

# Study of the rare decay $K^\pm \rightarrow \pi^\pm \gamma\gamma$

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on behalf of the NA48 and NA62 collaboration

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- NA48/NA62 experiments at CERN
- $K^\pm \rightarrow \pi^\pm \gamma\gamma$
- Conclusion

# NA48/NA62 experiments at CERN

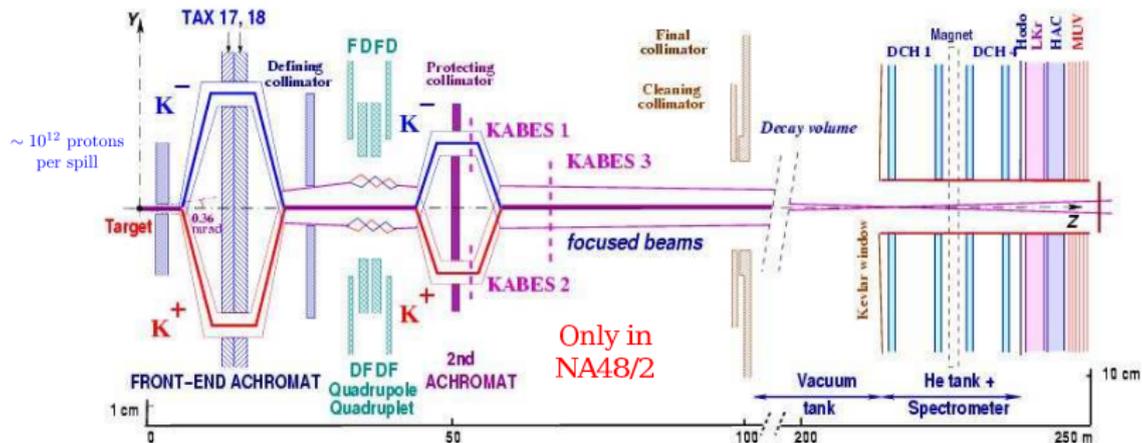


NA48/2 collaboration: Cambridge, CERN, Chicago, Dubna, Edinburgh, Ferrara, Firenze, Mainz, Northwestern, Perugia, Pisa, Saclay, Siegen, Torino, Vienna

NA62 collaboration: Birmingham, Bratislava, Bristol, CERN, Dubna, Fairfax, Ferrara, Firenze, Frascati, Glasgow, IHEP Protvino, INR Moscow, Liverpool, Louvain-la-Neuve, Mainz, Merced, Napoli, Perugia, Pisa, Prague, Roma I, Roma II, San Luis Potosí, Stanford, Sofia, Torino

Ancestor: NA31	
1997	$e^+e^-$ run $K_L + K_S$
1998	$e^+e^-$ run $K_L + K_S$
NA48	1999 $e^+e^-$ run $K_L + K_S$ $K_S$ Hi Int
	2000 $K_L$ only $K_S$ High Intensity NO Spectrometer
NA48/1	2001 $e^+e^-$ run $K_L + K_S$ $K_S$ High Int.
	2002 $K_S$ High Intensity
NA48/2	2003 $K^+$ High Intensity
	2004 $K^+$ High Intensity
NA62 $R_K$	2007/08: $K_{S2}^+ / K_{L2}^+$ runs
NA62	2007-2012: R&D
	2014: Start $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

# NA48/2 & NA62 Beam line



NA48/2  $K^+ / K^-$  simultaneous beams

$$P_K = (60 \pm 3) \text{ GeV}/c$$

NA62  $K^+ / K^-$  both simultaneous beams and single beams (mostly  $K^+$  beam, optimized for  $R_K$  measurement)

$$P_K = (74 \pm 1.4) \text{ GeV}/c$$

Decay volume: 114 m long

K decays in the vacuum tank: 22%(18%)



# NA48/2 & NA62 detectors: Magnetic Spectrometer

## Principal subdetectors:

Magnetic spectrometer ( $p$  in GeV/c):

4 views/DCH;

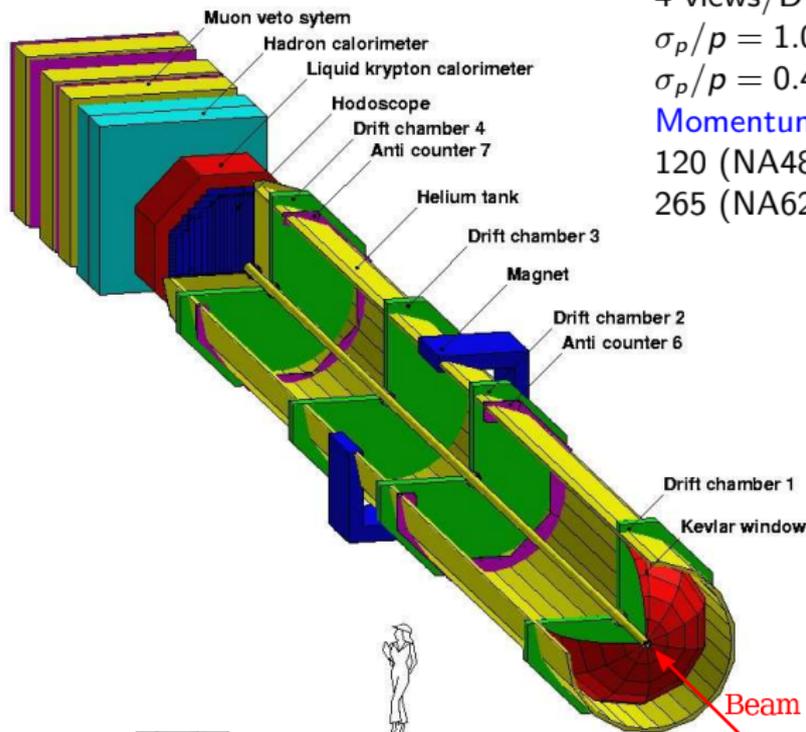
$$\sigma_p/p = 1.02\% \oplus 0.044\% \times p \text{ (NA48/2);}$$

$$\sigma_p/p = 0.48\% \oplus 0.009\% \times p \text{ (NA62);}$$

Momentum kick (MeV/c):

120 (NA48/2);

265 (NA62);



# NA48/2 & NA62 detectors: Hodoscope

Principal subdetectors:

Magnetic spectrometer ( $p$  in GeV/c):

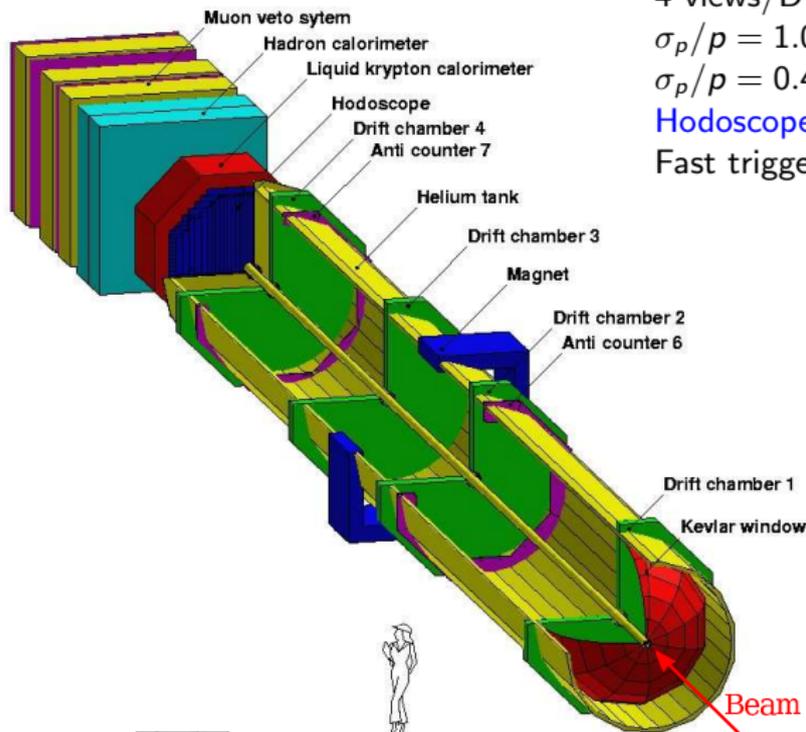
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Hodoscope:

Fast trigger,  $\sigma_t = 150\text{ps}$ ;



# NA48/2 & NA62 detectors: LKr EM calorimeter

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### Hodoscope:

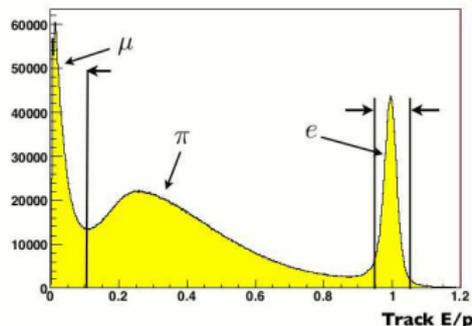
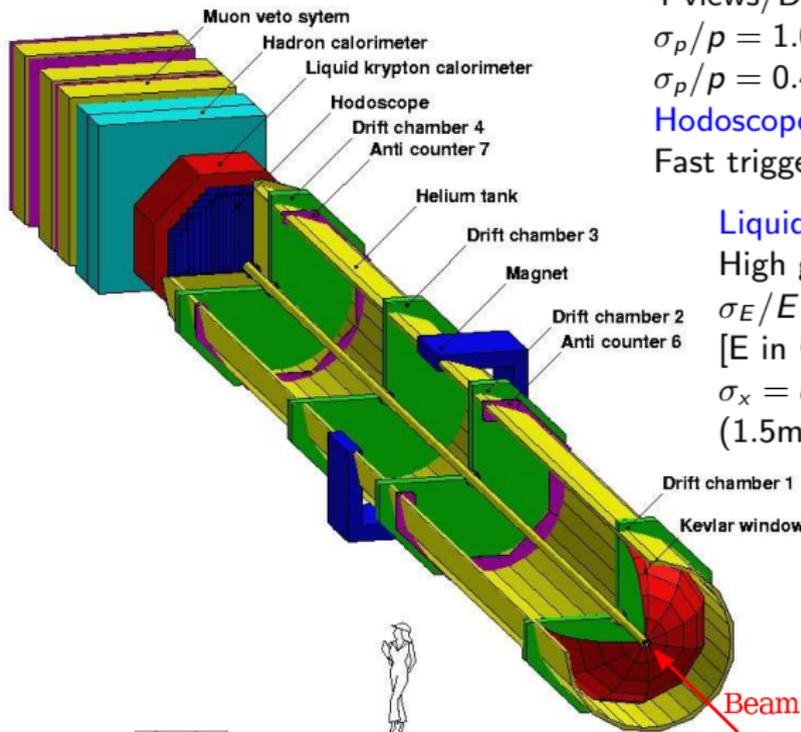
Fast trigger,  $\sigma_t = 150\text{ps}$ ;

### Liquid Krypton EM calorimeter:

High granularity, quasi-homogeneous;

$$\sigma_E/E = 3.2\%/\sqrt{E} \oplus 9\%/E \oplus 0.42\% \text{ [E in GeV];}$$

$$\sigma_x = \sigma_y = 4.2\text{mm}/\sqrt{E} \oplus 0.6\text{mm} \text{ (1.5mm@10GeV)}$$



# Theory: Chiral perturbation description (1)

In chiral perturbation theory the double differential rate in  $K \rightarrow \pi\gamma\gamma$  decays is

$$\frac{\partial^2 \Gamma}{\partial y \partial z} = \frac{M_K}{2^9 \pi^3} \left\{ z^2 (|A + B|^2 + |C|^2) + \left[ y^2 - \frac{1}{4} \lambda(1, r_\pi^2, z) \right]^2 (|B|^2 + |D|^2) \right\}$$

with no tree-level contributions of  $O(p^2)$ .

$$z = \frac{(P_{\gamma_1} + P_{\gamma_2})^2}{m_K^2} = \left( \frac{m_{\gamma\gamma}}{m_K} \right)^2$$

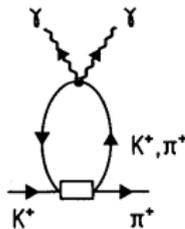
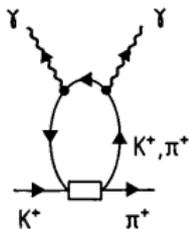
$$y = \frac{P_K (P_{\gamma_1} - P_{\gamma_2})}{m_K^2}$$

$$\lambda(a, b, c) = a^2 + b^2 + c^2 - 2(ab + bc + ca)$$

$$r_\pi = \frac{m_\pi}{m_K}$$

$A$ ,  $B$ ,  $C$  and  $D$  are invariant amplitudes functions of  $z$  and  $y$ .

Rate and spectrum depend on a single unknown  $O(1)$  parameter  $\hat{c}$ .



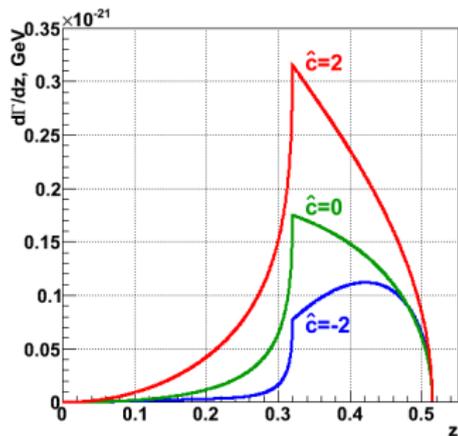
# Theory: Chiral perturbation description (2)

- Rate and spectrum depend on a single unknown  $O(1)$  parameter  $\hat{c}$ .
- Cusp at  $\pi^+\pi^-$  threshold  $m_{\gamma\gamma} = 2m_{\pi^\pm}$  ( $z \sim 0.32$ ).

$O(p^4)$

$B$  and  $D$  amplitudes are still zero

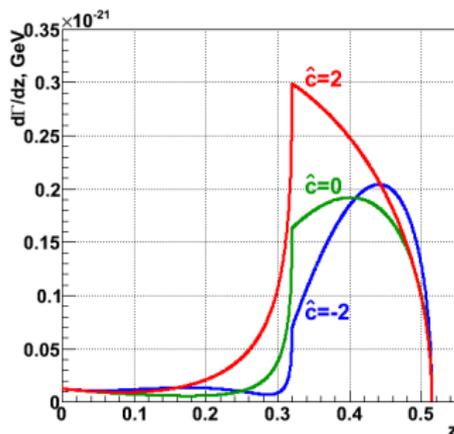
[Ecker, Pich, de Rafael NPB303(1988) 665]



$O(p^6)$

“Unitary corrections” increase BR at low  $\hat{c}$  and result in a non-zero rate at  $m_{\gamma\gamma} \rightarrow 0$ .

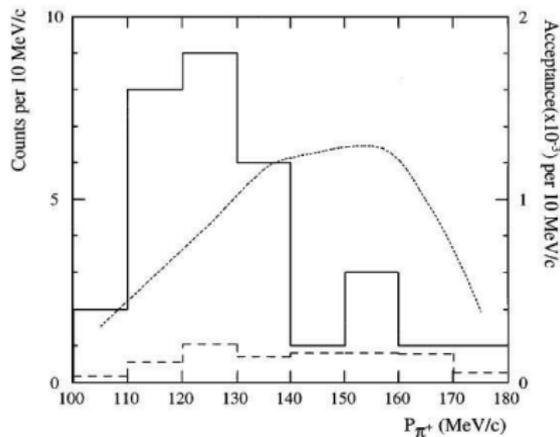
[D’Ambrosio, Portolés, PLB386 (1996) 403]



# Experimental status

E787 (BNL), 31 candidates with 5 background events

Fit the  $\pi^+$  spectrum to extract  $\hat{c}$



$$\hat{c} = (1.6 \pm 0.6) O(p^4)$$

$$\hat{c} = (1.8 \pm 0.6) O(p^6)$$

$$BR = (1.10 \pm 0.32) \times 10^{-6}$$

( $O(p^6)$  full kinematic range)

Figure:  $\pi^+$  momentum distribution for 31  $K^+ \rightarrow \pi^+ \gamma \gamma$  candidates (solid) and for estimated background events (dashed). The acceptance is given by the dotted line.

[PRL79 (1997) 4079]

- **Separate analysis of 2004 (NA48/2) and 2007 (NA62) run data**
  - 2004: minimum bias trigger, 3 days data taking
  - 2007: minimum bias triggers downscaled and served as control triggers ( $D \approx 20$ , 3 months of data taking)
  - Comparable statistics for NA48/2 and NA62 data
  - Different acceptances, different beam momentum
- **Combination of the two analyses**
  - Accounting for correlated systematics

# $K^\pm \rightarrow \pi^\pm \gamma\gamma$ selection (1)

The  $K^\pm \rightarrow \pi^\pm \gamma\gamma$  ( $K_{\pi\gamma\gamma}$ ) decay rate is measured with respect to the normalization decay chain ( $K_{2\pi}$ ):

$$K^\pm \rightarrow \pi^\pm \pi^0$$

followed by the  $\pi^0 \rightarrow \gamma\gamma$  decay

Signal and normalization contain the same set of particles in the final state:  
**the principal selection criteria are common for the two modes**

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No  $K_{\pi\gamma\gamma}$  acceptance loss, but  $K_{2\pi}$  acceptance reduced

Differences between the selection conditions for the NA48/2 and NA62 data due to the **different central values of kaon momentum and momentum kick of the spectrometer magnet**

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$\pi^\pm$  identification

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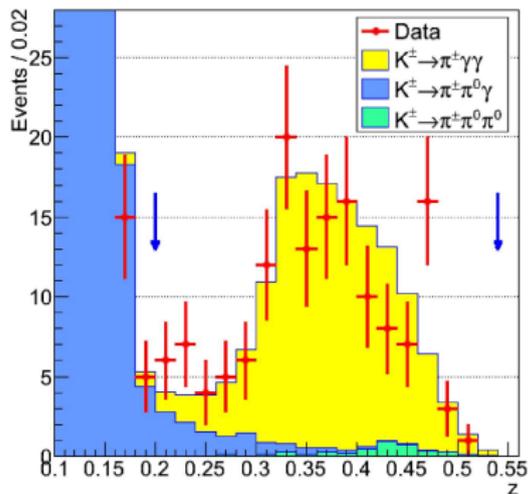
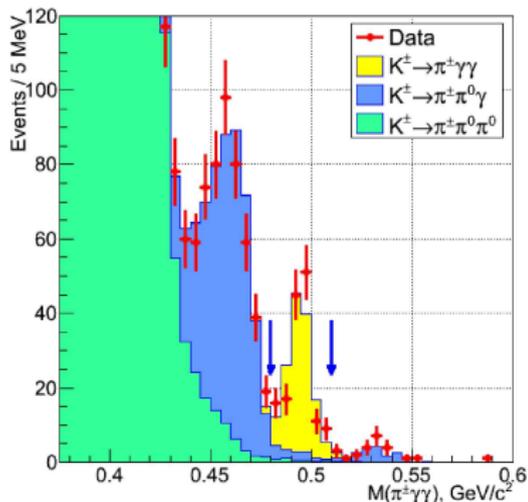
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The  $K_{\pi\gamma\gamma}$  and  $K_{2\pi}$  selection conditions differ only in the di-photon invariant mass requirement.

For the  $K_{\pi\gamma\gamma}$ :

$0.2 < z = (m_{\gamma\gamma}/m_K)^2 < 0.54$  ( $K^\pm \rightarrow \pi^\pm \pi^0$  decays peak at  $z=0.075$ )

# 2004 data set - NA48/2



$K_{\pi\gamma\gamma}$ candidates	149
$K_{2\pi(\gamma)}$ background	$11.4 \pm 0.6$
$K_{3\pi}$ background	$4.1 \pm 0.4$
$K_{\pi\gamma\gamma}$ signal	$134 \pm 12$

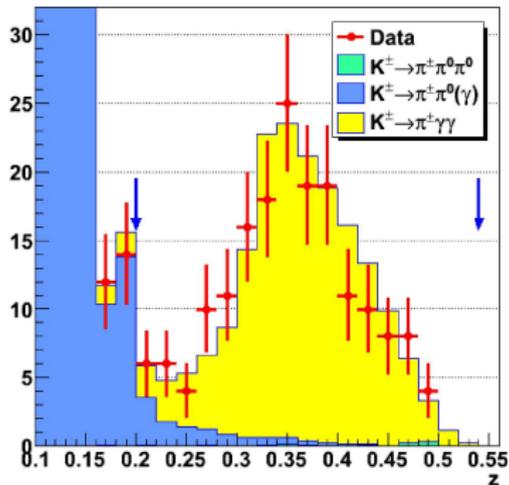
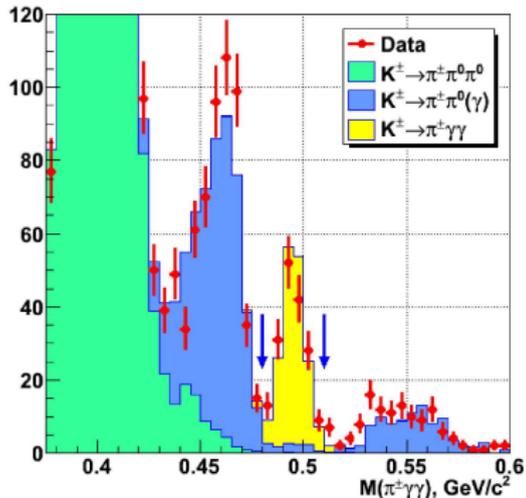
ChPT  $O(p^4)$ :

$$\hat{c} = 1.36 \pm 0.33_{stat} \pm 0.07_{syst} = 1.36 \pm 0.34$$

ChPT  $O(p^6)$ :

$$\hat{c} = 1.67 \pm 0.39_{stat} \pm 0.09_{syst} = 1.67 \pm 0.40$$

# 2007 data set - NA62



$K_{\pi\gamma\gamma}$ candidates	175
$K_{2\pi(\gamma)}$ background	$11.1 \pm 1.0$
$K_{3\pi}$ background	$1.3 \pm 0.3$
$K_{\pi\gamma\gamma}$ signal	$163 \pm 13$

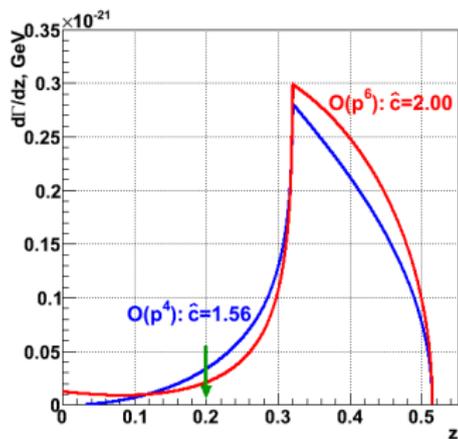
ChPT  $O(p^4)$ :

$$\hat{c} = 1.71 \pm 0.29_{\text{stat}} \pm 0.06_{\text{sys}} = 1.71 \pm 0.30$$

ChPT  $O(p^6)$ :

$$\hat{c} = 2.21 \pm 0.31_{\text{stat}} \pm 0.08_{\text{sys}} = 2.21 \pm 0.32$$

# Combined results



- Visible region above the  $K^+ \rightarrow \pi^+ \pi^0$  peak:  $z > 0.2$  ( $m_{\gamma\gamma} > 221 \text{ MeV}/c^2$ )
- Indications of cusp-like behavior at  $2m_\pi$
- ChPT  $O(p^4)$  vs  $O(p^6)$  models cannot be discriminated

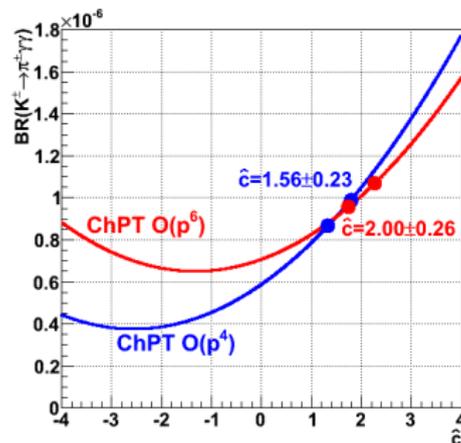
Fit results:

$O(p^4)$ :

$$\hat{c} = 1.56 \pm 0.22_{\text{stat}} \pm 0.07_{\text{syst}} = 1.56 \pm 0.23$$

$O(p^6)$ :

$$\hat{c} = 2.00 \pm 0.24_{\text{stat}} \pm 0.09_{\text{syst}} = 2.00 \pm 0.26$$



$$BR = (1.01 \pm 0.06) \times 10^{-6} \text{ (Model dependent)}$$

$$\text{PDG } BR = (1.10 \pm 0.32) \times 10^{-6}$$

# NA48/2 Model independent Branching Ratio

To compute the model-independent branching fraction in the signal region,  $z > 0.2$ , partial branching fractions are computed in 8 sufficiently small  $z$  bins: acceptance almost independent of kinematical distribution

$z$ range	$N_j$	$N_j^B$	$A_j$	$\mathcal{B}_j \times 10^6$
0.20–0.24	13	4.89	0.194	$0.045 \pm 0.020$
0.24–0.28	9	2.73	0.198	$0.034 \pm 0.016$
0.28–0.32	18	2.33	0.194	$0.087 \pm 0.024$
0.32–0.36	33	1.30	0.190	$0.180 \pm 0.033$
0.36–0.40	31	0.98	0.184	$0.177 \pm 0.033$
0.40–0.44	18	1.61	0.173	$0.103 \pm 0.027$
0.44–0.48	23	1.21	0.135	$0.175 \pm 0.038$
$z > 0.48$	4	0.52	0.049	$0.076 \pm 0.044$

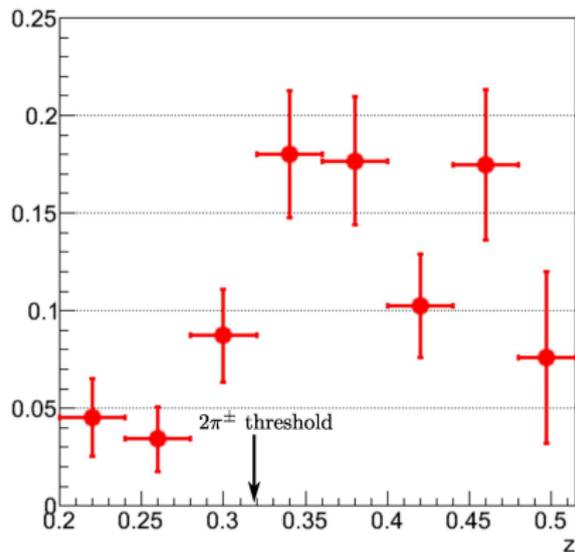


Figure: Model independent Branching Ratio ( $\times 10^6$ )

$$BR_{MI}(z > 0.2) = (0.877 \pm 0.087_{stat} \pm 0.017_{syst}) \times 10^{-6}$$

Main systematic effect: background estimate (LKr cluster merging)

- Measurements of  $\hat{c}$  in both  $O(p^6)$  and  $O(p^4)$  frame
- $BR$  measurement compatible with PDG but with a smaller error ( $\sim 5$  times)
- New result: model-independent  $BR(z > 0.2)$
- Final results and publications are in preparation



Thank you for your  
attention