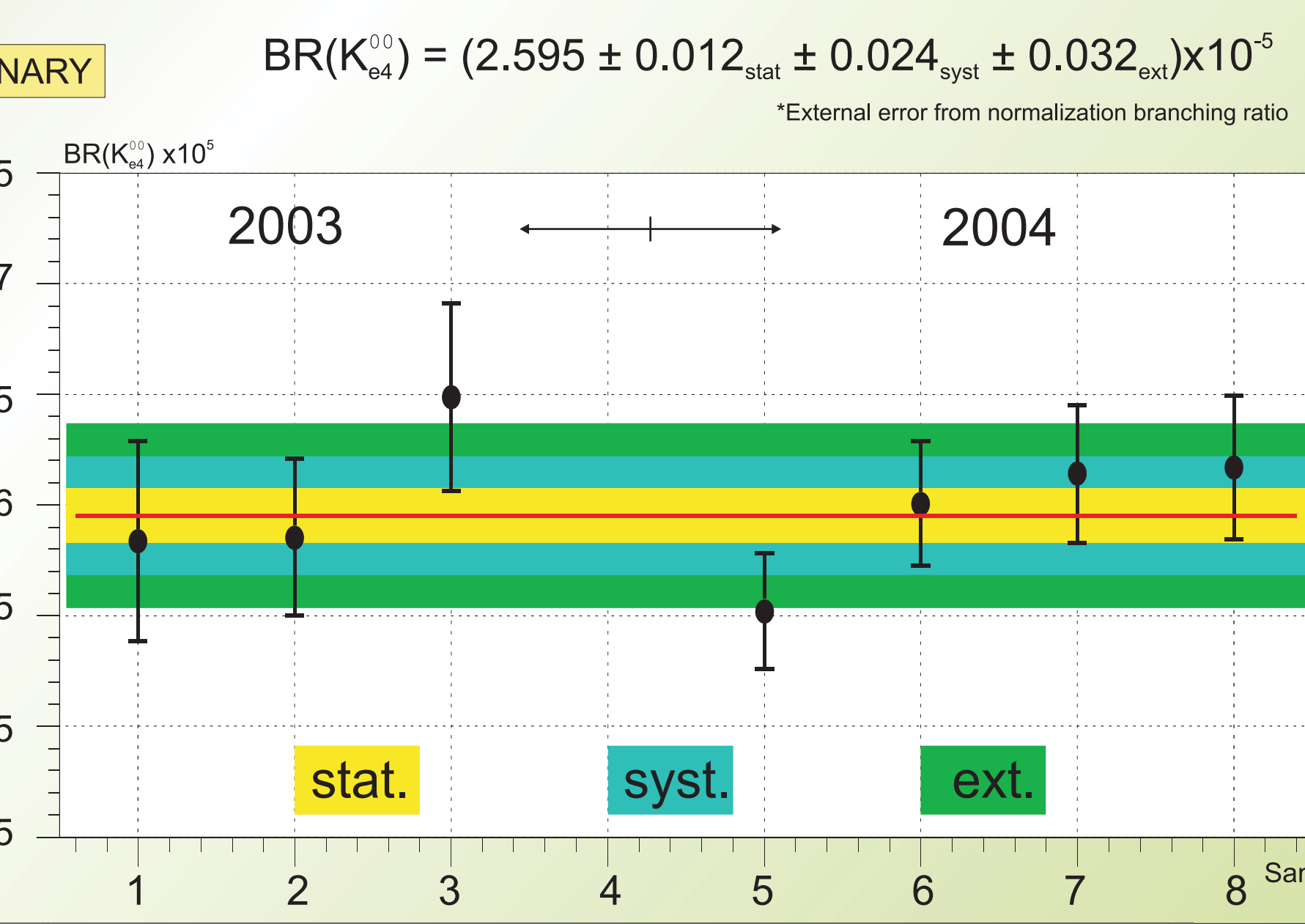
Unperturbed amplitude:  $M_0 = F_s(q^2)$   
 One loop charge exchange contribution:  $M_1 \approx -\frac{2}{3}(a_0 - a_2) \sqrt{\frac{|q^2|}{1+q^2}} f_s$   
 Above  $2m_\pi$  threshold:  $|M_0 + iM_1|^2 = M_0^2 + M_1^2$   
 Below  $2m_\pi$  threshold:  $|M_0 + M_1|^2 = M_0^2 + M_1^2 + 2M_0 M_1$  with destructive interference.

Source of systematic uncertainty	Error [%]
Acceptance and beam geometry	0.18
Muon vetoing	0.16
Accidental activity	0.15
Background	0.14
Particle ID	0.09
Radiative effects	0.08
Independent analysis	0.10

**$BR(K_{e4}^{+-}) = (4.279 \pm 0.035) \times 10^{-5}$  (0.8%)**



**$BR(K_{e4}^{00}) = (2.595 \pm 0.042) \times 10^{-5}$  (1.6%)**



Source of systematic uncertainty	Error [%]
Background	0.35
Simulation statistics	0.12
Form factors dependence	0.20
Radiative effects	0.23
Trigger efficiency	0.80
Particle ID	0.10
Beam Geometry	0.10