

# Triple and Quartic Gauge Couplings at LEP

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on behalf of the LEP collaborations

- Overview of Couplings Between Gauge Bosons
- LEP2 Measurements
  - Charged TGC's
  - QGC's
  - Neutral TGC's
- Summary and Outlook

# Couplings Between Gauge Bosons

- Within the Standard Model
  - Electroweak interactions mediated by  $\gamma$ ,  $Z^0$ ,  $W^\pm$
  - $SU(2)_L \times U(1)_Y$  gauge group structure
  - Non-Abelian group  $\Rightarrow$  gauge bosons couplings
- Beyond the Standard Model
  - W sub-structure (technicolour?)
  - Loops of ‘new physics’ particles (MSSM?)

	TGC	QGC
Charged	$\gamma WW, ZWW$	$(WWWW),$ $(WWZZ),$ $WWZ\gamma,$ $WW\gamma\gamma$
Neutral	$ZZZ, ZZ\gamma,$ $Z\gamma\gamma, (\gamma\gamma\gamma)$	$(ZZZZ),$ $(ZZZ\gamma),$ $ZZ\gamma\gamma,$ $(Z\gamma\gamma\gamma),$ $(\gamma\gamma\gamma\gamma)$

SM Coupling

SM Coupling but negligible at LEP2

Zero in SM

# Charged Triple Gauge Couplings

- Lorentz invariance and  $U(1)_{em}$   
 $\Rightarrow 7 \gamma WW + 7 ZWW$  independent parameters
- C and P invariance  
 $\Rightarrow 3 \gamma WW + 3 ZWW$  independent parameters
- Charge of  $W^\pm$  known  
 $\Rightarrow 2 \gamma WW + 3 ZWW$  independent parameters

$$\{\kappa_\gamma, \lambda_\gamma, g_1^Z, \kappa_Z, \lambda_Z\}$$

- Use  $SU(2) \times U(1)$  operators
- Assume new physics scale is high

$$\left. \begin{aligned} \kappa_Z &= g_1^Z - (\kappa_\gamma - 1) \tan^2 \theta_W \\ \lambda_Z &= \lambda_\gamma \end{aligned} \right\}$$

$\Rightarrow 3$  independent parameters

$$\{g_1^Z, \kappa_\gamma, \lambda_\gamma\}$$

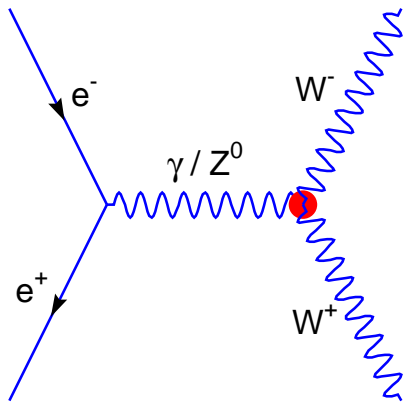
- Magnetic dipole moment

$$\mu_W = \frac{e}{2m_W} (1 + \kappa_\gamma + \lambda_\gamma)$$

- Electric quadrupole moment

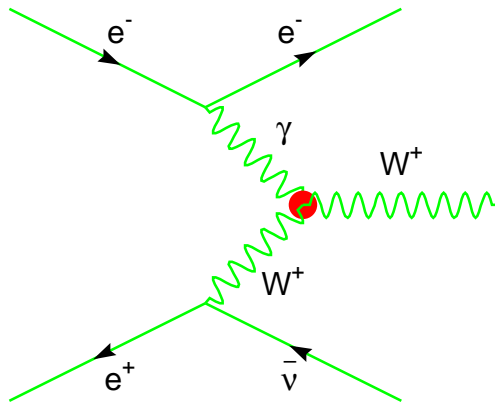
$$q_W = \frac{e}{m_W^2} (\kappa_\gamma - \lambda_\gamma)$$

# cTGC physics at LEP2

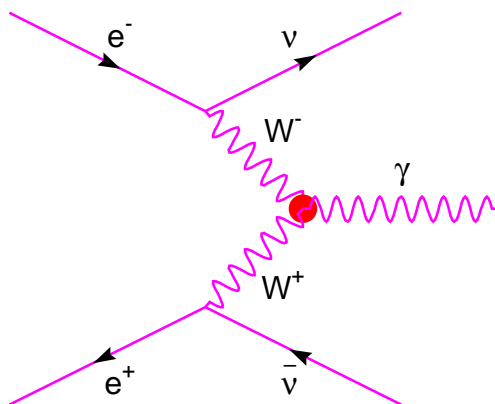


W pair ( $g_1^Z, \kappa_\gamma, \lambda_\gamma$ )

- $qqqq$
- $qql\nu$
- $l\nu l\nu$



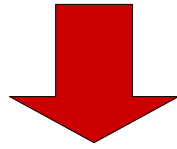
Single W  
( $\kappa_\gamma, \lambda_\gamma$ )



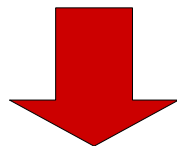
Single  $\gamma$   
( $\kappa_\gamma, \lambda_\gamma$ )

## cTGC Measurements at LEP2

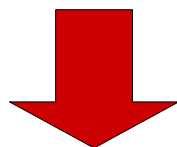
	ALEPH	DELPHI	L3	OPAL
$WW \rightarrow qqqq$	×	×		×
$WW \rightarrow qql\nu$	×	×	×	×
$WW \rightarrow l\nu l\nu$	×			×
single W	×	×	×	×
single $\gamma$	×			×



	ALEPH	DELPHI	L3	OPAL
$g_1^Z$	$1.022^{+0.033}_{-0.033}$	$1.002^{+0.041}_{-0.043}$	$0.952^{+0.053}_{-0.048}$	$0.987^{+0.037}_{-0.036}$
$\kappa_\gamma$	$0.967^{+0.091}_{-0.088}$	$0.966^{+0.106}_{-0.106}$	$0.892^{+0.099}_{-0.095}$	$0.925^{+0.087}_{-0.082}$
$\lambda_\gamma$	$0.010^{+0.034}_{-0.034}$	$0.013^{+0.048}_{-0.045}$	$-0.030^{+0.057}_{-0.054}$	$-0.065^{+0.036}_{-0.035}$



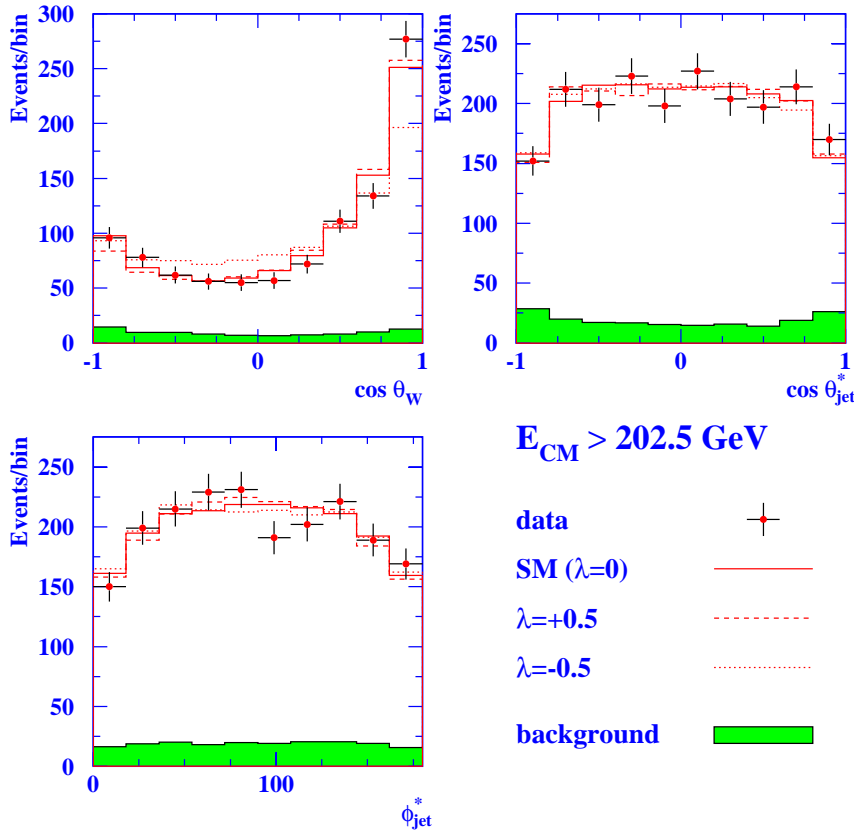
Errors not symmetric in general  
Some systematic errors correlated



Combine log likelihood curves

# Examples of WW Angular Distributions

## OPAL Preliminary

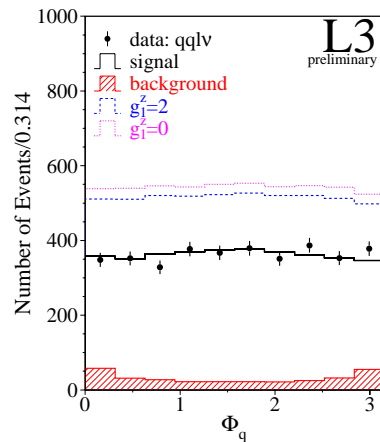
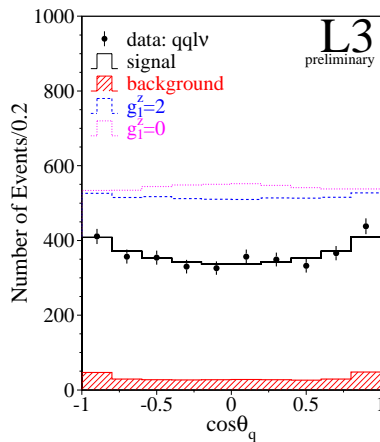
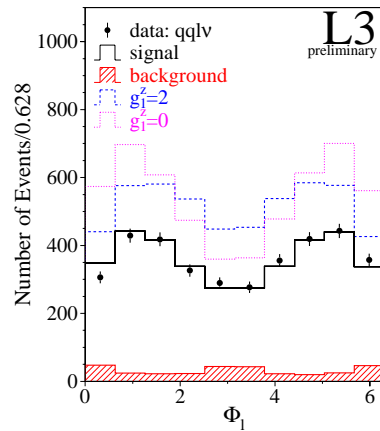
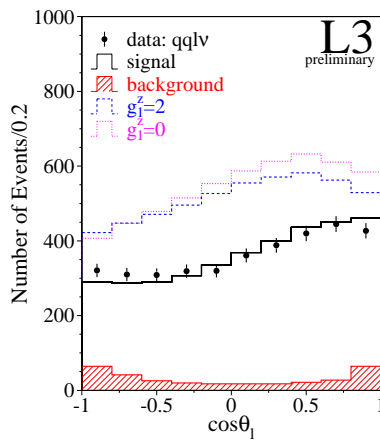


*qqqq*

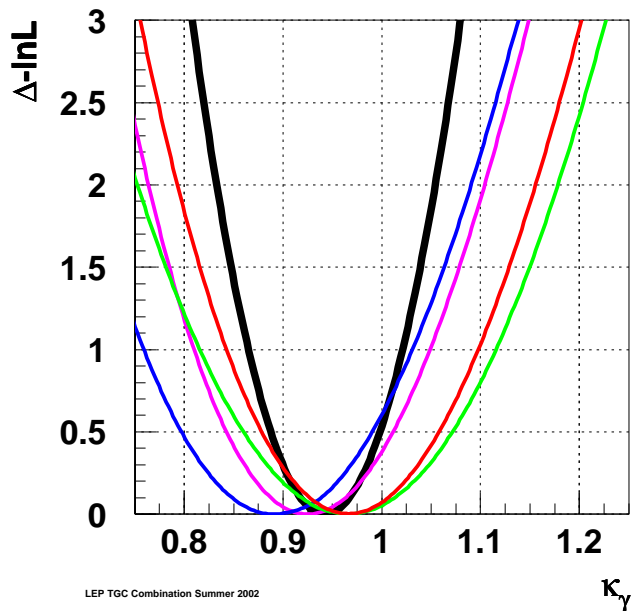
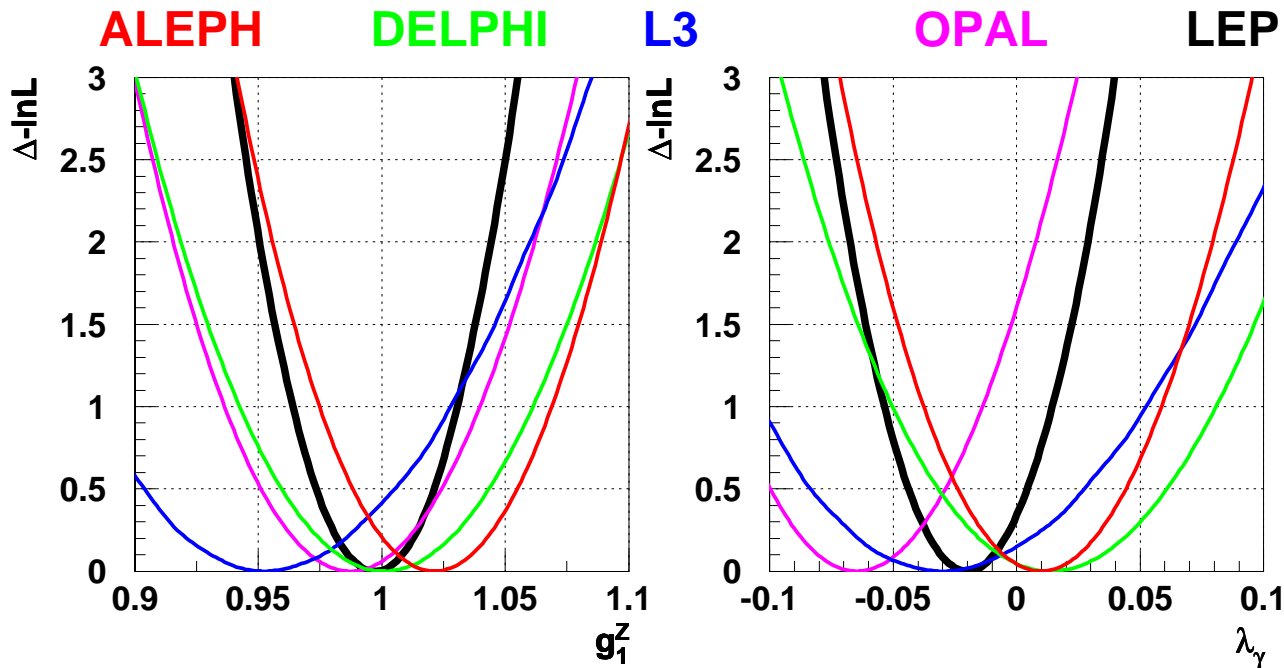
- Jet assignment ambiguity

- Folded decay distributions

*qqlv*



# LEP combined cTGC Results

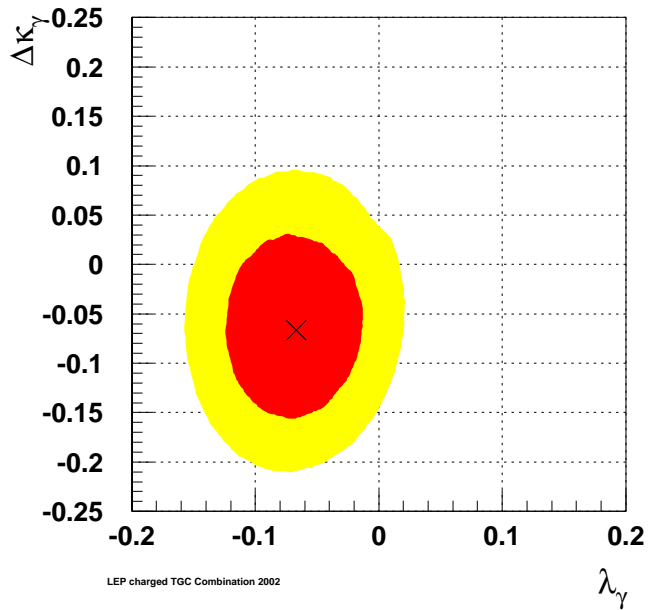
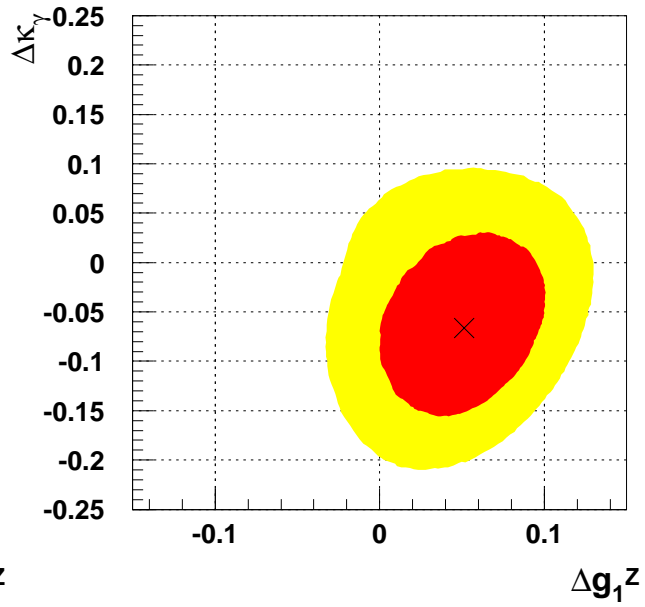
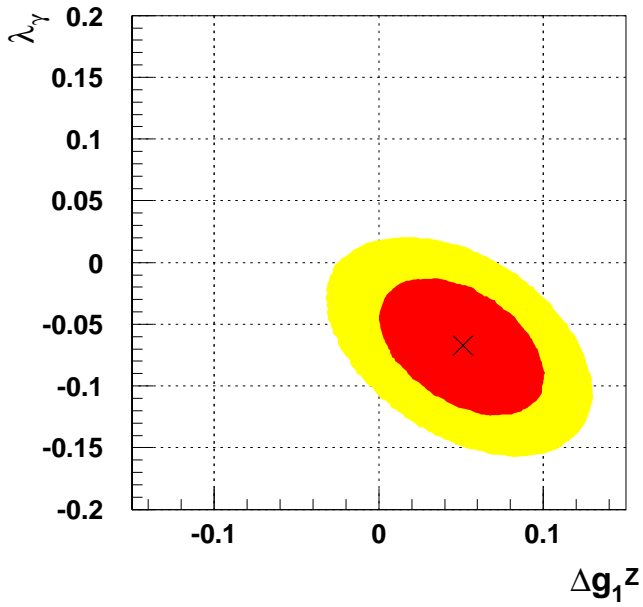


LEP preliminary

$$\begin{aligned} \kappa_\gamma &= 0.943 \quad +0.055 \\ &\quad \quad \quad -0.055 \\ \lambda_\gamma &= -0.020 \quad +0.024 \\ &\quad \quad \quad -0.024 \\ g_1^Z &= 0.998 \quad +0.023 \\ &\quad \quad \quad -0.025 \end{aligned}$$

- Theory uncertainty for  $\mathcal{O}(\alpha_{em})$  corrections gives largest contribution to systematic error

# LEP combined cTGC Results - 3D fits



DELPHI L3 OPAL 3D Fit - Preliminary

- 95% c.l.
- 68% c.l.
- × 3d fit result

$$\kappa_\gamma = 0.933^{+0.061}_{-0.059}$$

$$\lambda_\gamma = -0.067^{+0.036}_{-0.038}$$

$$g_1^Z = 1.051^{+0.031}_{-0.032}$$



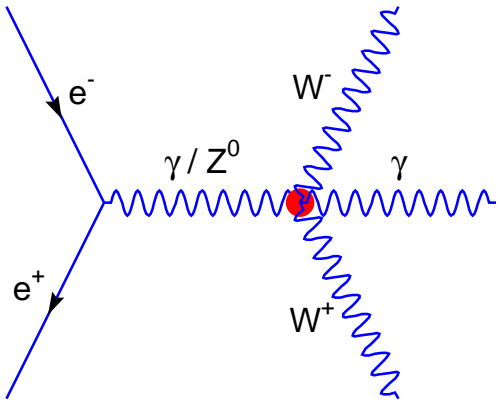
# Quartic Gauge Couplings

- Consider ‘genuine’ quartic gauge couplings
  - Assume
    - Lorentz invariance
    - $U(1)_{em}$
    - Use  $SU(2) \times U(1)$  operators
    - New physics scale is high (dim-6 operators)
- $\Rightarrow 2 WW\gamma\gamma + 2 ZZ\gamma\gamma + 1 WWZ\gamma$  parameters

$$\{a_0^W, a_c^W, a_0^Z, a_c^Z, a_n\}$$

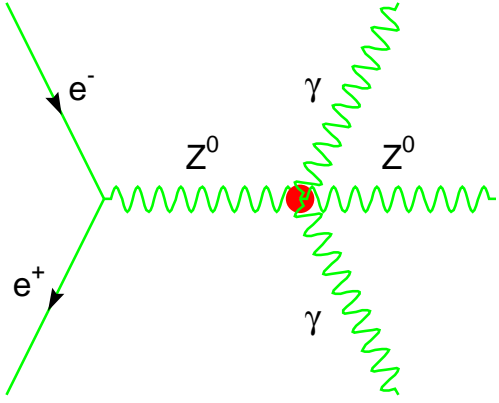
- $a_n$  is CP violating

# QGC physics at LEP2



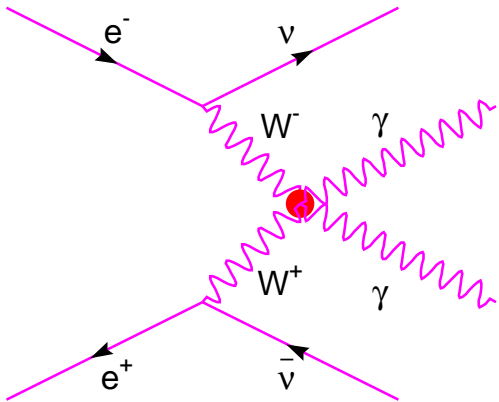
$WW\gamma$  ( $a_0^W, a_c^W, a_n$ )

- $qqqq\gamma$
- $qq\nu\gamma$



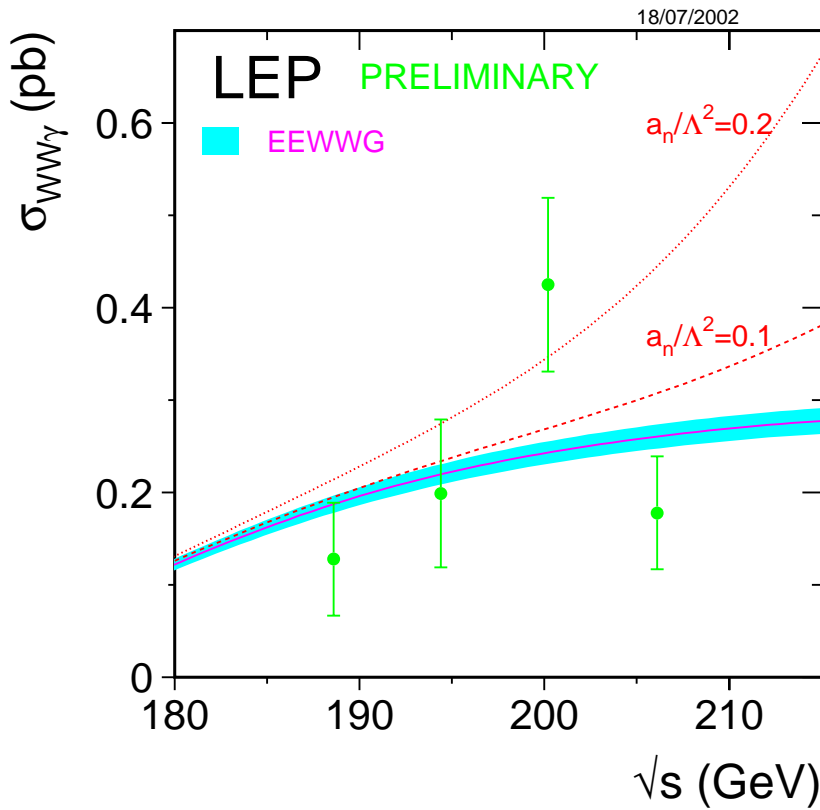
$Z\gamma\gamma$  ( $a_0^Z, a_c^Z$ )

- $qq\gamma\gamma$
- $\nu\nu\gamma\gamma$



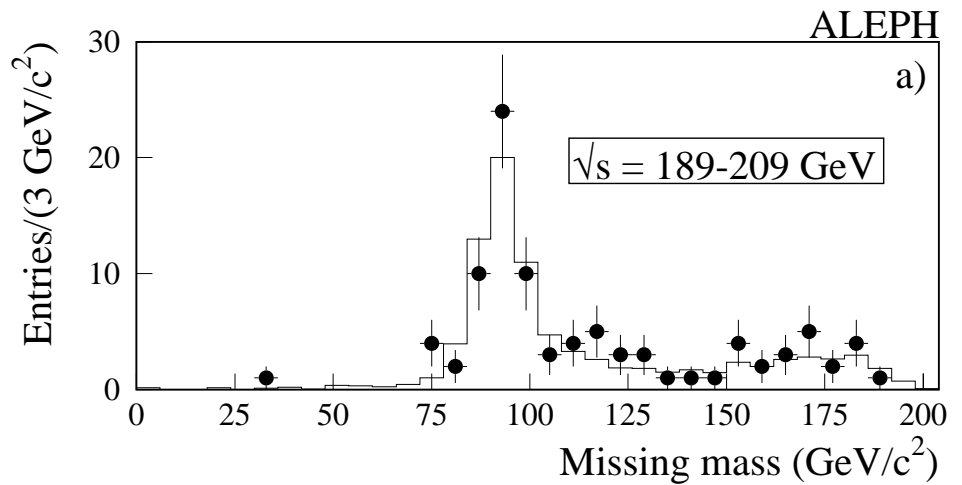
$\nu\nu\gamma\gamma$  ( $a_0^W, a_c^W$ )

# $a_0^W$ , $a_c^W$ and $a_n$ Measurements



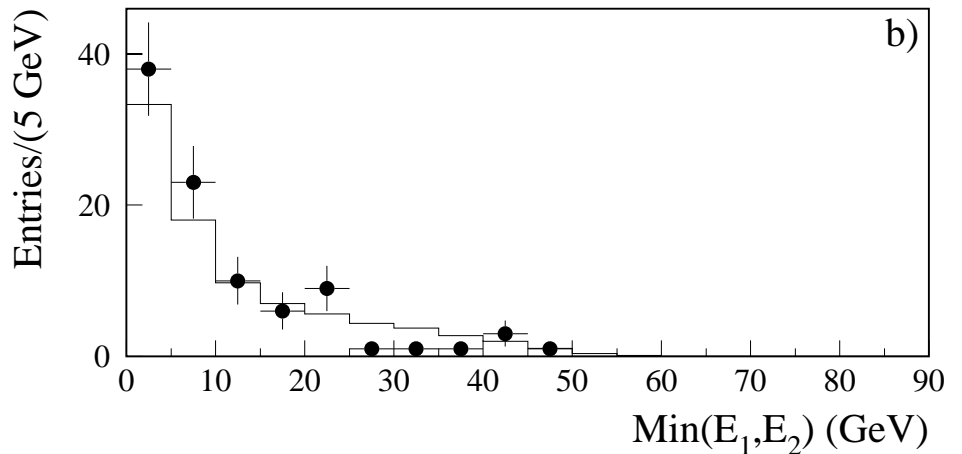
WW $\gamma$

● Hard, isolated  $\gamma$



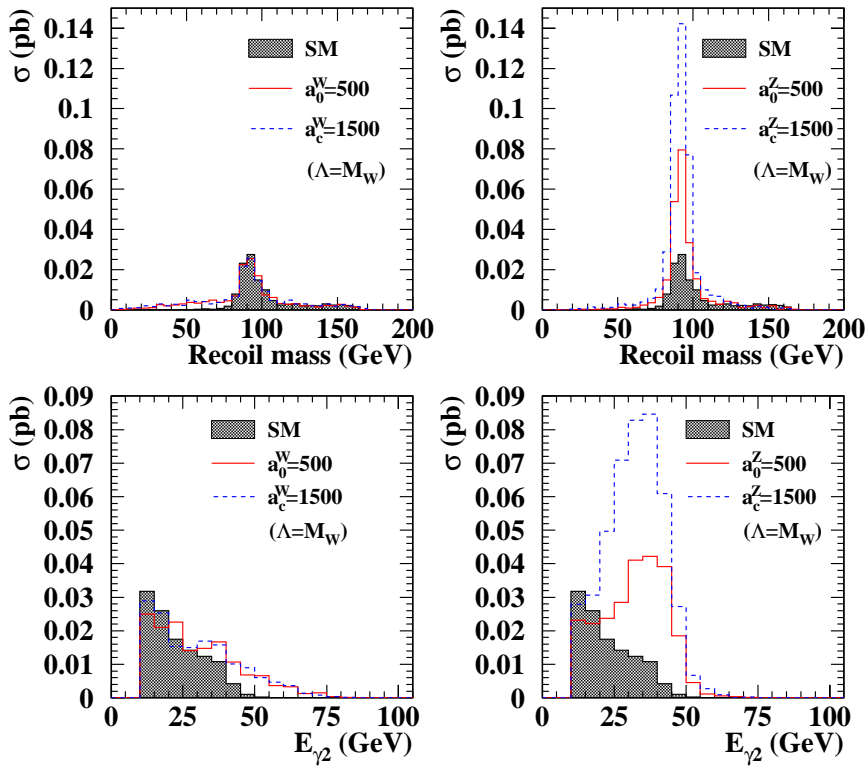
$\nu\nu\gamma\gamma$

● Radiative return



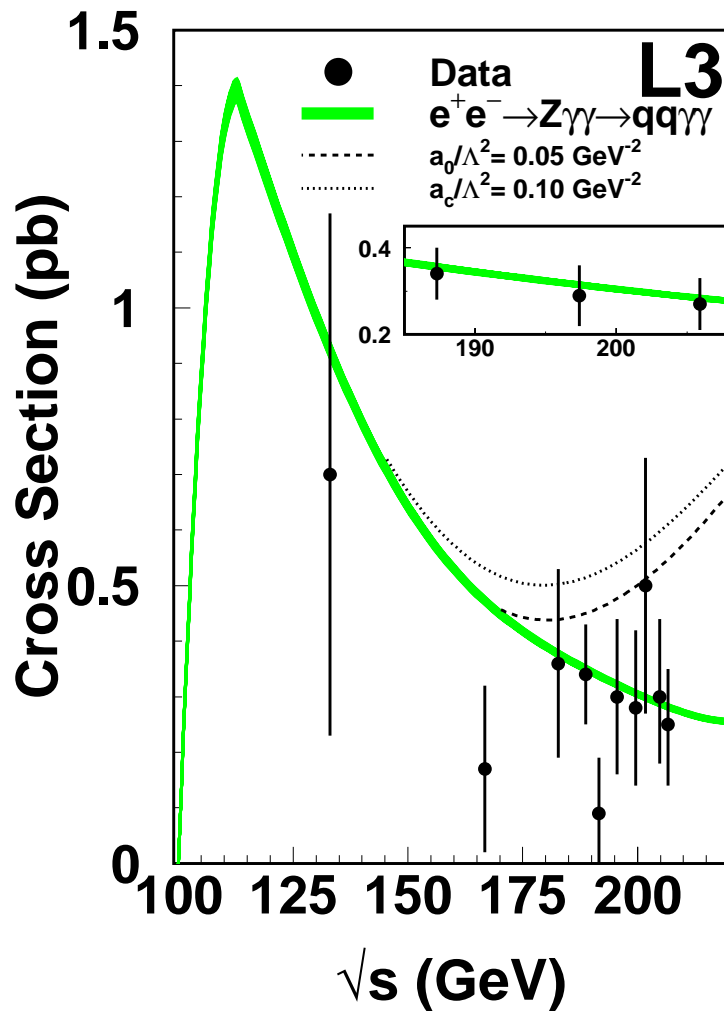
# $a_0^Z$ and $a_c^Z$ Measurements

OPAL preliminary



$\nu\nu\gamma\gamma$

$qq\gamma\gamma$

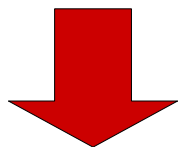
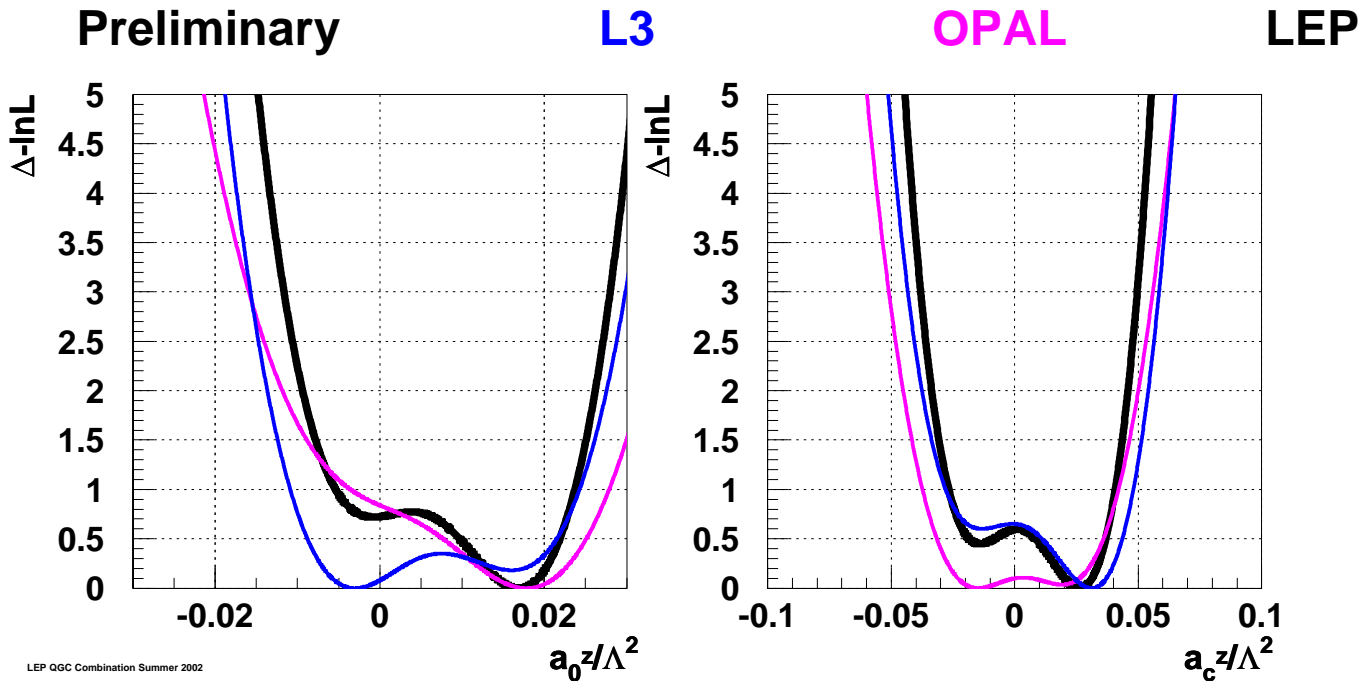


# LEP Combined QGC Results

- 95% confidence level limits

	DELPHI	L3	OPAL
$a_0^W$	$[-0.018, 0.018]$	$[-0.015, 0.015]$	$[-0.054, 0.052]$
$a_c^W$	$[-0.057, 0.030]$	$[-0.048, 0.026]$	$[-0.15, 0.14]$
$a_n$	$[-0.16, 0.12]$	$[-0.14, 0.13]$	$[-0.61, 0.57]$

Combination expected soon



	L3	OPAL	LEP Combined
$a_0^Z$	$[-0.037, 0.054]$	$[-0.045, 0.050]$	$[-0.033, 0.046]$
$a_c^Z$	$[-0.014, 0.027]$	$[-0.012, 0.031]$	$[-0.009, 0.026]$

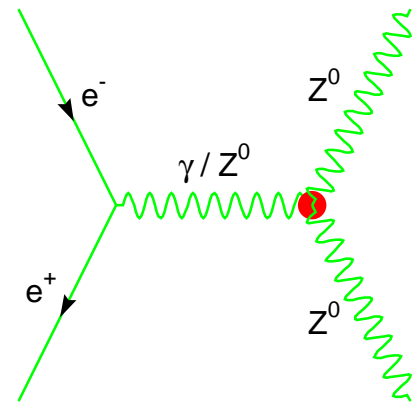
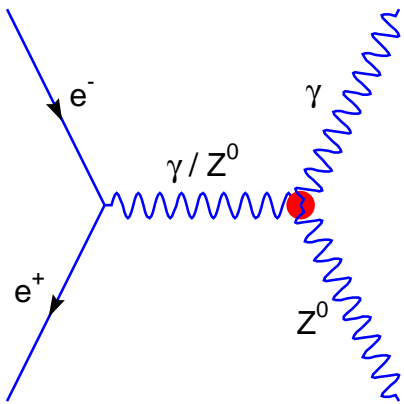
# Neutral Triple Gauge Couplings

- Assume

- Lorentz invariance
- $U(1)_{em}$
- Bose symmetry

$\Rightarrow 4 Z\gamma\gamma^* + 4 Z\gamma Z^* + 2 ZZ\gamma^* + 2 ZZZ^*$  parameters

	CP even	CP odd
$Z\gamma\gamma^*$	$h_3^\gamma, h_4^\gamma$	$h_1^\gamma, h_2^\gamma$
$Z\gamma Z^*$	$h_3^Z, h_4^Z$	$h_1^Z, h_2^Z$
$ZZ\gamma^*$	$f_5^\gamma$	$f_4^\gamma$
$ZZZ^*$	$f_5^Z$	$f_4^Z$



- $qq\gamma$
- $\nu\nu\gamma$

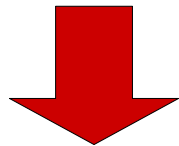
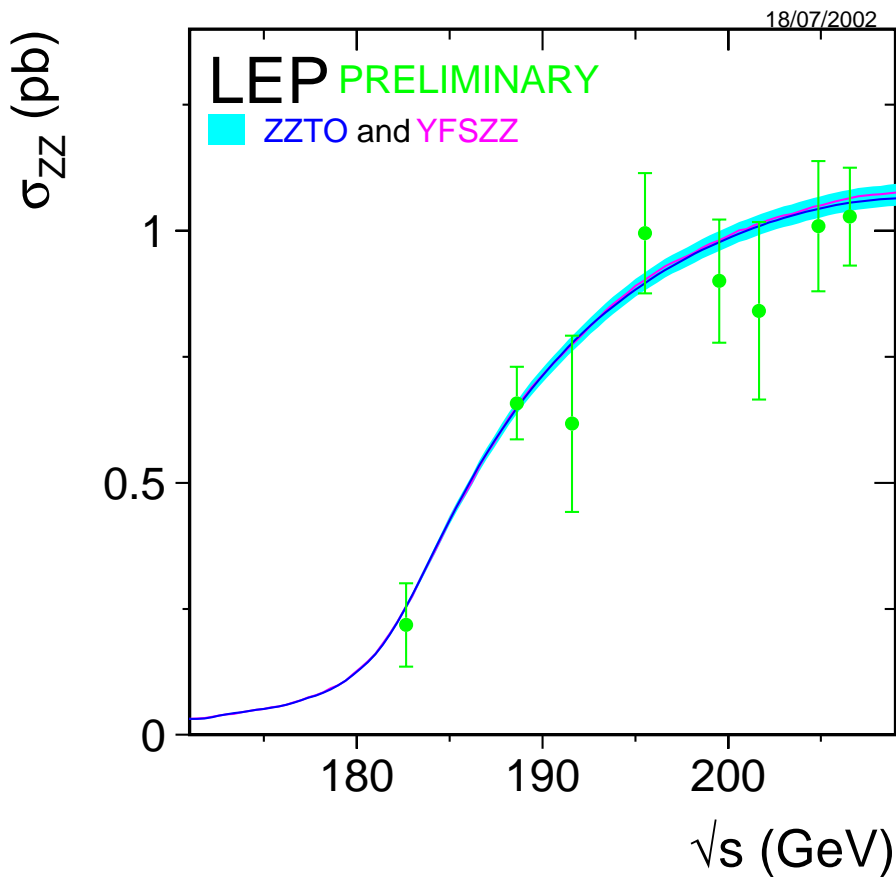
- all 4f decay modes

# LEP Combined nTGC Results

- 95% confidence level limits

$h_1^\gamma$	[-0.056, +0.055]
$h_2^\gamma$	[-0.045, +0.025]
$h_3^\gamma$	[-0.049, +0.008]
$h_4^\gamma$	[-0.002, +0.034]

$h_1^Z$	[-0.13, +0.13]
$h_2^Z$	[-0.078, +0.071]
$h_3^Z$	[-0.20, +0.070]
$h_4^Z$	[-0.05, +0.012]



$f_4^\gamma$	[-0.17, +0.19]
$f_5^\gamma$	[-0.36, +0.40]

$f_4^Z$	[-0.31, +0.28]
$f_5^Z$	[-0.36, +0.39]

## Conclusion

- Preliminary GC results from LEP  
(CERN-EP / 2002-091)
- All values consistent with SM
- cTGC
  - Expect reductions in  $\mathcal{O}(\alpha_{em})$  systematic
  - CP violating cTGC measurements ongoing
- QGC
  - Combination of  $a_0^W$ ,  $a_c^W$  and  $a_n$
- nTGC
- Future for GC physics
  - Final LEP combinations soon
  - Tevatron, LHC, NLC, ...