Search for new resonant states in ¹⁰C and ¹¹C and their impact on the cosmological lithium problem

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The observed primordial 7 Li abundance in metal-poor halo stars is found to be lower than its Big-Bang nucleosynthesis (BBN) calculated value by a factor of approximately three. Some recent works suggested the possibility that this discrepancy originates from missing resonant reactions which would destroy 7 Be, parent of 7 Li. The most promising candidate resonances which were found include a possibly missed 1^- or 2^- narrow state around 15 MeV in the compound nucleus 10 C formed by 7 Be + 3 He and a state close to 7.8 MeV in the compound nucleus 11 C formed by 7 Be + 4 He. In this work, we studied the high excitation energy region of 10 C and the low excitation energy region in 11 C via the reactions 10 B(3 He,t) 10 C and 11 B(3 He,t) 11 C, respectively, at the incident energy of 35 MeV. Our results for 10 C do not support 7 Be + 3 He as a possible solution for the 7 Li problem. Concerning 11 C results, the data show no new resonances in the excitation energy region of interest and this excludes the 7 Be + 4 He reaction channel as an explanation for the 7 Li deficit.

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The primordial nucleosynthesis of light elements 2 H, 3,4 He, and 7 Li, together with the expansion of the Universe and the cosmic microwave background (CMB), are the three observational pillars of the standard Big-Bang model where the last free parameter was the baryonic density of the universe, Ω_b . A precise value for this free parameter has been deduced from the analysis of the anisotropies of the CMB as observed by the Wilkinson Microwave Anisotropy Probe (WMAP) satellite ($\Omega_b h^2 = 0.02249 \pm 0.00056$) [1] and more recently by the Planck mission ($\Omega_b h^2 = 0.02207 \pm 0.00033$) [2].

A comparison between the calculations of the primordial abundances of the light nuclei and the observations reveals a good agreement for helium and an excellent agreement for deuterium. In contrast, the theoretical predictions show a discrepancy by a factor of ≈ 3 for ^7Li abundance [3,4]. Indeed, at the baryonic density of the Universe, $\Omega_b h^2$, derived from the CMB anisotropies, the predicted Big-Bang nucleosynthesis (BBN) abundance of ^7Li is $(^7\text{Li}/\text{H})_{\text{BBN}} = (5.12^{+0.71}_{-0.62}) \times 10^{-10}$ [3] when using WMAP data or $(4.89^{+0.41}_{-0.39}) \times 10^{-10}$ [5] with the Planck data. On the other hand, the observed ^7Li abundance, derived from the observations of low-metallicity halo dwarf

stars, was found to be $(^7\text{Li/H})_{\text{halo}*} = (1.58 \pm 0.31) \times 10^{-10}$ [6]. This significant discrepancy between the observations and the BBN predictions is known as the "lithium problem" [7].

Several ideas were addressed to try to explain this ⁷Li problem [8]. Some conceived the idea that the ⁷Li deficit points toward physics beyond the standard model such as decay of supersymmetric particles [8]. Others have suggested that the problem could be due to ⁷Li stellar destruction in the atmosphere of the halo stars [9]. However, a uniform destruction of ⁷Li over the so-called Spite-plateau region seems difficult [10]. Finally, several authors investigated the nuclear aspect of the problem concerning the ⁷Li abundance [11–13]. The main process for the production of the BBN ⁷Li at $\Omega_b h^2$ is the decay of ⁷Be, which is produced in the reaction ${}^{3}\text{He}({}^{4}\text{He},\gamma){}^{7}\text{Be}$. Direct measurements of this reaction cross -section were performed by several groups, resulting in a significant reduction of the thermonuclear reaction rate uncertainty [14] but no solution to the ⁷Li problem. More generally, the experimental nuclear data concerning the 12 main BBN reactions are sufficient to exclude a solution in this region, so that one has to extend the network to up to now-neglected reactions. For instance, it was found [11,15] that if the ${}^{7}\text{Be}(d,p)2\alpha$ reaction rate was significantly higher, the ⁷Li abundance would be brought down to the observed level. However, subsequent experiments [12,16,17] ruled out this possibility [18].

Very recent works have extended this search [19–21] and suggested the possibility of partially or totally solving the 7 Li problem if additional destruction of A=7 isotopes

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occurs via missed resonant nuclear reactions involving 7 Be. The most promising candidates are possibly missed resonant states in 7 Be + 3 He \rightarrow 10 C [19] and in 7 Be + 4 He \rightarrow 11 C [20,21] compound nuclei.

According to Ref. [19], the presence of any narrow ¹⁰C states with $J^{\pi} = (1^- \text{ or } 2^-)$, allowing s-wave capture close to the ${}^{7}\text{Be} + {}^{3}\text{He}$ reaction threshold (Q = 15.003 MeV), could bring a solution for the ⁷Li problem (see Fig. 8 in Ref. [19]). Unfortunately, the excitation energy range of ¹⁰C between 10.0 and 16.5 MeV is very poorly known [22–24]; the investigated excitation energy region in Ref. [22], where 10 C was populated via 10 B(3 He,t) reaction, was limited to the region between the ground state and 8 MeV, while in Ref. [23], where it was studied via (p, n) reaction up to 20 MeV excitation energy. The energy resolution of about 1 MeV and the important background does not allow us to draw any conclusions on the absence or presence of a narrow 1⁻ or 2⁻ state close to 15 MeV exitation energy. ¹⁰C was also studied via 12 C(p, t) reaction but this favors the population of 0^+ and 2^+ states [24].

Concerning the ⁷Be + ⁴He reaction channel, Civitarese *et al.* [21] claimed that any isolated state between 7.79 and 7.90 MeV excitation energy of ¹¹C having a total width between 30 and 160 keV and corresponding to a resonant energy between 250 and 350 keV respectively would solve the ⁷Li problem (see Figs. 5, 6, and 7 in Ref. [21]). The excited states of ¹¹C up to 9 MeV were studied in the past via various indirect reactions [25] and no state between 7.79 and 7.90 MeV is reported. However, no dedicated measurement in this narrow energy region was carried out in the previous works, so it cannot be excluded that a weakly populated state in this energy region has been missed.

In the present work, we report on an experimental study of the excited states of 10 C and 11 C where the high excitation energy region of 10 C and the low one of 11 C were investigated using 10 B(3 He,t) 10 C and 11 B(3 He,t) 11 C charge-exchange reactions respectively. We have chosen to use the (3 He,t) reaction because (i) it is less selective than the (p, t) reaction where odd parity and odd spins are strongly inhibited by the selection rules and (ii) it has much better resolution and detection efficiency than the (p, n) reaction.

The $^{10}\mathrm{B}(^3\mathrm{He},t)^{10}\mathrm{C}$ and $^{11}\mathrm{B}(^3\mathrm{He},t)^{11}\mathrm{C}$ reactions were carried out at an energy of 35 MeV using a $^3\mathrm{He}$ beam from the tandem accelerator of the Orsay-ALTO facility. The targets consisted of a 90(9) $\mu\mathrm{g/cm^2}$ enriched $^{10}\mathrm{B}$ with a gold backing of 200 $\mu\mathrm{g/cm^2}$ thickness and a self-supporting natural boron (80.1% $^{11}\mathrm{B}$) of 250 $\mu\mathrm{g/cm^2}$ thickness. Elastic scattering measurements were performed at 40° in order to evaluate the contaminants present in the two targets. A non-negligible contamination of $^{12}\mathrm{C}$ and $^{16}\mathrm{O}$ was observed in $^{10}\mathrm{B}$ and $^{nat}\mathrm{B}$ targets (Fig. 1). Hence, for background contaminant evaluation, we performed ($^3\mathrm{He},t$) measurements also on an 80(4) $\mu\mathrm{g/cm^2}$ $^{12}\mathrm{C}$ target and a 75(4) $\mu\mathrm{g/cm^2}$ $^{12}\mathrm{C}$ 04 target. Target thicknesses were determined by α -energy loss measurements. The beam current was measured with a Faraday cup and the intensity was about 200 enA.

The reaction products were momentum analyzed by the Split-pole magnetic spectometer [26] and were detected at the focal plane by a position-sensitive gas chamber, a ΔE

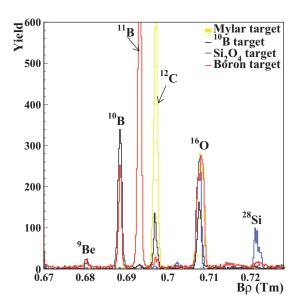


FIG. 1. (Color online) The black, red (gray), yellow (light gray), and blue (dark gray) solid lines represent the results from 3He elastic scattering at 35 MeV measured at 40° for $^{10}B,\,^{nat}B,\,Mylar,\,$ and Si_2O_4 targets respectively. The contamination from ^{12}C and ^{16}O can be easily identified in ^{10}B and ^{nat}B targets.

proportional gas counter, and a plastic scintillator. The light fragments emitted by the 10 B(3 He,t) 10 C reaction were detected at 7°, 10°, 13°, and 15° in the laboratory system while those coming from 11 B(3 He,t) 11 C were detected at 7° and 10°. Well-known excited states of 11 C from 2 to 8.655 MeV excitation energy were used to calibrate the focal plane position detector.

The energy resolution obtained in this experiment was about 70 keV (FWHM) in the laboratory frame for the low excitation energy region ($E_x \le 8$ MeV) and around 37 keV (FWHM) for the high excitation energy region ($E_x \ge 12$ MeV) of 10 C and 11 C.

Typical spectra obtained for the ${}^{10}\mathrm{B}({}^{3}\mathrm{He},t){}^{10}\mathrm{C}$ reaction at 10° (laboratory) is shown in Fig. 2 for the exitation energy region from 0 to 7 MeV in ${}^{10}\mathrm{C}$ and in Fig. 3 for the excitation region of astrophysical interest from 14 to 16.6 MeV in ${}^{10}\mathrm{C}$. Peaks not explicitly labeled in the figures are assigned to unidentified impurities and peaks of ${}^{10}\mathrm{C}$ are only labeled by their excitation energy.

The well-known levels of ¹⁰C [22] at 3.35, 5.22, 5.38, and 6.58 MeV excitation energies as well as the ground state are observed in this experiment (Fig. 2). The 5.22- and 5.38-MeV states are not separated because their natural width (225 and 300 keV, respectively) is much larger than their separation energy. A small contamination by the 6.905-MeV state of ¹¹C due to ¹¹B contamination in the target is also present in the 5.22 + 5.38 MeV peak.

The 10 C excitation energy region from 7 to 14 MeV (not displayed in this paper) was also investigated but no other peaks except those coming from 16 O(3 He,t) 16 F and 12 C(3 He,t) 12 N contaminant reactions were identified at the four measured angles. The two states at 9 and 10 MeV excitation energy in 10 C weakly populated in the 10 B(p, n) 10 C work [23] are not observed in this experiment.

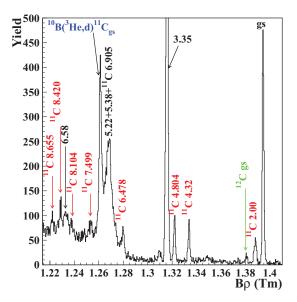


FIG. 2. (Color online) Triton B ρ spectrum measured at $\theta=10^\circ$ (lab) with the 35-MeV 3 He beam on the 10 B target in the excitation energy region from gs to 7.2 MeV. The excitation energy (MeV) of 10 C levels are indicated as well as those of 11 C coming from a small 11 B contamination of the target or a deuteron contamination of the selected reaction products.

In Fig. 3, the background becomes much more important because of the triton continuum. The well-populated and separated peaks belong to unbound states of 16 F and bound states of 12 N coming from (3 He,t) reactions on 16 O and 12 C contamination, respectively. A dominant peak corresponding to an excitation energy of 16.46 MeV in 10 C is observed at the angles 7° and 10° and follows well the 10 B(3 He,t) 10 C reaction

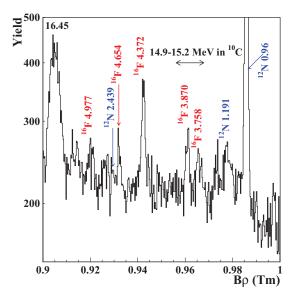


FIG. 3. (Color online) Triton B ρ spectrum measured at $\theta=10^\circ$ (lab) with the 35-MeV 3 He beam on 10 B target in the excitation energy region from 14 to 16.5 MeV. The excitation energy (MeV) of 10 C levels are indicated as well as those of 12 N and 16 F coming from a substantial 12 C and 16 O contamination of the target. The unlabeled peaks correspond to unidentified heavy contamination.

kinematic. From the peak analysis of this state, we deduced a peak position of $E_x = 16.46 \pm 0.01$ MeV and a peak width of about 159 \pm 19 keV. Note that a state at the energy of about 16.5 MeV was already observed in the 10 B(p, n) 10 C experiment [23].

Concerning the excitation energy region between 14.9 and 15.2 MeV in 10 C, no unknown state is observed. The only observed peaks in this energy region are the unbound states of 16 F at 3.758 and 3.87 MeV excitation energy due to 16 O contamination in the target. The absence of a new 10 C state at the four measured angles may have three nonexclusive explanations: First, the state of interest is too large and cannot be distinguished from the triton continuum. Second, the charge exchange (3 He, t) reaction cross section is too small, and third, there is no isolated state of 10 C in this excitation energy region.

The choice among these explanations is thus dependent on the width of the peak of interest and the (${}^{3}\text{He},t$) cross section. In order to visualize the effect of these quantities for our particular experimental conditions, a numerical simulation has been performed of an assumed state at 15.1 MeV on top of the measured (${}^{3}\text{He},t$) spectrum at $\theta_{\text{lab}} = 10^{\circ}$ once the ${}^{16}\text{O}$ contamination is subtracted from a spectrum obtained with the Si₂O₄ target. The assumed state is given different widths and is populated with different charge-exchange cross sections. For these simulations, we considered a ¹⁰B thickness of $90 \mu g/cm^2$, a number of incident ³He nuclei similar to the one measured in the experiment and the measured experimental resolution of 37 keV (FWHM) in the considered excitation energy range. The excitation energy region of interest is fitted with a linear function well describing the triton background $(\chi^2 = 0.85 \text{ with dof} = 96, \text{ where dof denotes degree of}$ freedom) and the parameters of which are left free.

The presence of the assumed state with the chosen properties lead to an increase of the χ^2 value, and the null hypothesis "there is a 10 C state in the region of interest" can be rejected at the usual significance level of 5% when $\chi^2 > 1.25$ for 96 degrees of freedom (goodness-of-fit test). An exclusion zone can then be drawn in the plane of the charge-exchange cross section versus the width of the assumed state as shown on Fig. 4. We conclude that if a state is present in this region, a peak would have been identified with a probability larger than 95% confidence level in the red (gray) exclusion zone.

According to the literature [27,28], typical (3 He,t) differential charge exchange cross sections to 1^- or 2^- states at energies close to our incident energy are generally much larger than 25 μ b/sr at 10° in the laboratory system. Therefore, if we assume comparable cross sections, we can conclude from the 95% CL exclusion zone that any 1^- or 2^- state of 10 C in the excitation energy region around 15 MeV should have, if present, a total width larger than 590 keV in order to not be observed in this experiment.

To check the consistency of our simulations and conclusions concerning a hypothetical existing 10 C state, we used the same procedure for states of 12 N populated by the 12 C(3 He,t) 12 N reaction and using $10 \mu g/cm^2$ of 12 C, which is the amount of contamination present in our 10 B target. In this case, the total width limit of observation of any 1^- or 2^- existing state of 12 N is found to be lower, $\Gamma_T = 300$ keV, at the expected cross section of $60 \mu b/sr$ [29]. This result is in agreement with the

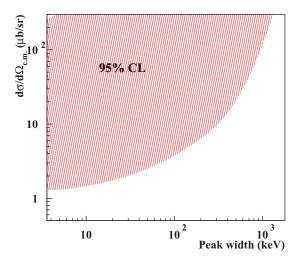


FIG. 4. (Color online) Exclusion zone in the plane of the charge-exchange cross section vs the width of the state. The red (gray) hatched area corresponds to a 95% confidence level (CL) exclusion zone of an isolated 10 C state when using a 10 B target of 90 μ g/cm² thickness.

observation in our experiment of the 1.191 MeV ($J^{\pi}=2^{-}$) state of ¹²N, which has a total width of 118 keV and the lack of observation of the known 1.8 MeV ($J^{\pi}=1^{-}$) state of ¹²N, which has a total width of 750 keV.

Concerning the ${}^{11}B({}^{3}He,t){}^{11}C$ measurements, spectra obtained at 7° (lab) and 10° (lab) are shown in Figs. 5 and 6.

In Fig. 5, we can observe that all the known states of ¹¹C up to 9 MeV excitation energy are populated with large cross sections in this experiment.

In Fig. 6, we do not observe any triton peak in the excitation energy region between 7.79 and 7.90 MeV of

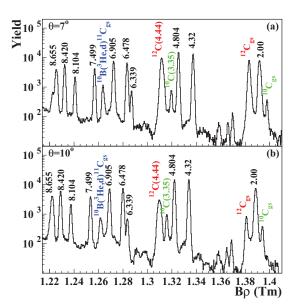


FIG. 5. (Color online) 11 B(3 He,t) 11 C B ρ spectra measured at the laboratory angles, $\theta = 7^{\circ}$ (a) and 10° (b) in the excitation energy region from gs to 9 MeV. Excitation energies (MeV) of 11 C levels are indicated. The unlabeled peaks correspond to unidentified contamination.

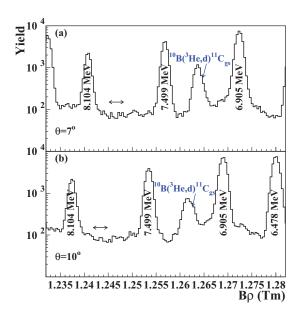


FIG. 6. (Color online) 11 B(3 He,t) 11 C B ρ spectra measured at $\theta = 7^{\circ}$ (a) and 10° (b) in the excitation energy region of interest close to 8 MeV. Excitation energies of 11 C levels are indicated. The double arrow indicates the astrophysical region of interest.

¹¹C corresponding to the energy resonance between 250 and 350 keV. Owing to the very large signal-to-background ratio observed in the spectrum, which is 10 times better than in ¹⁰C case, it is very unlikely that a new state of ¹¹C exists in this energy region. This result is strengthen by the fact that all the known states in the mirror nuclei ¹¹B [25] have their counterpart in ¹¹C at energies lower than 12 MeV.

The reactions ${}^{7}\text{Be}({}^{3}\text{He},p){}^{9}\text{B}$ and ${}^{7}\text{Be}({}^{3}\text{He},\alpha){}^{6}\text{Be}$ are the only possible open channels for the reaction ${}^{7}\text{Be} + {}^{3}\text{He} \rightarrow {}^{10}\text{C}$, so calculations of their reaction rates were performed for the lower limit derived from our experiment concerning the study of resonant state in the compound nucleus ¹⁰C. Hence, we assumed a 1⁻ state in the compound nucleus ¹⁰C with a total width equal to the experimental lower limit of $\Gamma_T = 590 \text{ keV}$ in one case and also with $\Gamma_T=200~\text{keV}$ in the case where the (3 He,t) differential charge exchange cross section to this state is a factor of three smaller than the expected minimum one. The resonance position was varied so that the corresponding resonance energy $E_{\rm R}$ would take the values of 10, 100, and 500 keV, spanning the range of interest for BBN, for such a broad state. In these calculations, the Wigner limit value of 1.842 MeV was used for the reduced partial width in the entrance channel. This leads, at the three resonance energies mentioned above, to partial widths, $\Gamma_{^{3}\text{He}}$, of respectively 5.70×10^{-43} , 6.25×10^{-9} , and 2.38 keV at a channel radius of 4.026 fm.

Since $\Gamma_{^3\text{He}} \ll \Gamma_T$, the total width is dominated by the exit channel partial widths, $\Gamma_T \simeq \Gamma_p + \Gamma_\alpha$. To obtain the rates, we numerically integrated a Breit-Wigner formula assuming for the $^7\text{Be}(^3\text{He},p)^9\text{B}$ and $^7\text{Be}(^3\text{He},\alpha)^6\text{Be}$ reactions that $\Gamma_p = \Gamma_T$ and $\Gamma_\alpha = \Gamma_T$, respectively.

The results are displayed in Fig. 7 and correspond for each case to the maximum possible rate. The calculated rates were included in a BBN nucleosynthesis calculation and were found

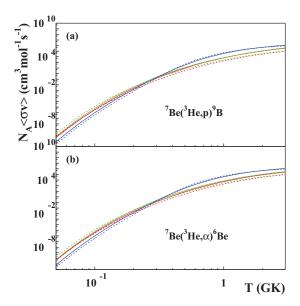


FIG. 7. (Color online) 7 Be(3 He,p) 9 B and 7 Be(3 He, α) 6 Be reaction rate in panels (a) and (b) respectively. The red (gray), green (light gray), and blue (dark gray) solid lines correspond to calculations with $E_{R}=10$, 100, and 500 keV respectively and $\Gamma_{T}=590$ keV and the dotted lines with $\Gamma_{T}=200$ keV.

to have no effect on the primordial ⁷Li/H abundance. Thus, we can conclude that this channel is irrelevant for the ⁷Li problem.

In summary, missing resonant states in the compound nuclei ¹⁰C and ¹¹C nuclei were investigated via measurements at

the Tandem-Alto facility of Orsay of the charge-exchange reactions ${}^{10}B({}^{3}He,t){}^{10}C$ and ${}^{11}B({}^{3}He,t){}^{11}C$ at the incident energy of 35 MeV. In the case of ${}^{10}C$, because of the presence of a large triton continuum background, the conclusion we could assert is that any state of ${}^{10}C$ in the excitation energy region around 15 MeV requires a total width larger than 590 keV to escape its detection in our experiment. With this experimental width limit and even with a three times lower one, 200 keV, the ${}^{7}Be + {}^{3}He$ calculated rates were found to be much too small to solve the lithium problem.

Concerning the ¹¹C case, the present data show that no new state is present at energies between 7.79 and 7.9 MeV of ¹¹C.

Finally, our two results concerning 10 C and 11 C compound nuclei put an end to the various discussions concerning the missing resonant states in these nuclei, which were thought to partially or totally solve the 7 Li problem [19–21] and exclude 7 Be + 3 He and 7 Be + 4 He reaction channels as responsible for the observed 7 Li deficit. With our conclusion and those of previous works concerning the other important reaction channels 3 He + 4 He and 7 Be + d , the 7 Li problem remains unsolved. The solution has very likely to be found outside of nuclear physics.

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